



Polarized Nucleon Targets for Europe

JRA8 in the 6th European Framework Program

1st Meeting, Bochum, November 29/30, 2004

- Spin effects in:
 - * lepton-nucleon interaction
 - * nucleon-nucleon interaction
 - * the decay of radioactive nuclei

- Miroslav Finger

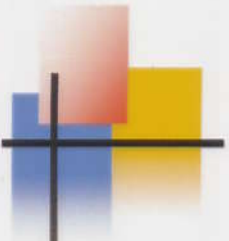
- Charles University, Prague



Spin Physics Experiments

lepton-nucleon interaction

- Hadron structure and hadron spectroscopy
- HELP program at CERN
- HMC program at CERN
- COMPASS program at CERN



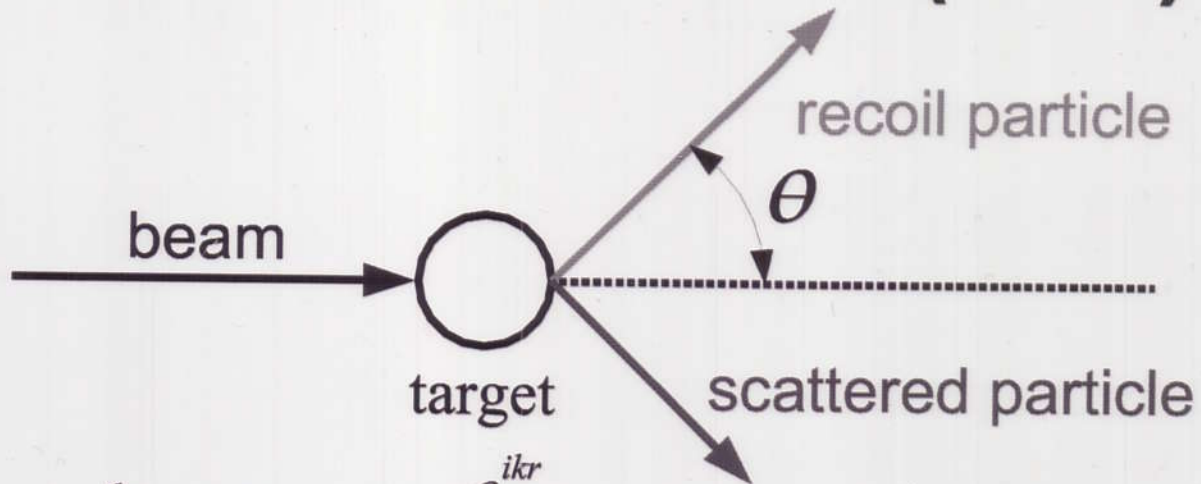
Spin Physics Experiments

nucleon-nucleon interaction

- 1. Spin effects in Elastic NN-scattering
 - *Complete experiment in NN interactions*
- 2. Spin effects in Inelastic (inclusive and exclusive) NN-interactions
- 3. Spin effects in NA-interactions
 - *Nuclear medium modification of*
 - *NN-interactions*

Elastic Scattering Formalism

SPIN PARTICLES ($\frac{1}{2} \frac{1}{2}$)



$$\psi \simeq \zeta_i e^{ikz} + M(\theta, \varphi) \zeta_i \frac{e^{ikr}}{r}$$

$$f(\theta) = \sum_{l=0}^{\infty} (2l+1) a_l P_l(\cos(\theta)) = \sum_{l=0}^{\infty} \sqrt{4\pi(2l+1)} a_l Y_l^0(\theta)$$

$$\zeta_i = \begin{pmatrix} a \\ b \\ c \\ d \end{pmatrix}$$

spin matrix

$$M(\theta, \varphi) = \begin{pmatrix} m_{11} & m_{12} & m_{13} & m_{14} \\ m_{21} & m_{22} & m_{23} & m_{24} \\ m_{31} & m_{32} & m_{33} & m_{34} \\ m_{41} & m_{42} & m_{43} & m_{44} \end{pmatrix} \text{scattering matrix}$$

$$\zeta_f = M(\theta, \varphi) \zeta_i$$

$$\sigma(\theta, \varphi) = \frac{1}{g} \text{Tr } M^+ M$$

differential cross section

Elastic Scattering Formalism

SPIN PARTICLES ($\frac{1}{2} \frac{1}{2}$)

Spin density matrix P_i (beam+target)

$$P_f = M \cdot P_i \cdot M^+$$

$$\sigma(\theta, \varphi) = \frac{\text{Tr } M P_i M^+}{\text{Tr } P_i} = \frac{\text{Tr } P_f}{\text{Tr } P_i}$$

$$\langle \bar{O} \rangle = \frac{\text{Tr } (P O)}{\text{Tr } P}$$

$$\begin{aligned} M(\theta, \varphi) = & A + B(\sigma_1 \cdot \sigma_2 + 1) + C(\sigma_1 + \sigma_2) \cdot \vec{n} \\ & + D(\sigma_1 - \sigma_2) \cdot \vec{n} + E(\sigma_1 \cdot \vec{K})(\sigma_2 \cdot \vec{K}) \\ & + G(\sigma_1 \cdot \vec{P})(\sigma_2 \cdot \vec{P}) \end{aligned}$$

$$\vec{n} = \vec{k}' + \vec{k}$$

$$\vec{K} = \vec{k}' - \vec{k}$$

$$\vec{P} = \vec{n} \times \vec{K}$$



Spin Effects In NN Interactions

generalized cross-section

$$\begin{aligned} \Sigma(P_b, P_T, P_1, P_2) = & I_1 I_2 d\delta/d\Omega \{ [1 + A_{ooio} P_{Bi} + A_{oook} P_{Tk} + A_{ooik} P_{Bi} P_{Tk}] \\ & + P_1 [P_{pooo} + P_{Bi} D_{poto} + P_{Tk} K_{pook} + P_{Bi} P_{Tk} M_{poik}] n_{1p} \\ & + P_2 [P_{oqoo} + P_{Bi} K_{oqio} + P_{Tk} D_{oqok} + P_{Bi} P_{Tk} M_{oqik}] n_{1p} \\ & + P_1 P_2 [C_{pqoo} + P_{Bi} C_{qpio} + P_{Tk} C_{pqok} + P_{Bi} P_{Tk} C_{pqik}] n_{1p} n_{2q} \} \end{aligned}$$

