

*New Insights for QCD  
from AdS/CFT  
and  
Novel Tests of QCD at GSI*

*Stan Brodsky, SLAC*

***Trento GSI-FAIR Workshop***

# Quantum Chromodynamics (QCD)

- Quantum Chromodynamics is the fundamental theory of hadron and nuclear physics, as fundamental as Quantum Electrodynamics is to atomic physics and chemistry!
- In fact: limit  $\text{QCD}(N_C \rightarrow 0) = \text{Quantum Electrodynamics (QED)}$
- Although we know the QCD Lagrangian, we have only begun to understand its remarkable properties and features.
- Novel QCD Phenomena: “hidden color”, “color transparency”, “quark-gluon plasma”, “intrinsic charm” anomalous heavy quark phenomena, diffraction, spin effects
- Remarkable new insights from AdS/CFT, the duality between conformal field theory and Anti-de Sitter Space

# *Hadron Dynamics at the Amplitude Level*

- DIS studies have primarily focussed on probability distributions: integrated and unintegrated.
- Test QCD at the amplitude level: Phases, multi-parton correlations, spin, angular momentum, exclusive amplitudes
- Impact of ISI and FSI: Single Spin Asymmetries, Diffractive Deep Inelastic Scattering, Shadowing, Antishadowing
- Hadron wavefunctions: Fundamental QCD Dynamics
- Remarkable new insights from AdS/CFT, the duality between conformal field theory and Anti-de Sitter Space

# Novel Tests of QCD at GSI

## Polarized 15 GeV stored anti-proton beam

- Characteristic momentum scale of QCD: 300 MeV
- Many Tests of AdS/CFT predictions possible
- Exclusive channels: Conformal scaling laws, quark-interchange
- proton-antiproton scattering: test fundamental aspects of nuclear force
- Color transparency: Coherent color effects
- Nuclear Effects, Hidden Color, Anti-Shadowing
- Anomalous heavy quark phenomena
- Spin Effects:  $A_N, A_{NN}$



**Testing quantum chromodynamics with antiprotons.**

[Stanley J. Brodsky \(SLAC\)](#) . SLAC-PUB-10811, Oct 2004. 92pp.

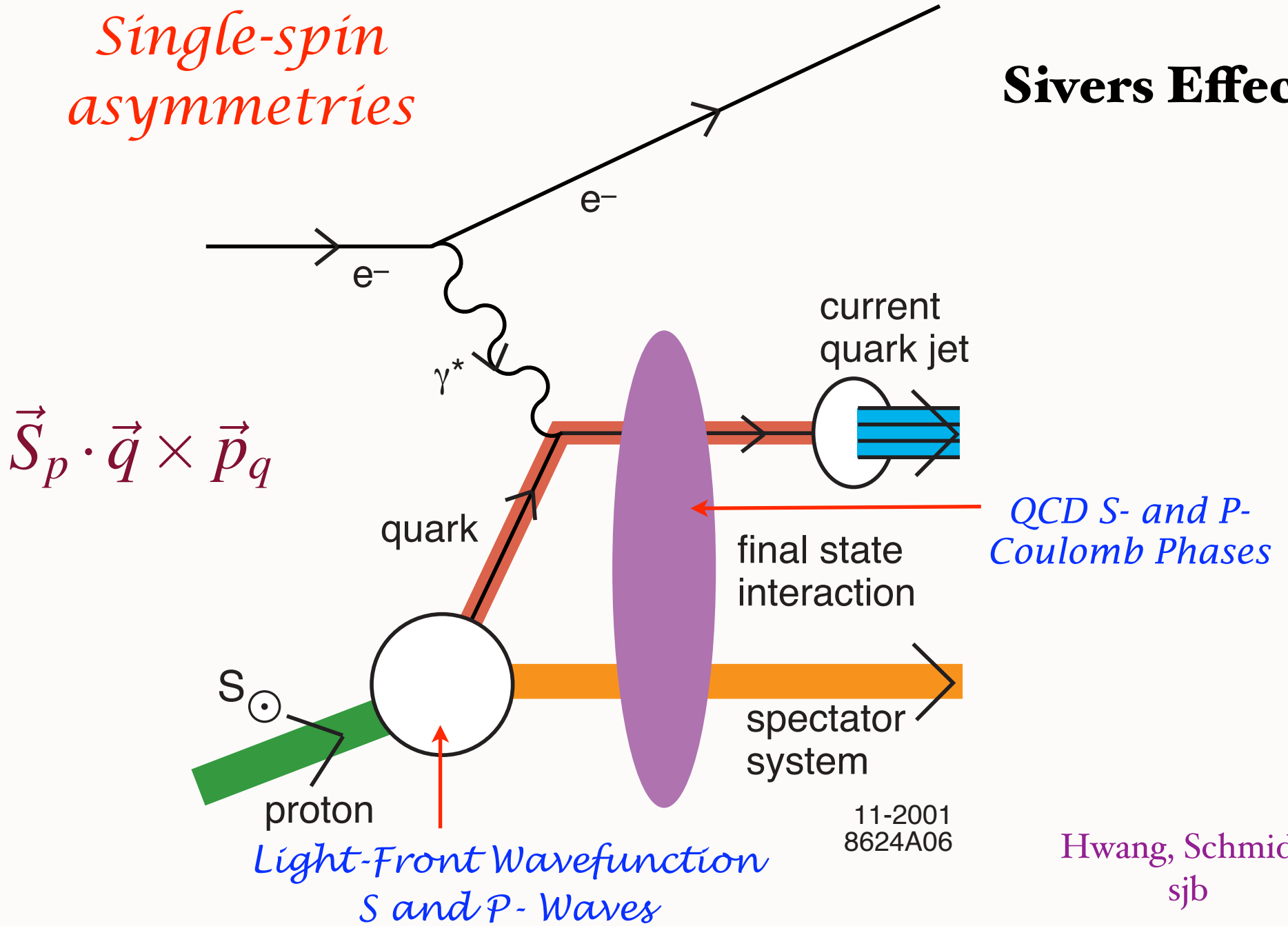
Published in \*Varenna 2004, Hadron physics\* 345-422

e-Print Archive: [hep-ph/0411046](#)

Novel QCD Phenomenology, [Part 1](#), [Part 2](#), [Part 3](#), [Part 4](#), [Part 5](#), [Part 6](#), [Part 7](#), [Part 8](#),  
International School of Physics Enrico Fermi, Varenna, Italy, 6/2004