$\vec{p} \odot \hat{n}$
590 MeV
 $\sim 10 \mu\text{A}$

PIREX $P_p \sim 75\%$

$\vec{p} \odot \hat{n}$

SOL1

$\vec{p}$

Production target
12cm C
 $\vec{a}^{12}\text{C} \rightarrow \vec{n} + X$

MAG

MAG

$\vec{n}$

γ

Collimator
2m

Pb filter

Spin
precession
mag

$\hat{n}$

$\hat{k}$

$\hat{s}$

MON1
M1 M2 X

CH₂ Pb

0,5m

PPT

S12

$\vec{p}$

MWPC

A

MON2
L

R

13,75m

$I = 5 \cdot 10^6 \text{ n/s} \cdot \text{cm}^2$
 $P_n \sim 20 - 40$

$\vec{p}$

20 ns

1 ns

γ

n

γ

n

γ

n

γ

n

Ambiguity

Ambiguity

Ambiguity

X_{ijkl}

X_{SRBT}

1-spin parameter

A_{00B0}
 A_{000T} } analysing power

2-spin parameter

A_{00BT} correlation

D_{0R0T} depolarisation

K_{0RB0} transfer

3-spin parameter

N_{0RBT}

PPT

100 cm³

$\hat{n}; \hat{k}; \hat{s}$

butanol

50 mK

$\tau \gg 1000$ hod

$P_T \sim 70\%$

$B_H = 0.8$ T

$B_P = 2.5$ T

Trigger:

Monitor: $\bar{X} \cdot S12 \cdot \bar{V} \cdot \sum N \cdot 3 JD$

MWPC: # of hits
slope $\nless$ } 3 μ s

Spin flipped every second

Angular settings:

$60^\circ < \theta_{cm} < 120^\circ$

$100^\circ < \theta_{cm} < 160^\circ$



SPIN EFFECTS IN NN INTERACTIONS

TRIUMF	200 – 520 MeV	<u>PSI</u> :	NN – NN	elastic
LAMPF	480 – 800 MeV		NN – NNII	inelastic
SATURNE II	800 – 1100 MeV		np → np	
PSI	200 – 580 MeV		np → np π^0	
			np → pp π^-	
			np → nn π^+	
			np → $\alpha\pi^0$	
JINR	1.0 – 6.0 GeV		np → np γ	

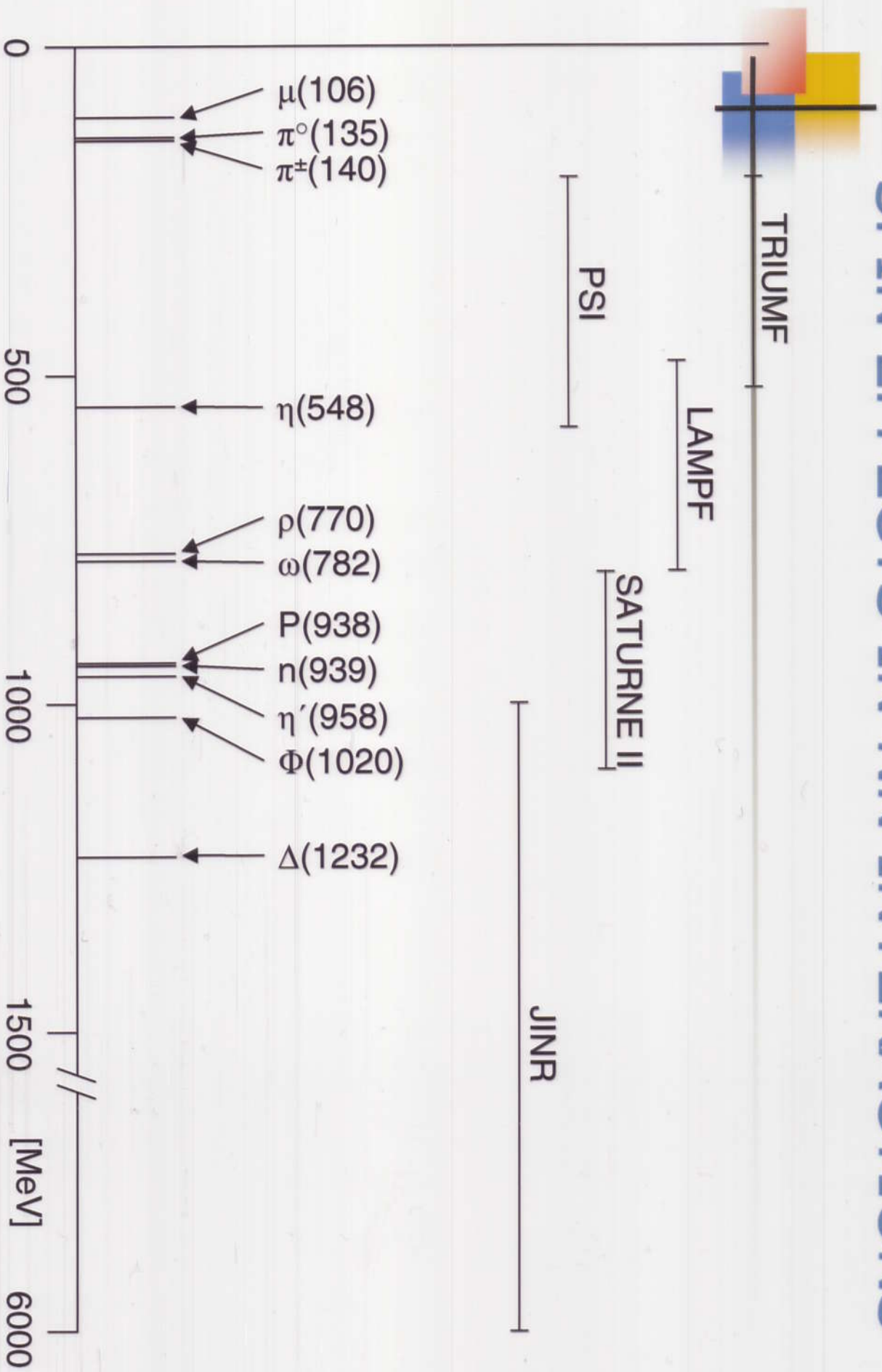


Spin Physics Experiments

JINR LNP - Department of Hadron Physics

1. LTNO	- DUBNA	Decay of Oriented Nuclei
2. $\vec{n} \cdot \vec{p}$	- PRAGUE	$E_n \cong 16 \text{ MeV}$
3. $\vec{n} \cdot \vec{p}$	- PSI Villigen	$E_n \cong 200 - 590 \text{ MeV}$
4. $\vec{n} \cdot \vec{p}$	- SACLAY	$E_n \cong 300 - 1150 \text{ MeV}$
5. $\vec{n} \cdot \vec{p}$	- DUBNA	$E_p \cong 1000 - 6000 \text{ GeV}$
6. $p \cdot \vec{p}$	- PROTVINO	$E_p \cong 70 \text{ GeV}$
7. $\pi^- \cdot \vec{p}$	- PROTVINO	$E_{\pi^-} \cong 40 \text{ GeV}$
8. $\vec{\mu} \cdot \vec{p}$	- CERN	$E_{\mu^-} \cong 100 - 200 \text{ GeV}$