*Single-spin asymmetries*

**Sivers Effect**



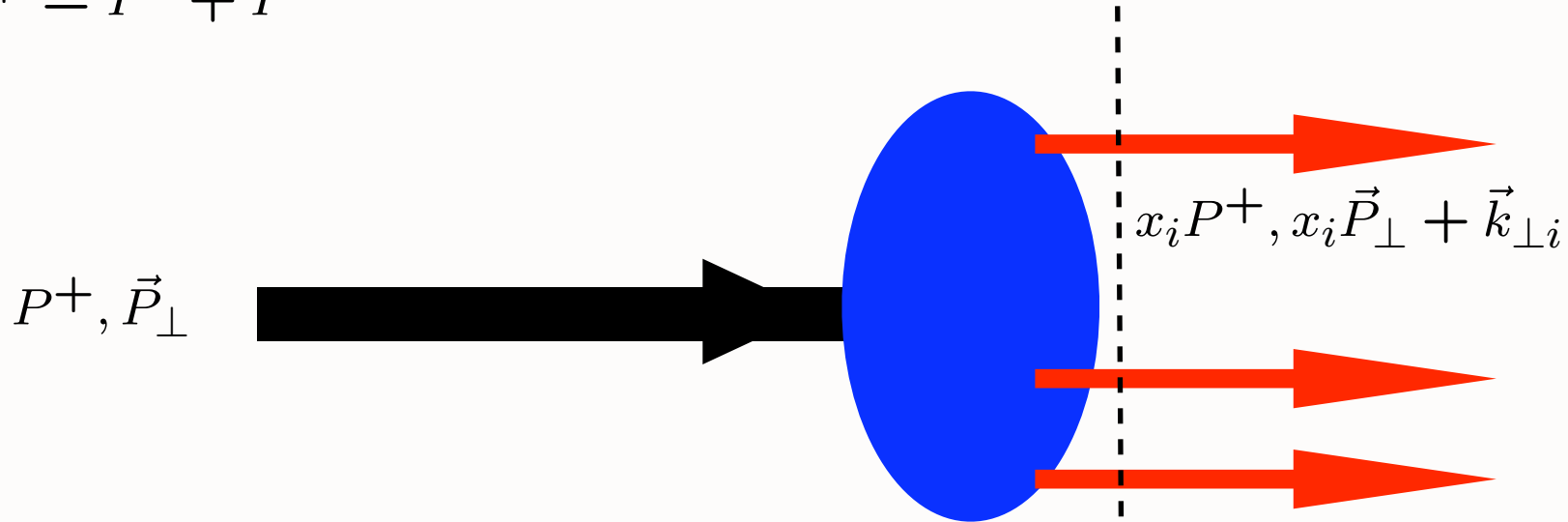
11-2001  
8624A06

Hwang, Schmidt.  
sjb

# Light-Front Wavefunctions

$$P^+ = P^0 + P^z$$

Fixed  $\tau = t + z/c$



$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

$$\sum_i^n x_i = 1$$

$$\sum_i^n \vec{k}_{\perp i} = \vec{0}_\perp$$

*Invariant under boosts! Independent of  $P^\mu$*

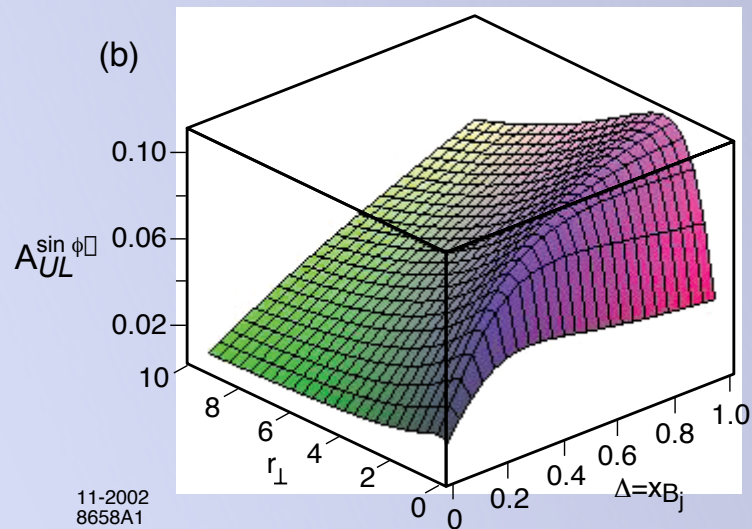
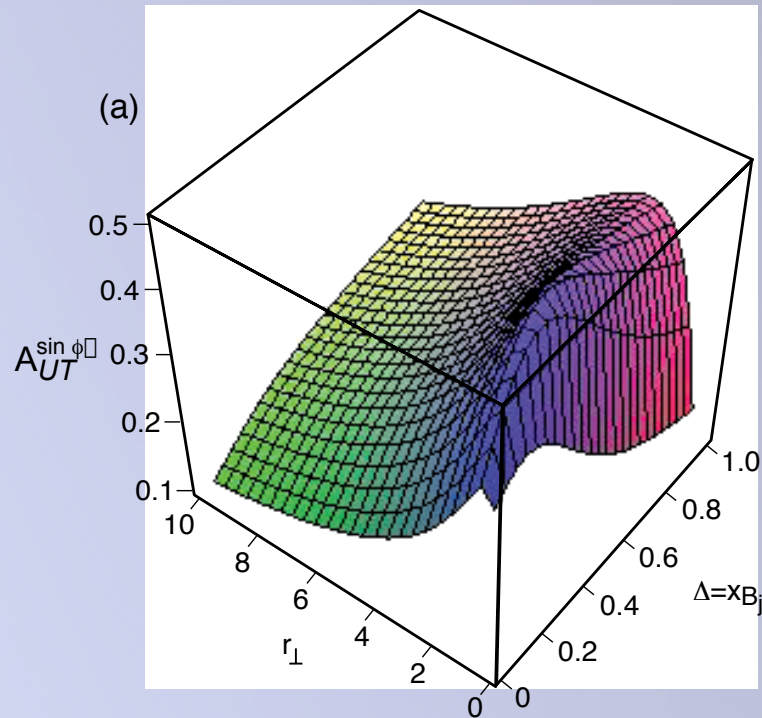
# Final-State Interactions Produce

*T-Odd (Sivers Effect)*  $\mathbf{i} \vec{S} \cdot \vec{p}_{jet} \times \vec{q}$

- Bjorken Scaling!
- Arises from Interference of Final-State Coulomb Phases in S and P waves
- Relate to the quark contribution to the target proton anomalous magnetic moment
- Sum of Sivers Functions for all quarks and gluons vanishes. (Zero gravito-anomalous magnetic moment:  $B(0) = 0$ )

Hwang, Schmidt. sjb;  
Burkardt

# Prediction for Single- Spin Asymmetry



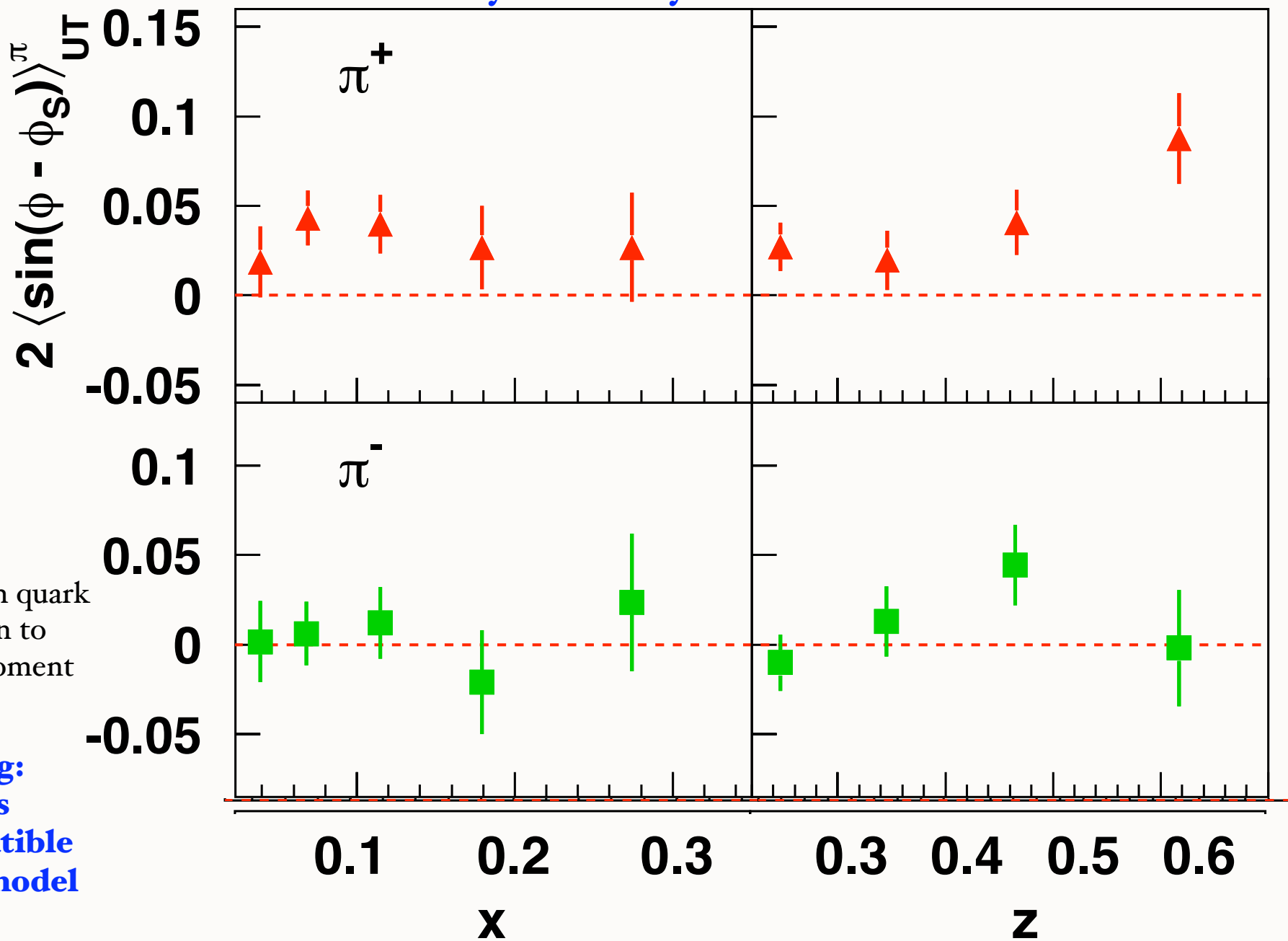
Hwang, Schmidt.  
sjb

Trento  
July 5, 2006

AdS/CFT, QCD, & GSI

Stan Brodsky, SLAC

# Sivers asymmetry from HERMES



SSA tracks with quark contribution to anomalous moment

**Gamberg:**  
**Hermes**  
data compatible with BHS model

AdS/CFT, QCD, & GSI

Stan Brodsky, SLAC

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July 5, 2006

# Key QCD Experiment at GSI

Measure single-spin asymmetry  $A_N$   
in Drell-Yan reactions

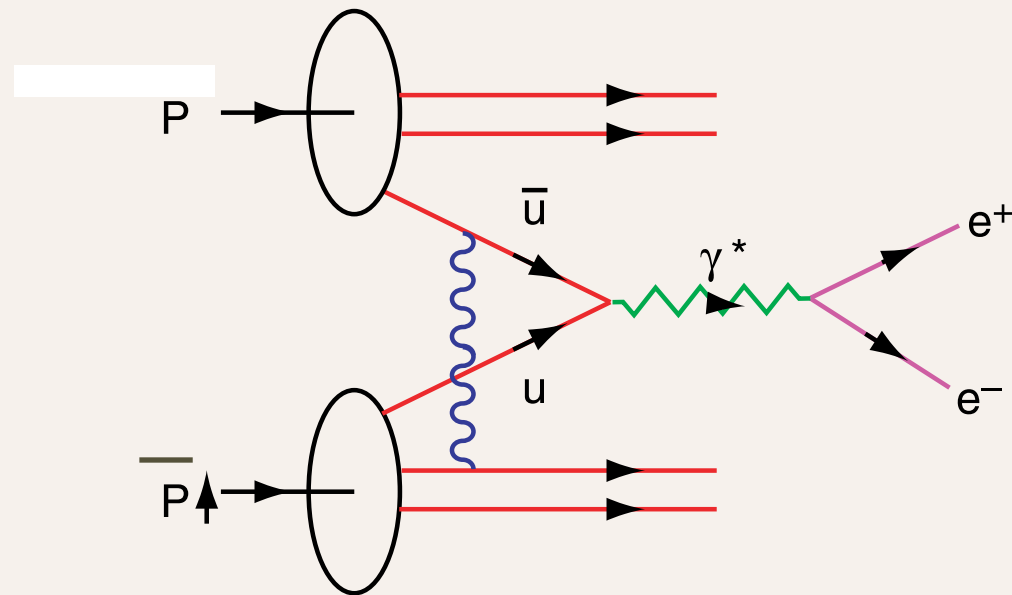
Leading-twist Bjorken-scaling  $A_N$   
from  $S, P$ -wave  
initial-state gluonic interactions