SPIN EFFECTS IN NN INTERACTIONS



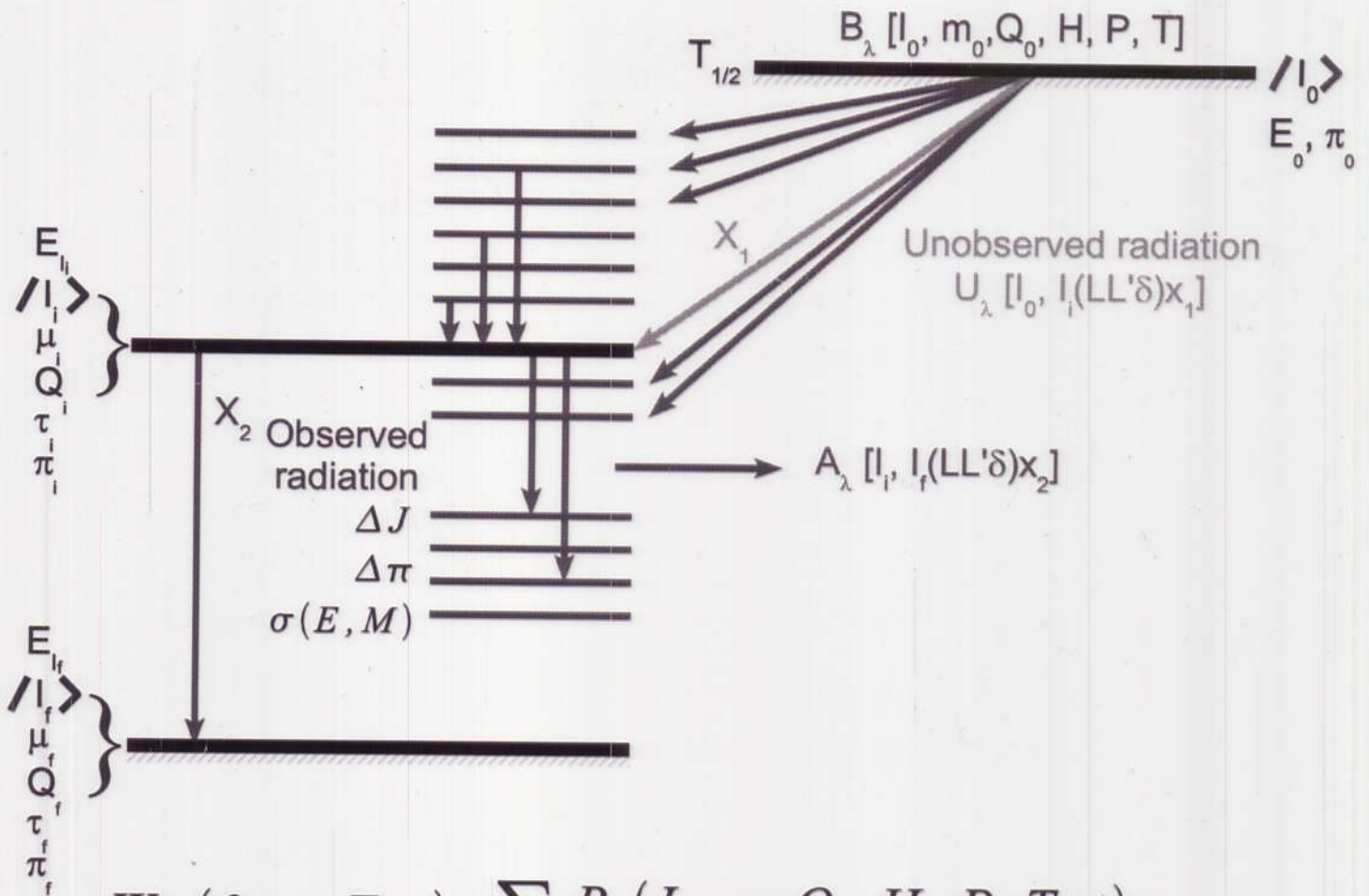


Spin Physics Experiments

in the decay of radioactive nuclei

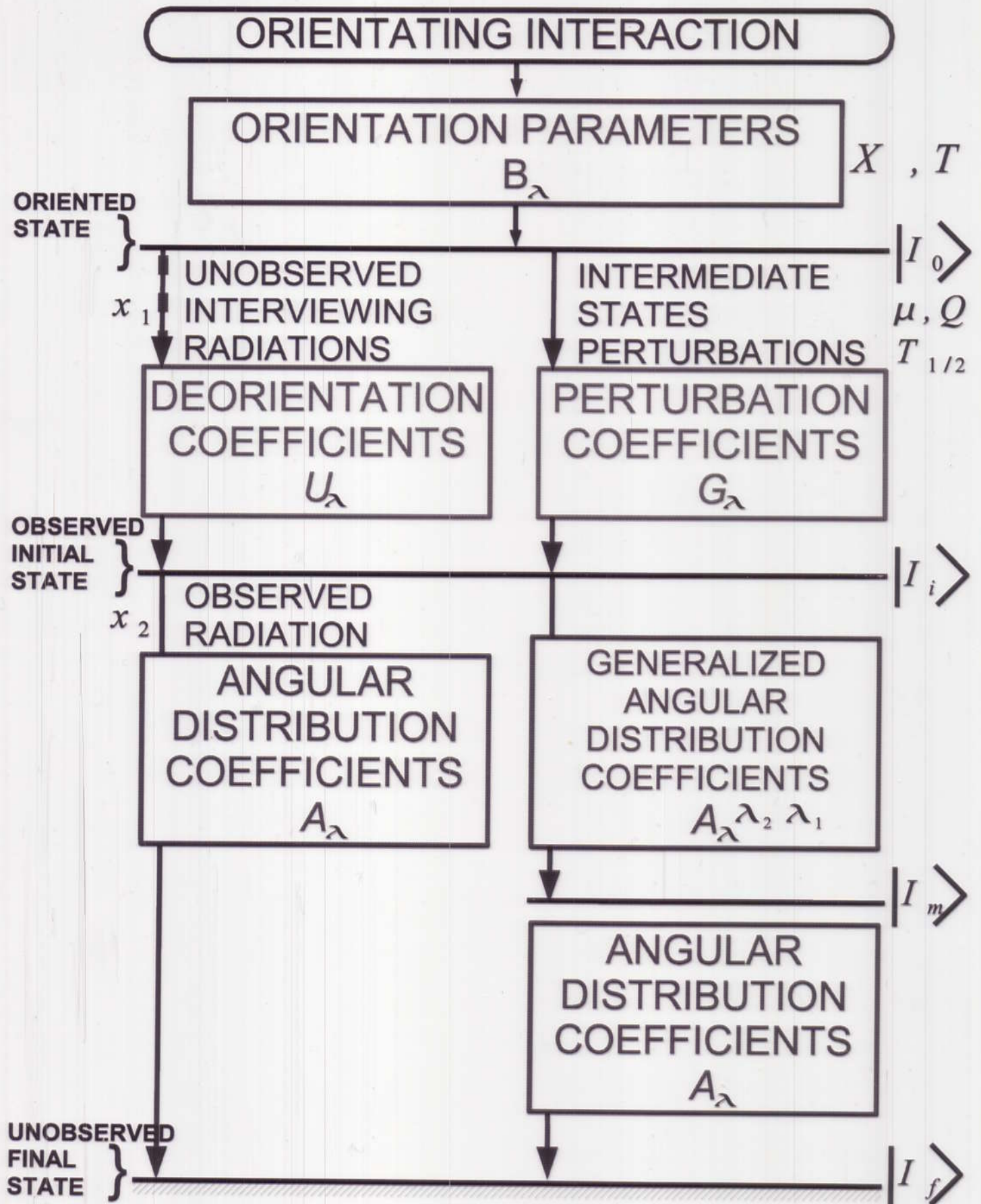
- 1. Radioactive nuclei as the laboratory
 - for symmetry tests
- 2. Supersymmetry concept in nuclear
 - physics

Parent State Orientation



$$W_{x_2}(\theta, \varphi, T, t) = \sum_{\lambda} B_{\lambda}(I_0, \mu_0, Q_0, H, P, T, t) \cdot U_{\lambda}[I_0 I_i(LL'\delta)_{x_1}] \cdot A[I_i I_f(LL'\delta)_{x_2}] \cdot Q_{\lambda} \cdot G_{\lambda} \cdot P(\cos \theta)$$

Nuclear Orientation of Radioactive Nuclei



$$W_{x_2}(\theta, \varphi, T, t) = \sum_{\lambda} B_{\lambda}(X, T, I_0 \mu, Q) \cdot U_{\lambda}[I_0 I_i (LL' \lambda)_{x_1}] \cdot A_{\lambda}[I_i I_f (LL' \delta)_{x_2}] \cdot Q_{\lambda} \cdot P_{\lambda}(\cos \theta)$$

Nuclear Orientation

Using Hyperfine Interactions at Low Temperatures

NUCLEI



J

spin

μ

magnetic moment

Q

electric quadrupole moment

$$(2J+1) \quad m = -J, \dots, +J \quad E_m$$

Hyperfine Interactions

$$H = H_M + H_Q = -\vec{\mu} \vec{H} + \frac{e Q V_{zz}}{4J(2J-1)} [J_z^2 - J(J+1)]$$

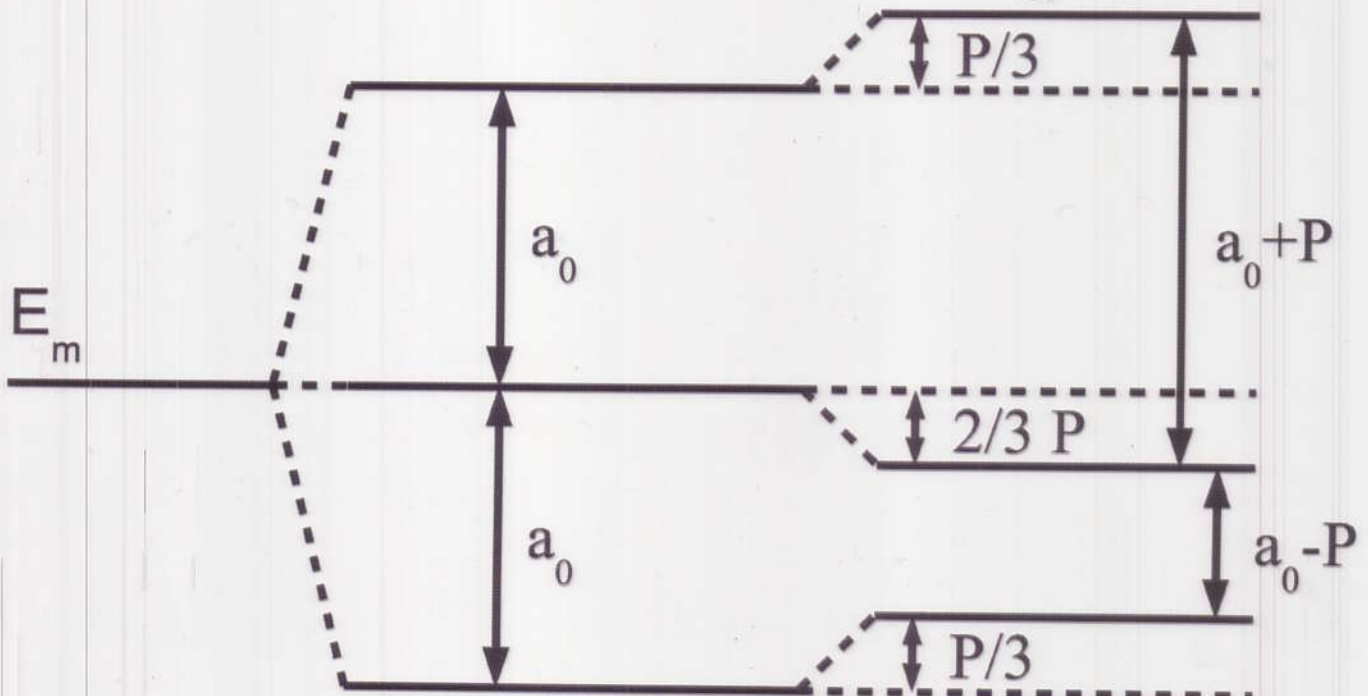
$$E_m = -\frac{\mu H_{eff}}{J} \cdot m + \frac{3eQ V_{zz}}{4J(2J-1)} [m^2 - \frac{J}{3}(J+1)]$$