Predict:  $A_N(DY) = -A_N(DIS)$   
Opposite in sign!

$$Q^2 = x_1 x_2 s$$

$$Q^2 = 4 \text{ GeV}^2, s = 80 \text{ GeV}^2$$

$$x_1 x_2 = .05, x_F = x_1 - x_2$$



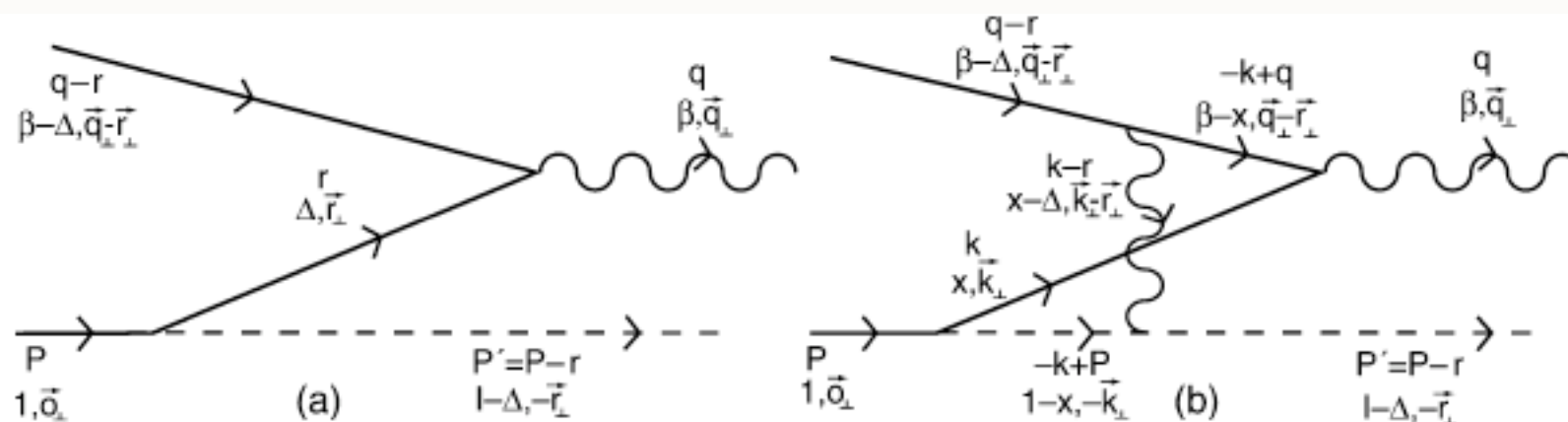
$$p\bar{p}_{\uparrow} \rightarrow l^+ l^- X$$

$\vec{S} \cdot \vec{q} \times \vec{p}$  correlation

# Initial-state interactions and single-spin asymmetries in Drell–Yan processes $\star$

Stanley J. Brodsky <sup>a</sup>, Dae Sung Hwang <sup>a,b</sup>, Ivan Schmidt <sup>c</sup>

Nuclear Physics B 642 (2002) 344–356

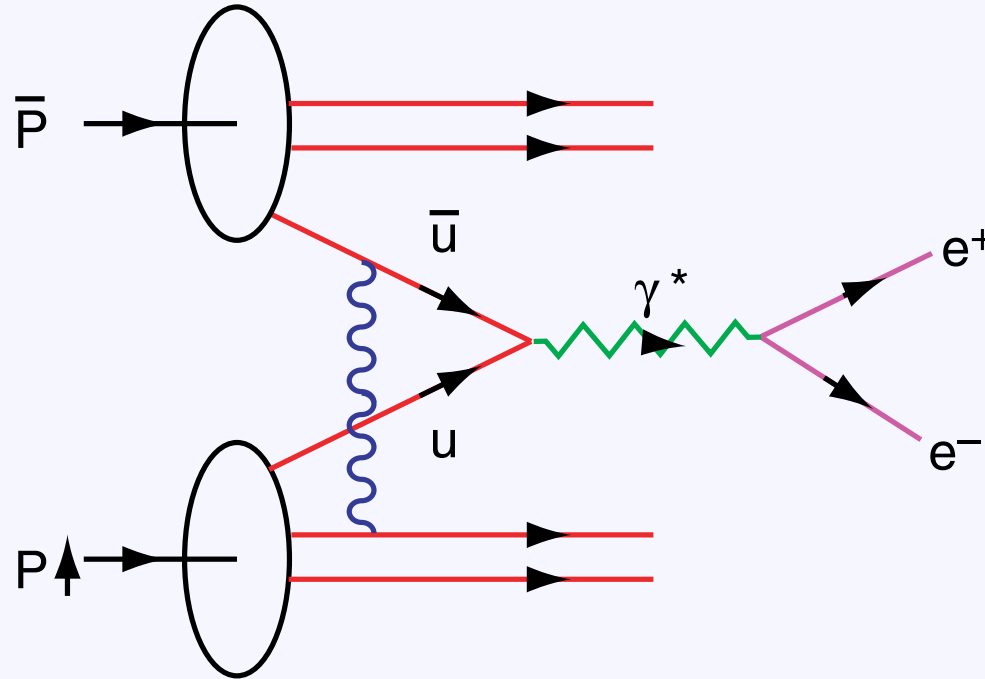


$$\mathcal{P}_y = -\frac{e_1 e_2}{8\pi} \frac{2(\Delta M + m)r^1}{[(\Delta M + m)^2 + \vec{r}_\perp^2]} \left[ \vec{r}_\perp^2 + \Delta(1-\Delta) \left( -M^2 + \frac{m^2}{\Delta} + \frac{\lambda^2}{1-\Delta} \right) \right] \\ \times \frac{1}{\vec{r}_\perp^2} \ln \frac{\vec{r}_\perp^2 + \Delta(1-\Delta) \left( -M^2 + \frac{m^2}{\Delta} + \frac{\lambda^2}{1-\Delta} \right)}{\Delta(1-\Delta) \left( -M^2 + \frac{m^2}{\Delta} + \frac{\lambda^2}{1-\Delta} \right)}.$$

Here  $\Delta = \frac{q^+}{2P \cdot q} = \frac{q^+}{2M\nu}$  where  $\nu$  is the energy of the lepton pair in the target rest frame.



# Key QCD Experiment at GSI



Single Spin Asymmetry In the Drell Yan Process

$$\vec{S}_p \cdot \vec{p} \times \vec{q}_{\gamma^*}$$

Quarks Interact in the Initial State

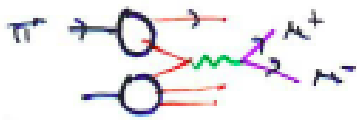
Interference of Coulomb Phases for  $S$  and  $P$  states

Produce Single Spin Asymmetry [Siver's Effect] Proportional  
to the Proton Anomalous Moment and  $\alpha_s$ .  
Opposite Sign to DIS! No Factorization

Collins;  
Hwang, Schmidt.  
sjb

## Drell-Yan Process and Higher Twist

$$\pi^- N \Rightarrow \gamma^* X \Rightarrow \mu^+ \mu^- X$$

$$\frac{1}{\sigma} \frac{d\sigma}{d\Omega_+} = 1 + \lambda \cos^2 \theta + \mu \sin 2\theta \cos \phi + \frac{\nu}{2} \sin^2 \theta \cos 2\phi$$


$$\lambda, \mu, \nu = f(x_L, Q^2, Q_s^2, s)$$

Leading twist PQCD predicts

$$\begin{aligned} \lambda &\approx 1 && + \mathcal{O}(\alpha_s) \\ \mu, \nu &\approx 0 && + \mathcal{O}(\alpha_s) \end{aligned}$$

Data:  $\lambda \rightarrow$  negative at  $x_L \rightarrow 1$  ?

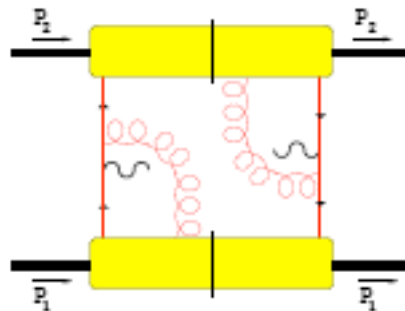
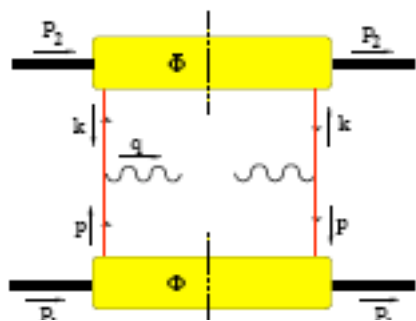
Large

$\mu, \nu$  contributions !