$$E_m = -a_0 m + P [m^2 - \frac{1}{3} J(J+1)]$$

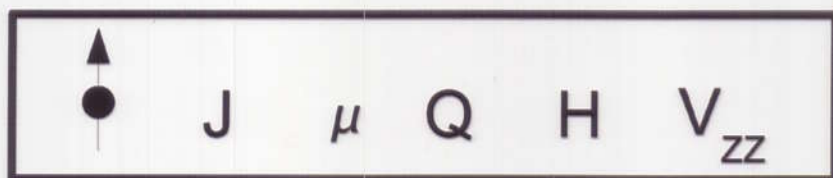
$$\Delta E_{m,m-1} = [-a_0 + P(2m-1)]$$

Example

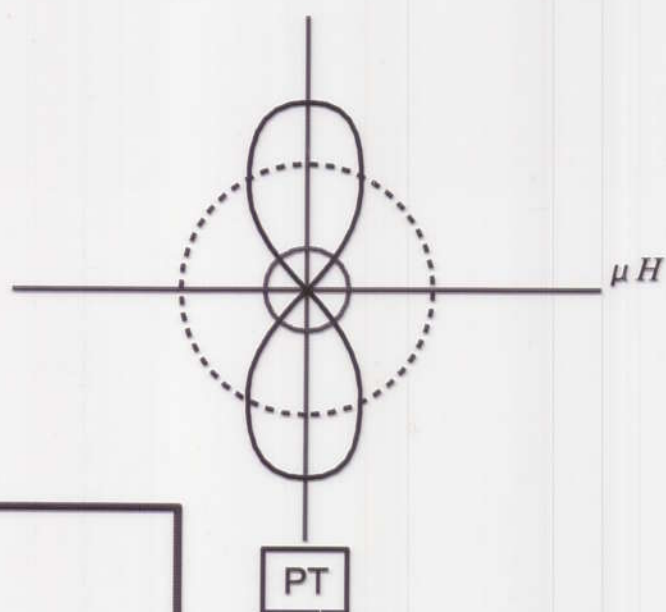
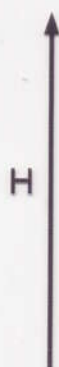
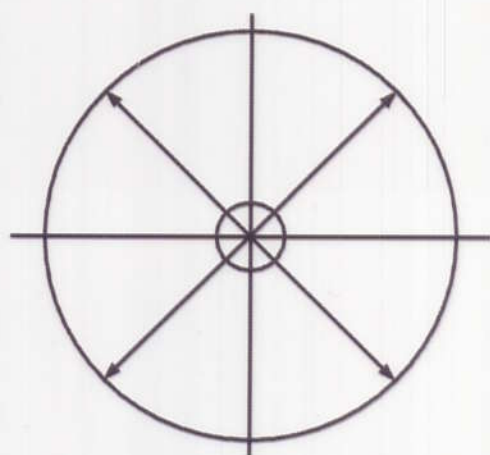
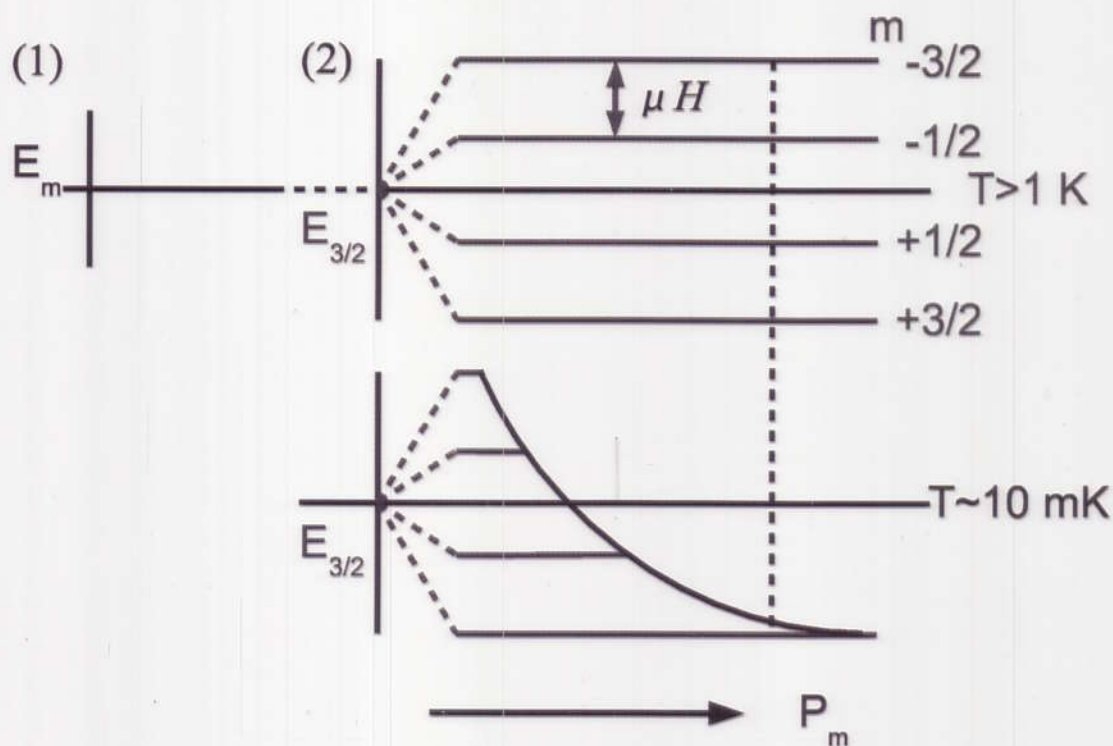
$$J=1 \quad ; \quad 2J+1=3 \quad ; \quad m=-1,0,1 \quad ; \quad a_0 > 0 \quad ; \quad P > 0$$