(NAB, CD)

# Key QCD Experiment at GSI

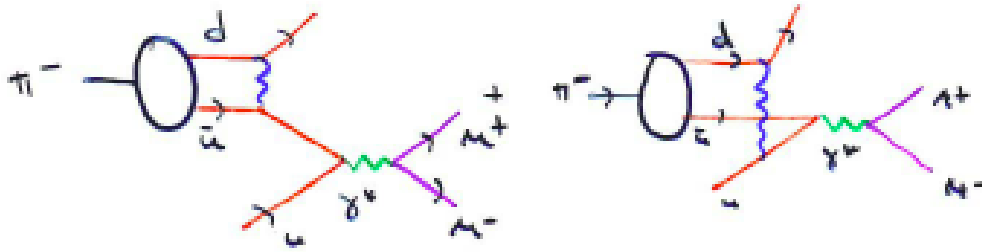
$\cos 2\phi$  correlation in DY from double ISI



Abstract

We show that initial-state interactions contribute to the  $\cos 2\phi$  distribution in unpolarized Drell-Yan lepton pair production  $pp$  and  $p\bar{p} \rightarrow \ell^+\ell^-X$ , without suppression. The asymmetry is expressed as a product of chiral-odd distributions  $h_1^\perp(x_1, p_\perp^2) \times \bar{h}_1^\perp(x_2, k_\perp^2)$ , where the quark-transversity function  $h_1^\perp(x, p_\perp^2)$  is the transverse momentum dependent, light-cone momentum distribution of transversely polarized quarks in an *unpolarized* proton. We compute this (naive)  $T$ -odd and chiral-odd distribution function and the resulting  $\cos 2\phi$  asymmetry explicitly in a quark-scalar diquark model for the proton with initial-state gluon interaction. In this model the function  $h_1^\perp(x, p_\perp^2)$  equals the  $T$ -odd (chiral-even) Siverts effect function  $f_{1T}^\perp(x, p_\perp^2)$ . This suggests that the single-spin asymmetries in the SIDIS and the Drell-Yan process are closely related to the  $\cos 2\phi$  asymmetry of the unpolarized Drell-Yan process, since all can arise from the same underlying mechanism. This provides new insight regarding the role of quark and gluon orbital angular momentum as well as that of initial- and final-state gluon exchange interactions in hard QCD processes.

Boer, Hwang, sjb



$\pi^- u \rightarrow d \gamma^*$  subprocess

Depends on pion distribution amplitude

$$\phi_\pi(x, Q)$$

Calculators by

Berges, SJB, Lopez  $\lambda(x_F)$

Brodsky, Khote, Müller, SID

Data consistent with  $\phi_{\pi 2}(x, Q)$

rather than asymptotic

## Higher Twist seen in Data NA10, CP

Drell-Yan  $\pi N \rightarrow l^+ l^- X$

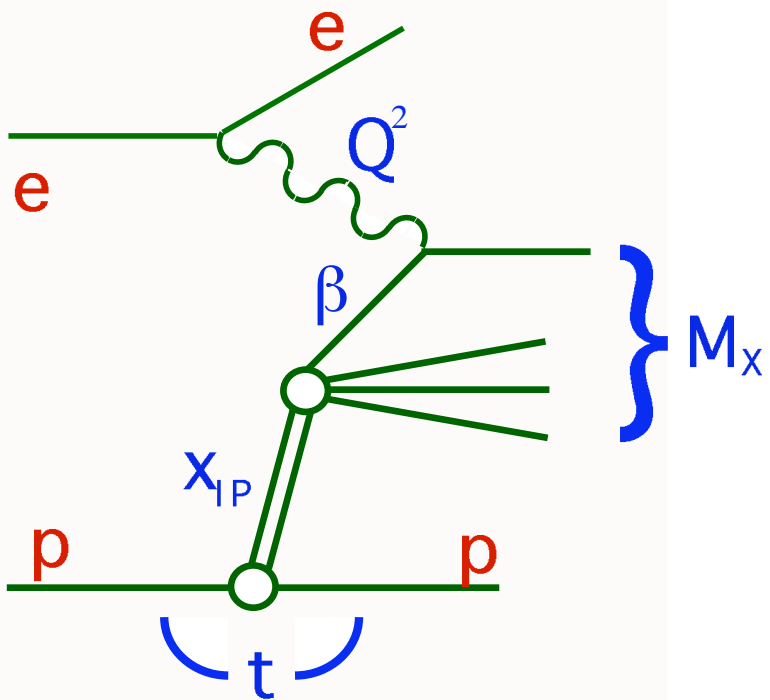
$$\frac{d\sigma}{dx d\cos\theta} = A(1-x)^2(1+\cos^2\theta) + B \frac{\sin^2\theta}{Q^2}$$

Higher Twist and Leading Twist  
comparable at

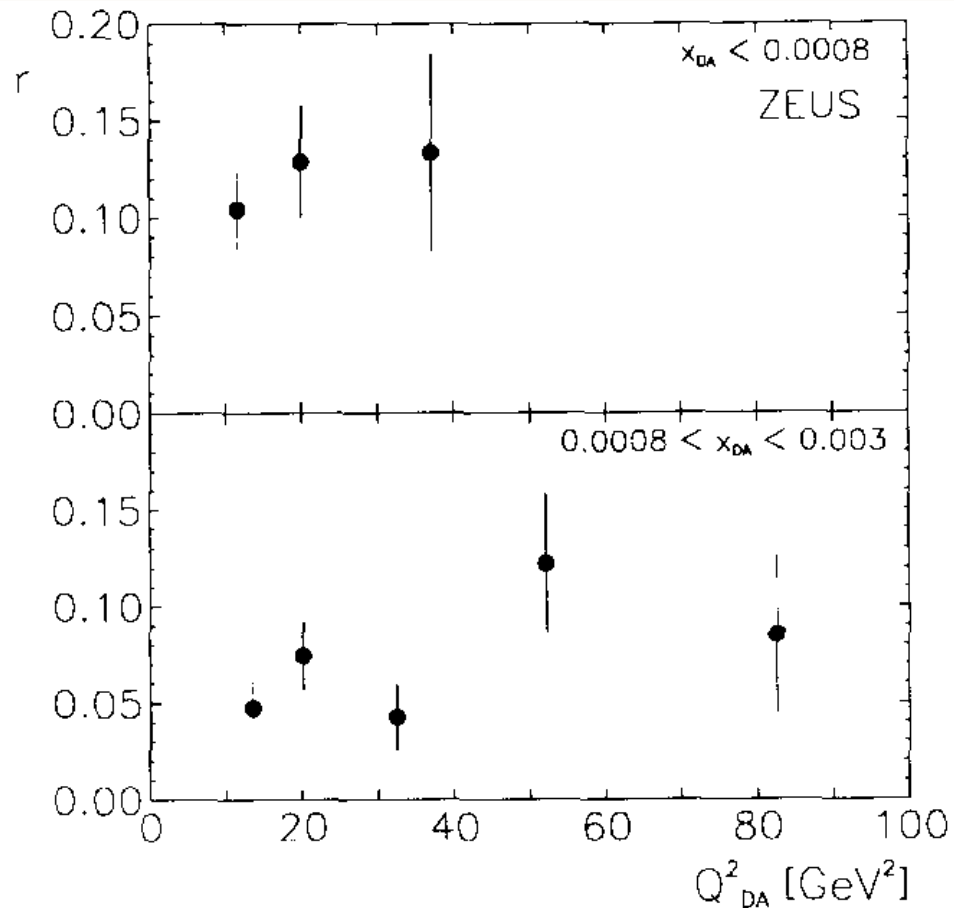
$$\mu^2 = (1-x)Q^2$$

fixed

# Remarkable observation at HERA



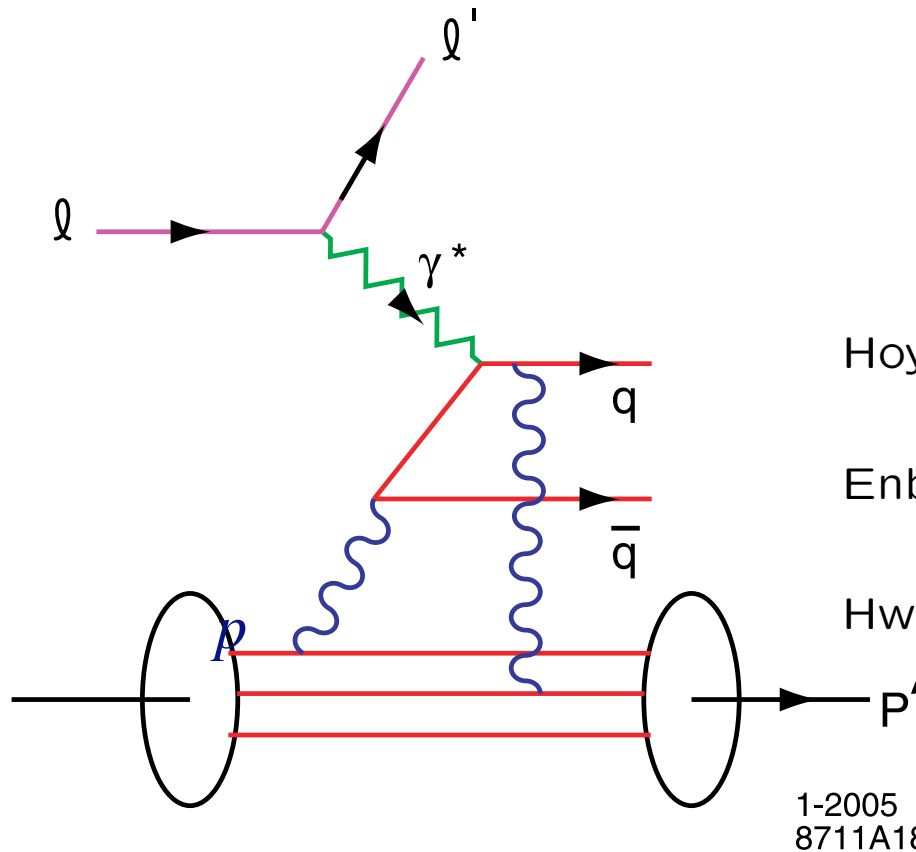
10% of DIS events are diffractive !



Fraction  $r$  of events with a large rapidity gap,  $\eta_{\max} < 1.5$ , as a function of  $Q_{DA}^2$  for two ranges of  $x_{DA}$ . No acceptance corrections have been applied.

M. Derrick et al. [ZEUS Collaboration], Phys. Lett. B 315, 481 (1993).

# Final State Interaction Produces Diffractive DIS



## Quark Rescattering

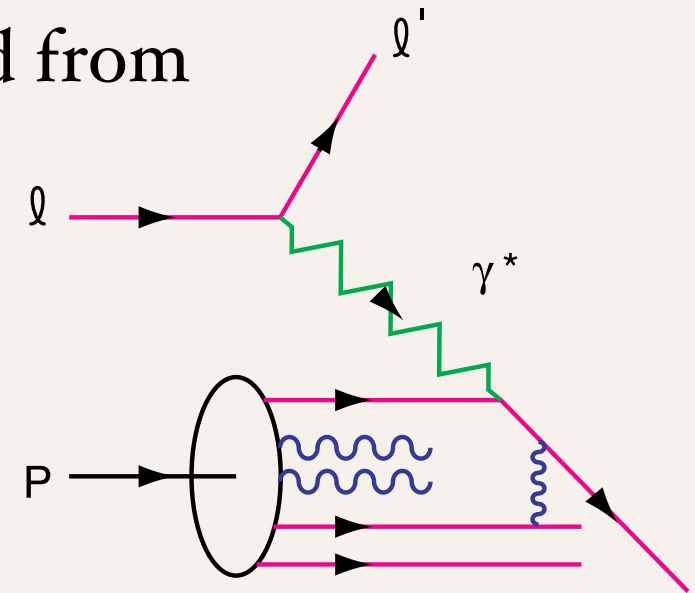
Hoyer, Marchal, Peigne, Sannino, SJB (BHM)

Enberg, Hoyer, Ingelman, SJB

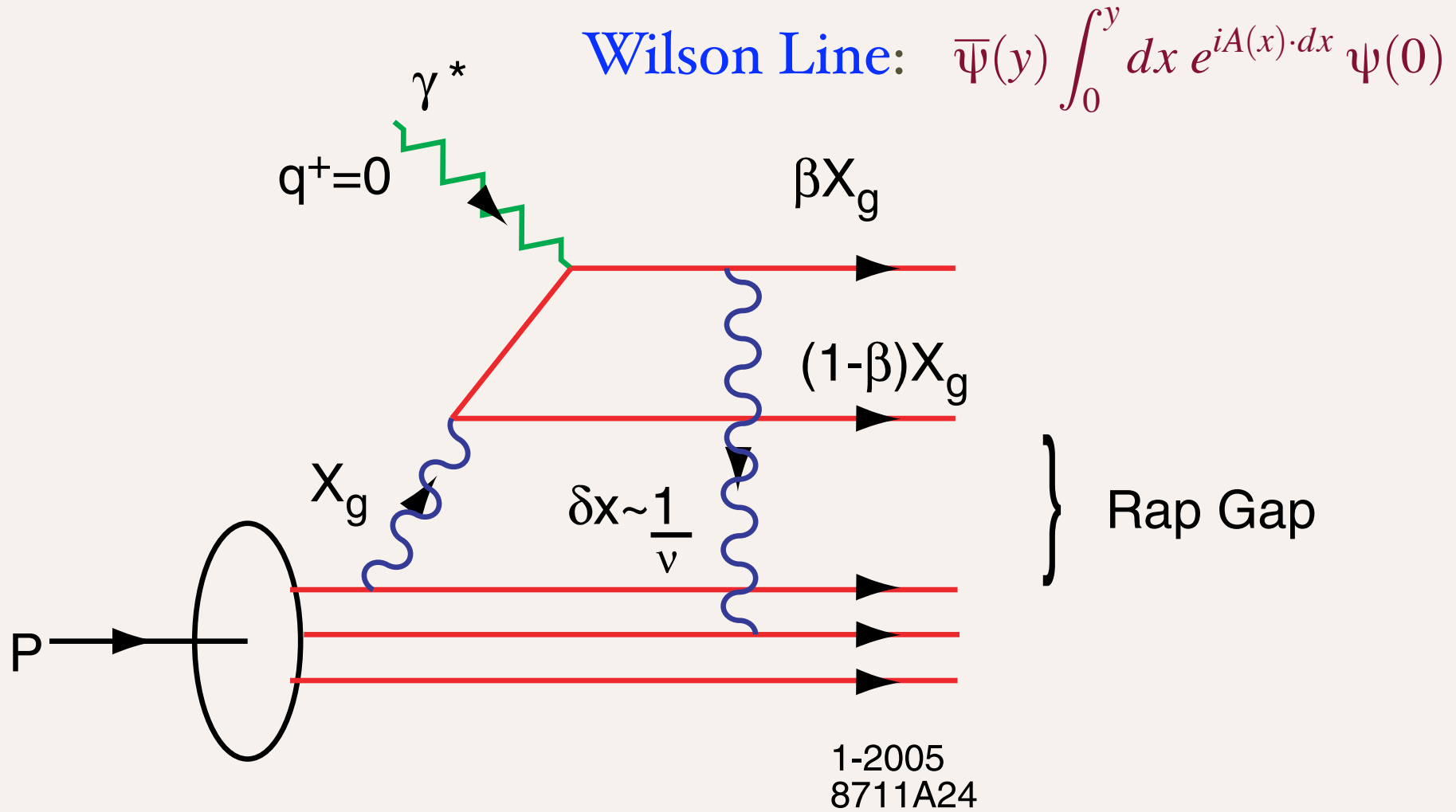
Hwang, Schmidt, SJB

1-2005  
8711A18

- Quarks Reinteract in Final State
- Analogous to Coulomb phases, but not unitary
- Observable effects: DDIS, SSI, shadowing, antishadowing
- Structure functions cannot be computed from LFWFs computed in isolation
- Wilson line not 1 even in lcg



# QCD Mechanism for Rapidity Gaps





# Key QCD Experiment at GSI

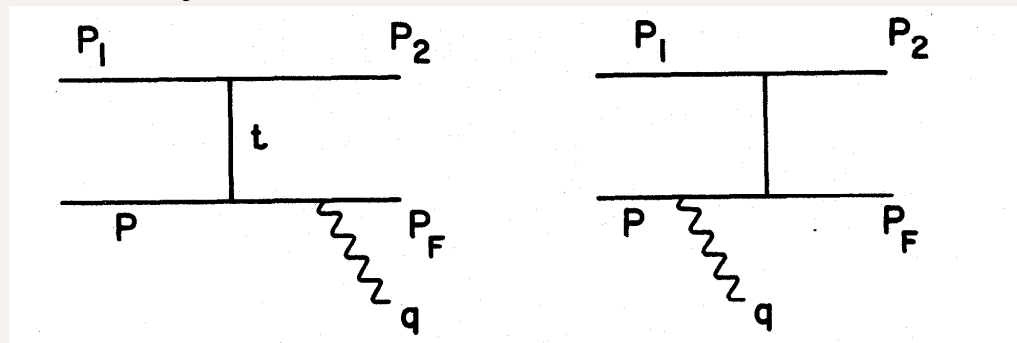
Double-Diffractive Drell-Yan

$$\bar{p}p \rightarrow \bar{p} + \ell^+ \ell^- + p$$

**Large-Mass Timelike Muon Pairs in Hadronic Interactions**

S. M. Berman\*, D. J. Levy, and T. L. Neff§

Phys. Rev. Lett. 23, 1363–1365 (1969)



Prototype for exclusive Higgs production

# Key QCD Experiment at GSI

Measure diffractive hidden charm production at forward  $x_F$

*Even close to threshold*

$$\frac{d\sigma}{dt_1 dt_2 dx_F} (\bar{p}p \rightarrow \bar{p} + J/\psi + p)$$

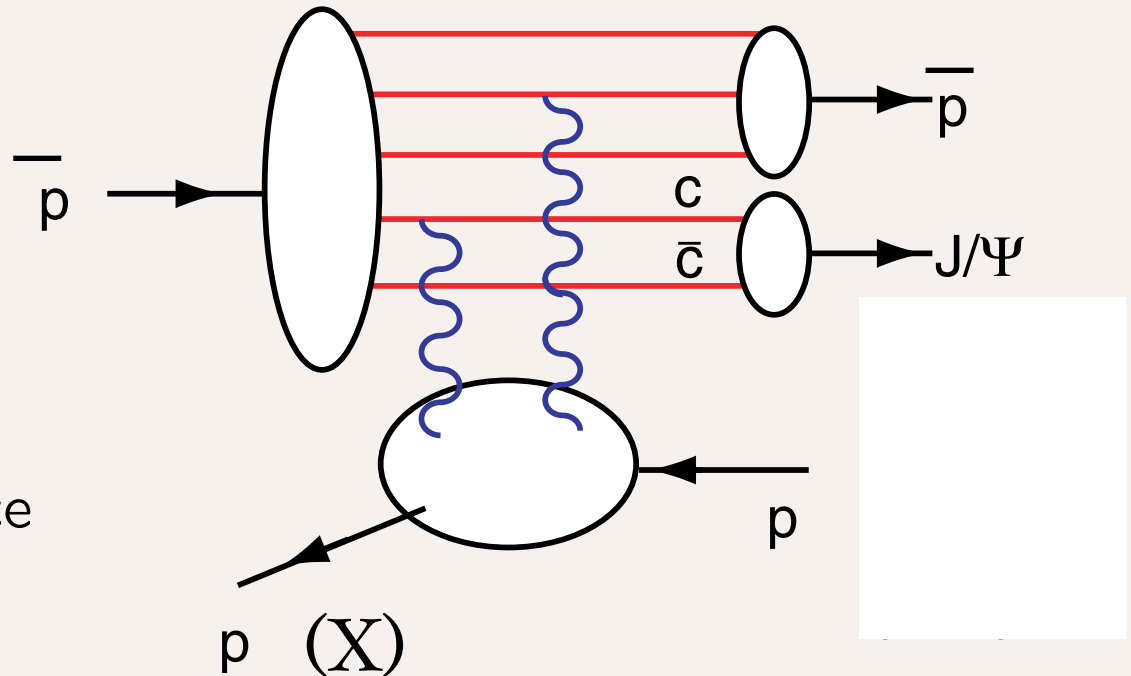
$$\frac{d\sigma}{dt dx_F} (\bar{p}p \rightarrow \bar{p} + J/\psi + X)$$