Low Temperature Nuclear Orientation of Radioactive Nuclei



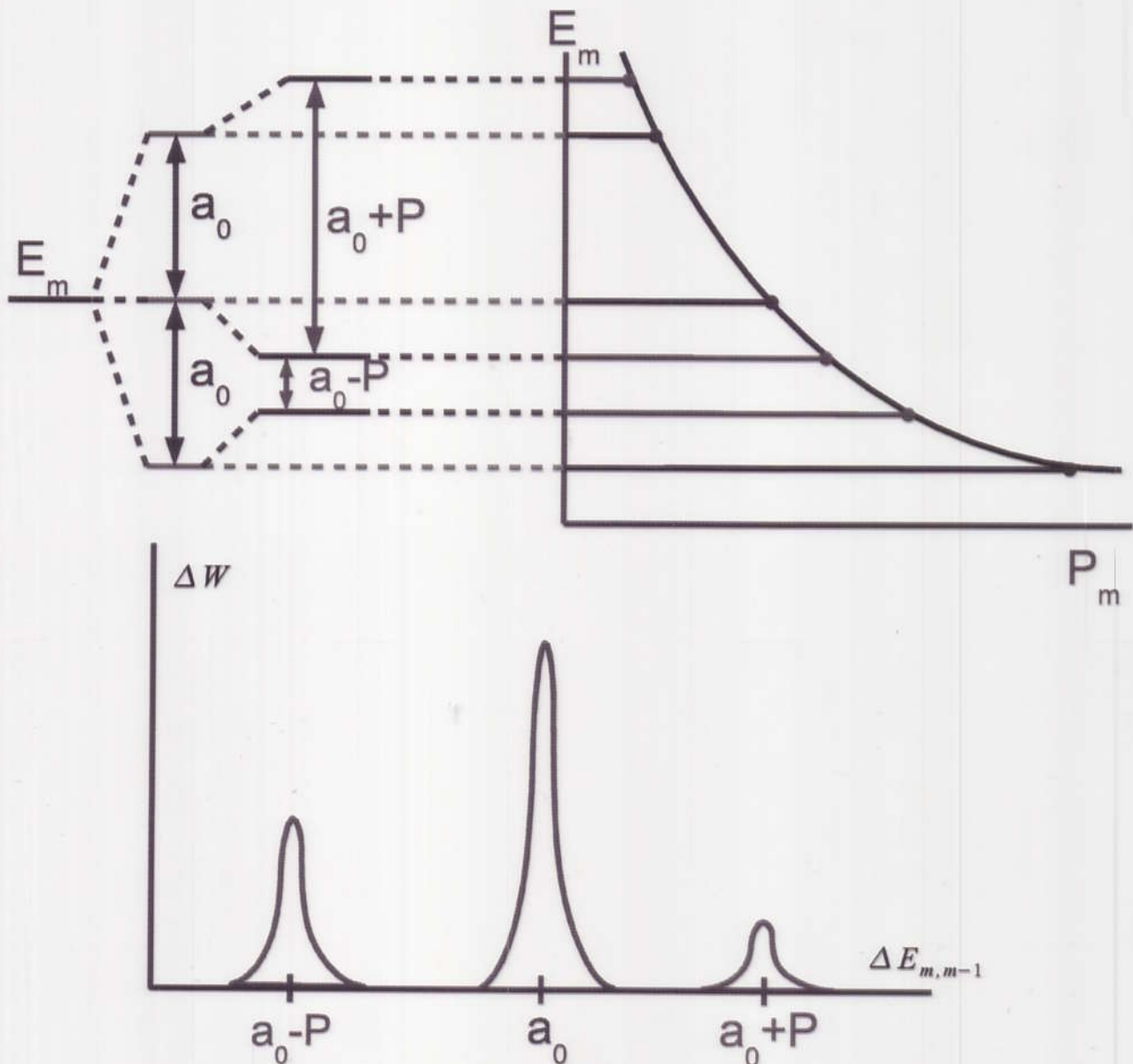
$$E_J \rightarrow E_m \quad (2J+1)$$



$$P \sim e^{\frac{-\mu H}{JkT}}$$

Hyperfine Interactions at Low Temperatures

$$P_m = \frac{\exp\left(\frac{-E_m}{kT}\right)}{\sum_m \exp\left(\frac{-E_m}{kT}\right)}$$



$$W(\theta, T) = \sum_i \sum_{\lambda} E_{i\lambda} B_{\lambda}(T) \cdot U_{\lambda} \cdot A_{\lambda} \cdot Q_{\lambda} P_{\lambda}(\cos \theta)$$

$$B_{\lambda}(T) = [(2\lambda + 1)(2J + 1)]^{1/2} \sum_m (-1)^{J+m} \begin{pmatrix} J & J & \lambda \\ -m & m & 0 \end{pmatrix} P_m$$

Nuclear Magnetic/Electric Resonance on Oriented Nuclei

Angular distribution

$$\text{I. } \gamma_{CP} \quad W(\theta, \tau) = \frac{d\Omega}{8\pi} \sum_{\lambda} B_{\lambda}(J_0) \tau^{\lambda} A_{\lambda}(\gamma) P_{\lambda}(\cos \theta)$$

$$W(\theta, Q_3) = \frac{d\Omega}{4\pi} \sum_{\lambda} B_{\lambda}(J_0) A_{\lambda}(\gamma) [1 + (-1)^{\lambda} + (1 - (-1)^{\lambda} Q_3)] \cdot P(\cos \theta)$$

no dependence on $\pi(E, M)$

$$\text{II. } \gamma_{LP} \quad W(\theta, \psi, Q_1) = \frac{d\Omega}{8\pi} \sum_{\lambda} B_{\lambda}(J_0) [A_{\lambda}(\gamma) P_{\lambda}(\cos \theta) + 2 A^{\lambda} \Lambda\{\frac{\lambda-2}{\lambda+2}\}]$$

$$\Gamma(E)=0 \quad \Gamma(M)=1$$

$$\text{III. } \gamma \quad W(\theta) = \frac{d\Omega}{4\pi} \sum_{\lambda} B_{\lambda}(J_0) A_{\lambda}(\gamma) P_{\lambda}(\cos \theta)$$