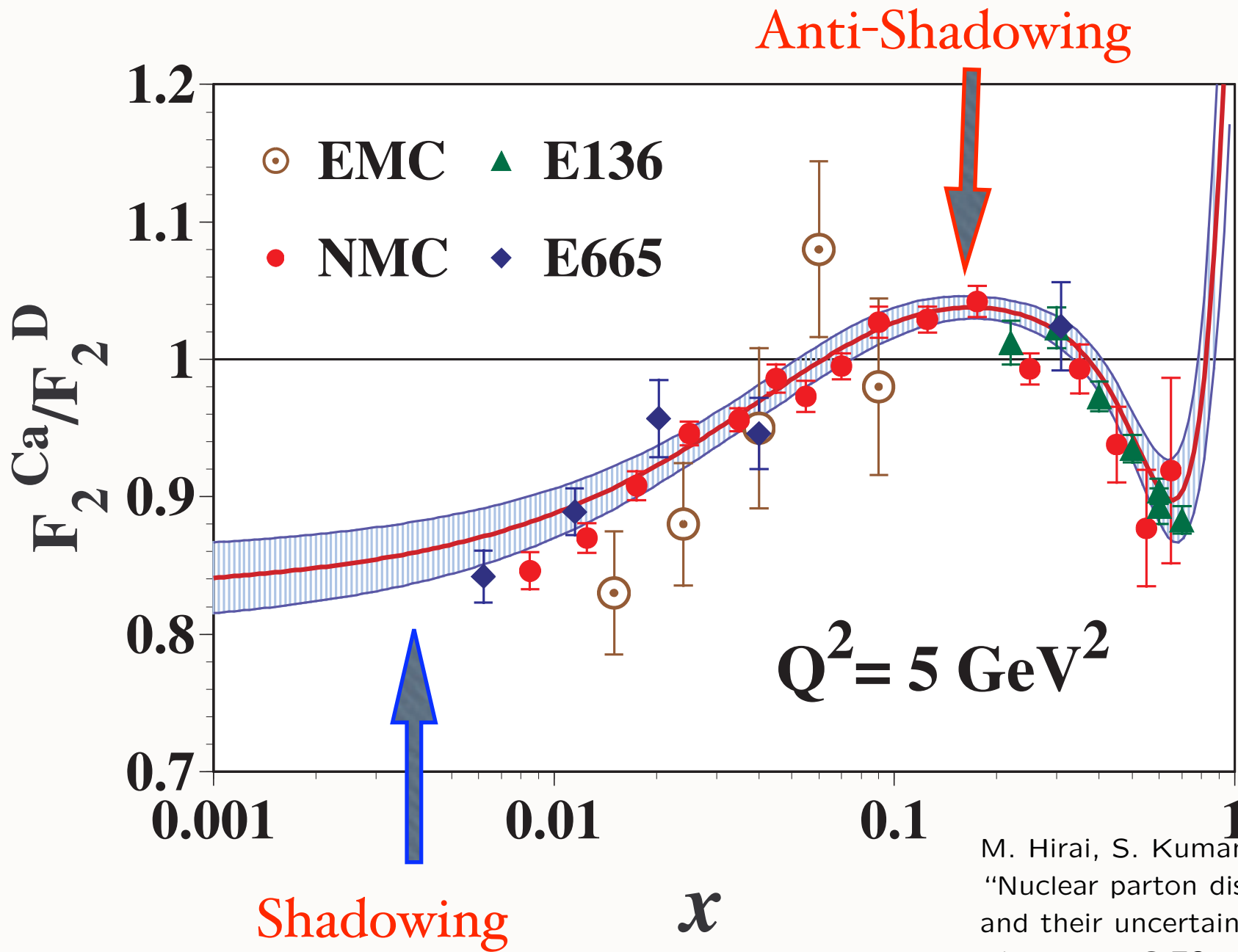
Anomalous nuclear dependence

$$\frac{d\sigma}{dx_F} (\bar{p}A \rightarrow J/\psi + X)$$

$A^{\alpha(x_2)}$  versus  $A^{\alpha(x_F)}$

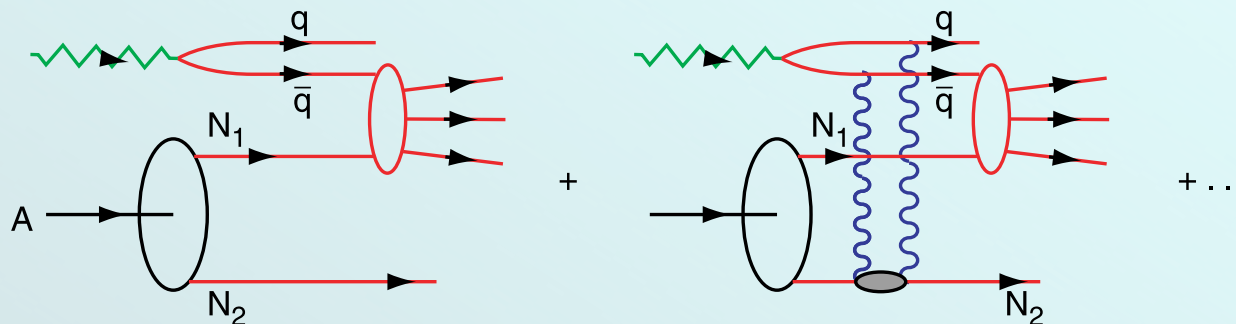
## Important Tests of Intrinsic Charm





M. Hirai, S. Kumano and T. H. Nagai,  
 "Nuclear parton distribution functions  
 and their uncertainties,"  
 Phys. Rev. C **70**, 044905 (2004)  
 [arXiv:hep-ph/0404093].

# Origin of Nuclear Shadowing in Glauber - Gribov Theory



## *Interference of one-step and two-step processes*

Interaction on upstream leading-twist nucleon diffractive

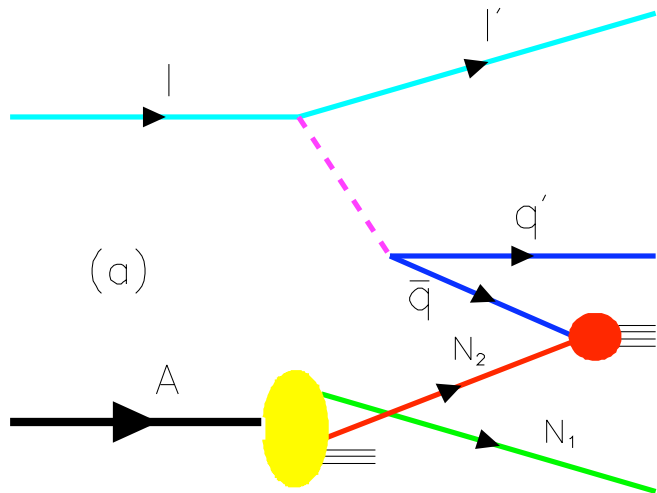
Phase  $i X i = -1$  produces destructive interference

No Flux reaches down stream nucleon

# Shadowing and Antishadowing in Lepton-Nucleus Scattering

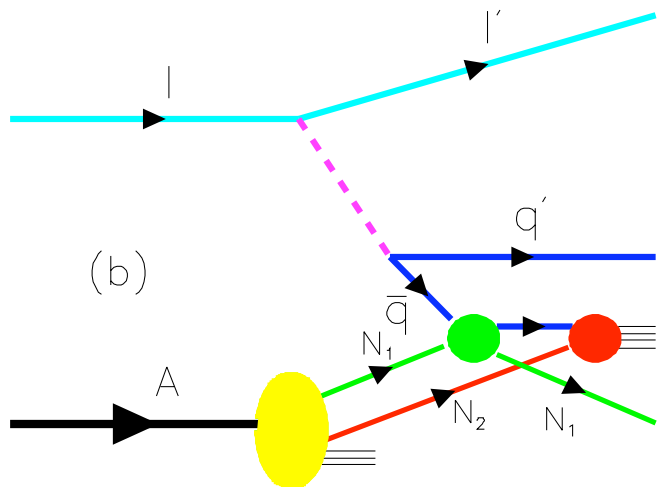
- Shadowing: **Destructive Interference** of Two-Step and One-Step Processes  
*Pomeron Exchange*
- Antishadowing: **Constructive Interference** of Two-Step and One-Step Processes!  
*Reggeon and Odderon Exchange*
- Antishadowing is Not Universal!  
Electromagnetic and weak currents:  
different nuclear effects !  
**Potentially significant for NuTeV Anomaly}**

Schmidt, Yang, Lu, sjb



The one-step and two-step processes in DIS on a nucleus.