Nuclear Magnetic/Electric Resonance on Oriented Nuclei

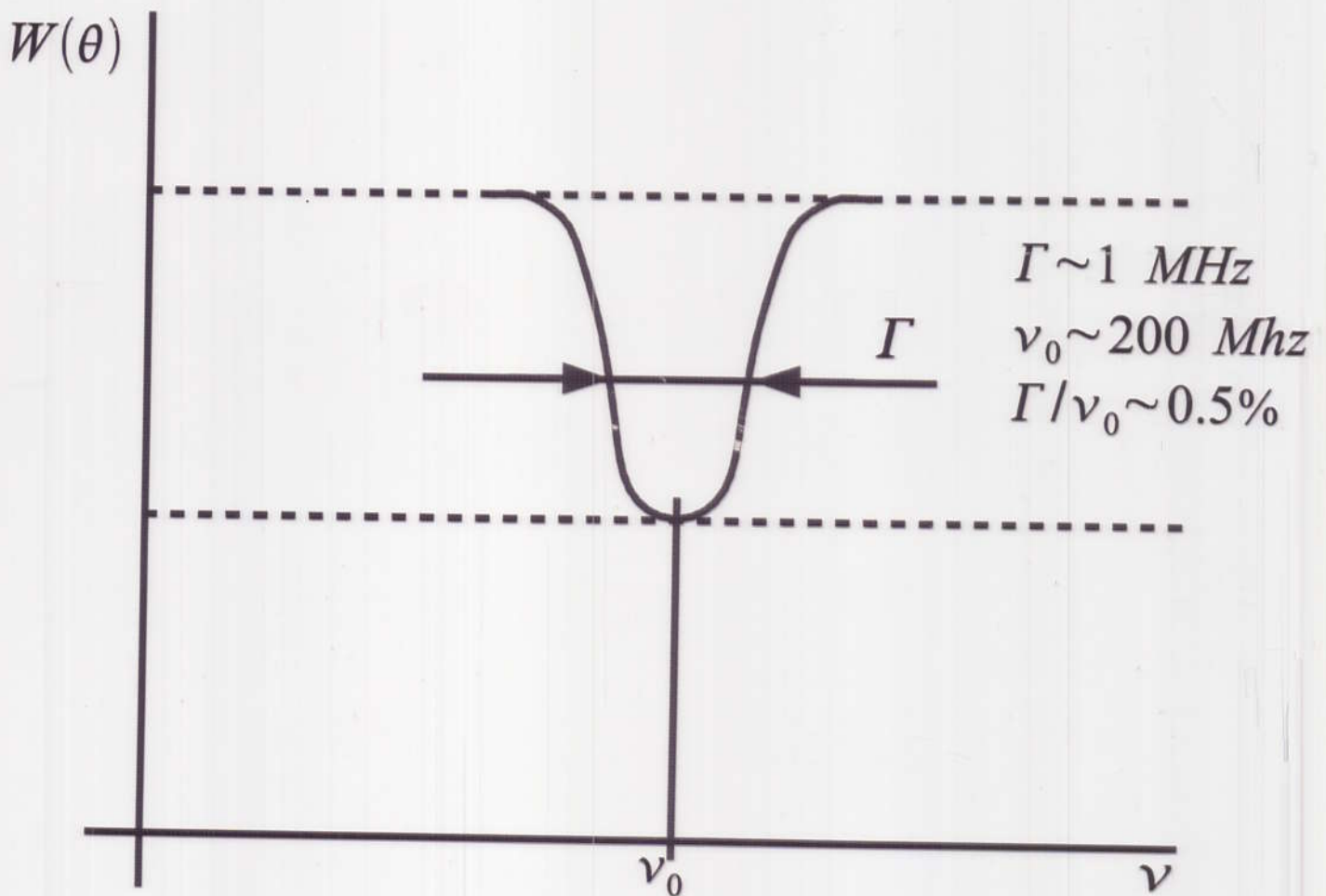
NMR/ON

NQR/ON

$$h\nu = \Delta E_{m,m-1} = |-a_0 + P(2m-1)|$$

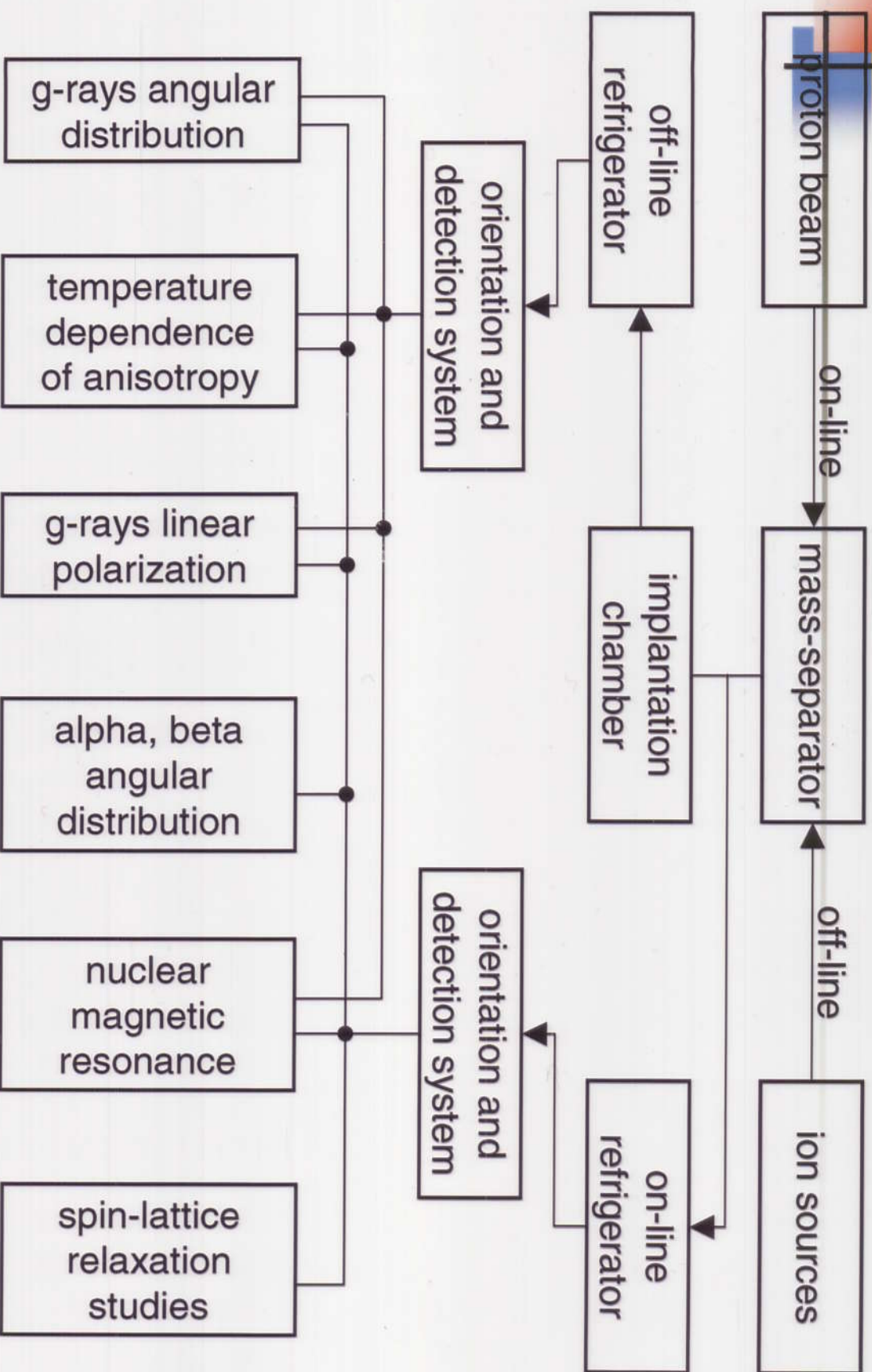
$$\vec{H}_{eff} = \vec{H}_{hf} + (1+S)\vec{H}_{ext} - D\vec{M} \quad \text{in ferromagnets}$$

$$h\nu = \left| -\left(\frac{\vec{\mu}}{J}\right) \{ \vec{H}_{hf} + (1+S)\vec{H}_{ext} - D\vec{M} \} + P(2m-1) \right|$$



SPIN – ISOLDE-YASNAPP-2 FACILITY

AVAILABLE EXPERIMENTS





SUSY CONCEPTS FOR NUCLEI