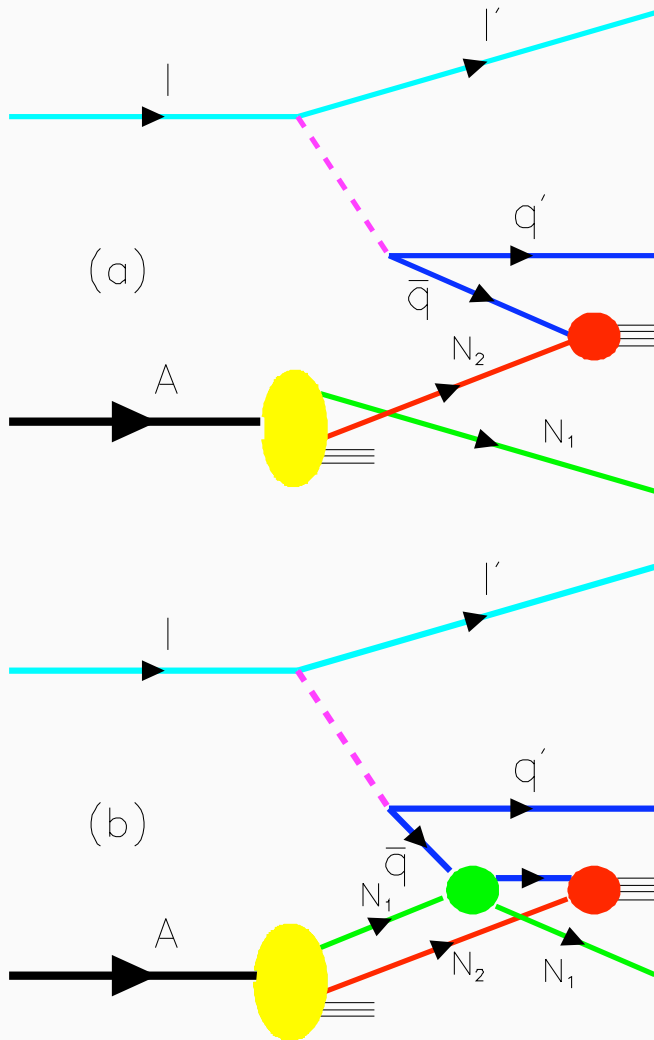
Coherence at small Bjorken  $x_B$  :  
 $1/Mx_B = 2\nu/Q^2 \geq L_A$ .



If the scattering on nucleon  $N_1$  is via pomeron exchange, the one-step and two-step amplitudes are opposite in phase, thus diminishing the  $\bar{q}$  flux reaching  $N_2$ .

→ Shadowing of the DIS nuclear structure functions.

**Kowalski: HERA DDIS produces observed nuclear shadowing**



The one-step and two-step processes in DIS on a nucleus.

If the scattering on nucleon  $N_1$  is via  $C = -$  Reggeon or Odderon exchange, the one-step and two-step amplitudes are

**constructive in phase, enhancing** the  $\bar{q}$  flux reaching  $N_2$

→ **Antishadowing** of the DIS nuclear structure functions

# Reggeon Exchange

Phase of two-step amplitude relative to one step:

$$\frac{1}{\sqrt{2}}(1 - i) \times i = \frac{1}{\sqrt{2}}(i + 1)$$

Constructive Interference

Depends on quark flavor!

Thus antishadowing is not universal

Different for couplings of  $\gamma^*$ ,  $Z^0$ ,  $W^\pm$

*Critical test: Tagged Drell-Yan*



# Shadowing and Antishadowing in Lepton-Nucleus Scattering

- Shadowing and Antishadowing in DIS arise from interference of multi-nucleon processes in nucleus **Phases!**

- Not due to nuclear wavefunction  
Wavefunction of stable nucleus is real.  
Effect of multi-scattering of  $q\bar{q}$  in nucleus.

- Bjorken Scaling :  
Interference requires leading-twist diffractive DIS processes

# Key QCD Experiment at GSI

Measure Non-Universal Anti-Shadowing in Drell-Yan

$$\bar{p}A \rightarrow \ell^+ \ell^- X$$

$$Q^2 = x_1 x_2 s$$

$$x_1 x_2 = .05, x_F = x_1 - x_2$$

$$A^\alpha(x_1) = \frac{2 \frac{d\sigma}{dQ^2 dx_F}(\bar{p}A \rightarrow \ell^+ \ell^- X)}{A \frac{d\sigma}{dQ^2 dx_F}(\bar{p}d \rightarrow \ell^+ \ell^- X)}$$

Flavor  
u, d tag

Higher twist effects at high  $x_F$ :

Deviations from  $(1 + \cos^2 \theta)$

$\cos 2\phi$  correlation.

# PQCD and Exclusive Processes

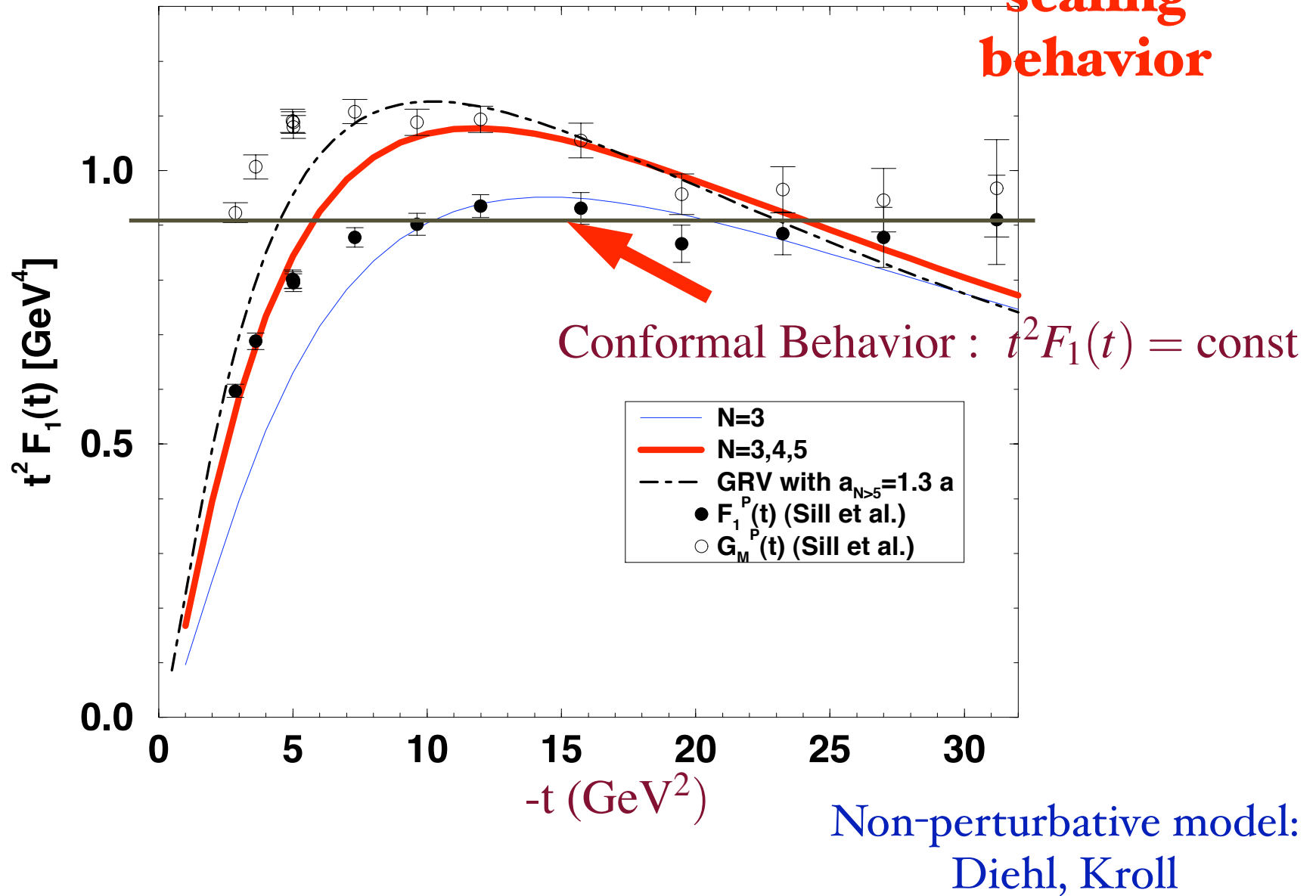
Lepage; SJB  
Efremov, Radyuskin

$$M = \int \prod dx_i dy_i \phi_F(x, \tilde{Q}) \times T_H(x_i, y_i, \tilde{Q}) \phi_I(y_i, Q)$$

- Iterate kernel of LFWFs when at high virtuality; distribution amplitude contains all physics below factorization scale
- **Rigorous Factorization Formulae: Leading twist**
- Underly Exclusive B-decay analyses
- Distribution amplitude: gauge invariant, OPE, evolution equations, conformal expansions
- BLM scale setting: sum nonconformal contributions in scale of running coupling
- Derive Dimensional Counting Rules/ Conformal Scaling

# Proton Form Factor

**Remarkable  
scaling  
behavior**



# Scaling is a manifestation of asymptotically free hadron interactions and AdS/CFT

From dimensional arguments at high energies in binary reactions:

## CONSTITUENT COUNTING RULE

Brodsky and Farrar, Phys. Rev. Lett. 31 (1973) 1153  
Matveev et al., Lett. Nuovo Cimento, 7 (1973) 719

Counting Rules:

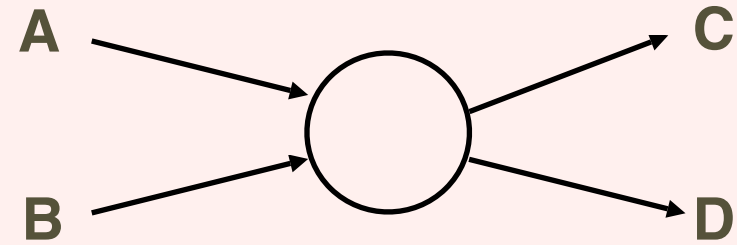
$$q(x) \sim (1-x)^{2n_{spect}-1} \text{ for } x \rightarrow 1$$

$$F(Q^2) \sim \left(\frac{1}{Q^2}\right)^{(n-1)}$$

$$\frac{d\sigma}{dt}(AB \rightarrow CD) \sim \frac{F(t/s)}{s^{(n_{participants}-2)}}$$

$$n_{participants} = n_A + n_B + n_C + n_D$$

$$\frac{d\sigma}{d^3p/E}(AB \rightarrow CX) \sim F(\hat{t}/\hat{s}) \times \frac{(1-x_R)^{(2n_{spectators}-1)}}{(p_T^2)^{(n_{participants}-2)}}$$



Predictions  
from conformal  
symmetry

hadron helicity  
conservation

Farrar, Jackson;  
Lepage, sjb;  
Burkardt, Schmidt, Sjb

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July 5, 2006

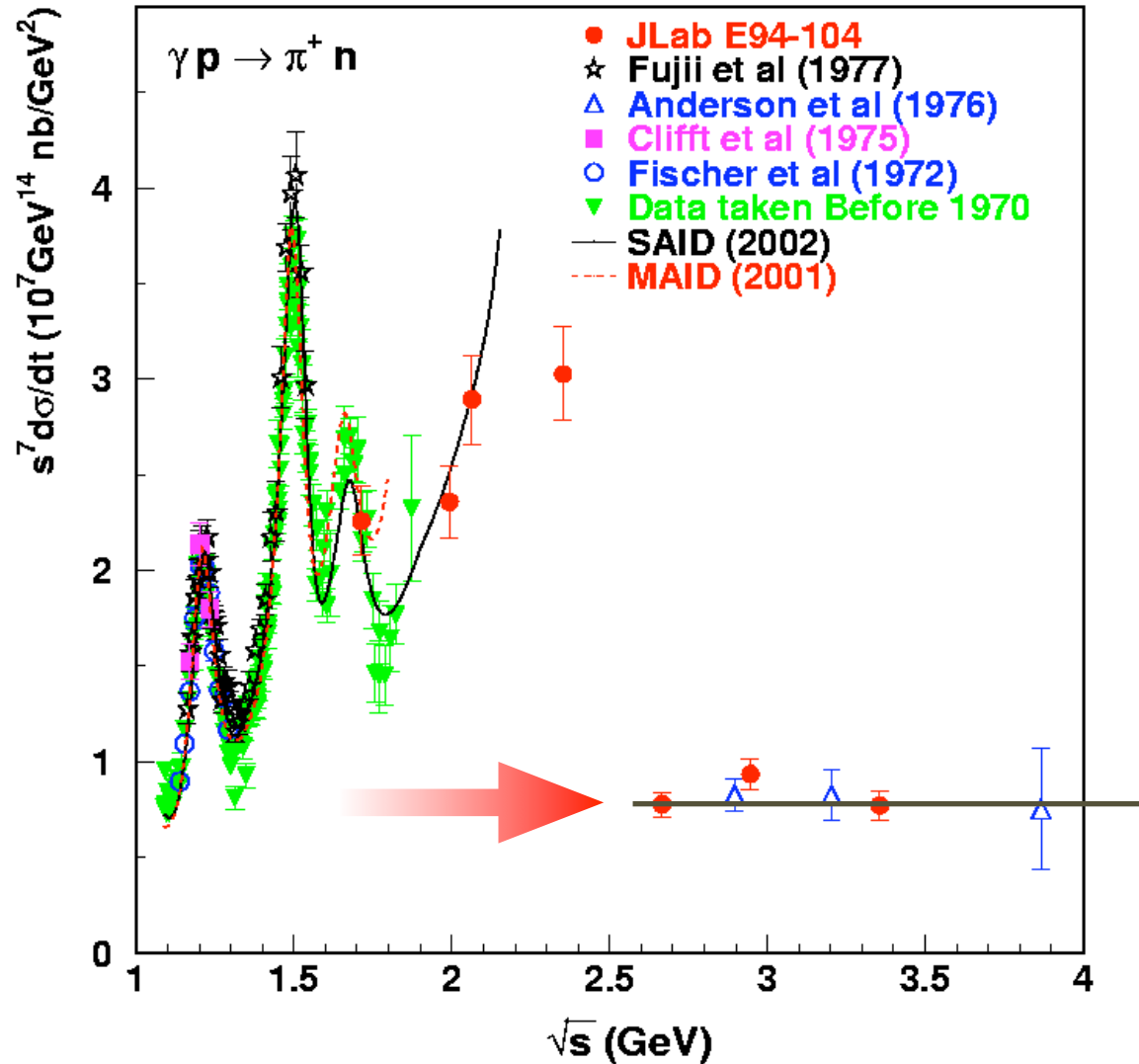
AdS/CFT, QCD, & GSI

Stan Brodsky, SLAC

# Test of PQCD Scaling

## Constituent counting rules

Farrar, sjb; Muradyan, Matveev, Taveklidze



$$s^7 d\sigma/dt(\gamma p \rightarrow \pi^+ n) \sim \text{const}$$

fixed  $\theta_{CM}$  scaling

PQCD and AdS/CFT:

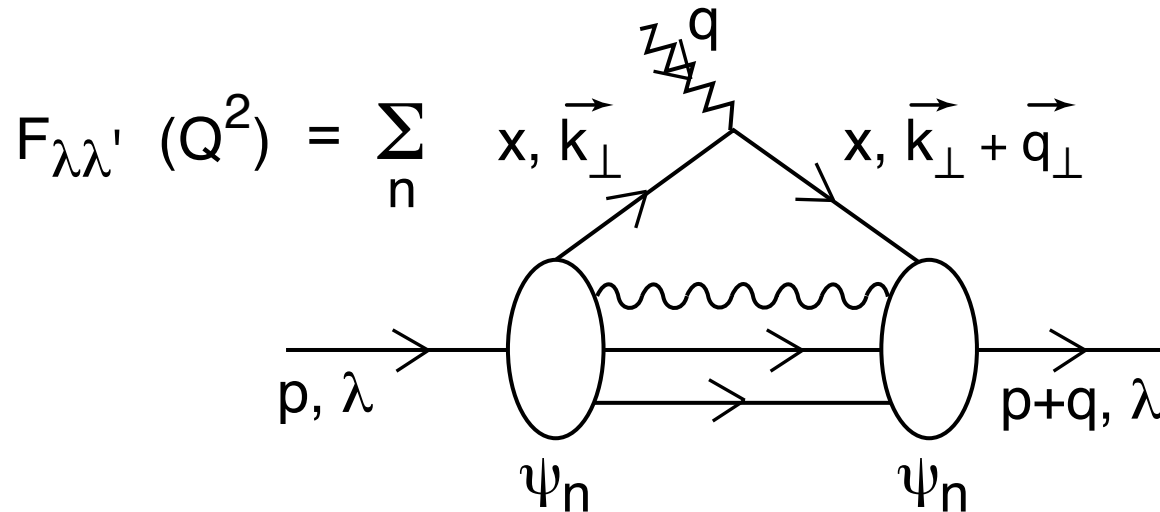
$$s^{n_{tot}-2} \frac{d\sigma}{dt}(A + B \rightarrow C + D) = F_{A+B \rightarrow C+D}(\theta_{CM})$$

$$s^7 \frac{d\sigma}{dt}(\gamma p \rightarrow \pi^+ n) = F(\theta_{CM})$$

$$n_{tot} = 1 + 3 + 2 + 3 = 9$$

*Conformal invariance at high momentum transfer*

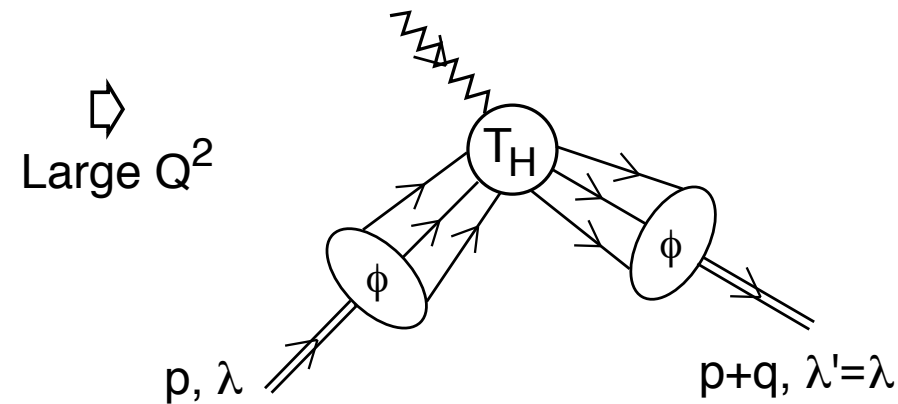
Form Factors  $\ell p \rightarrow \ell' p' \langle p' \lambda' | J^+ (0) | p \lambda \rangle$



Lepage, Sjb  
Efremov  
Radyushkin

## QCD Factorization

*Normalization,  
scale-setting, higher order issues*



$$T_H = \sum \int dx_1, \dots, dx_n$$

$$= \frac{\alpha_s^2}{Q^4} f(x_i, y_i)$$

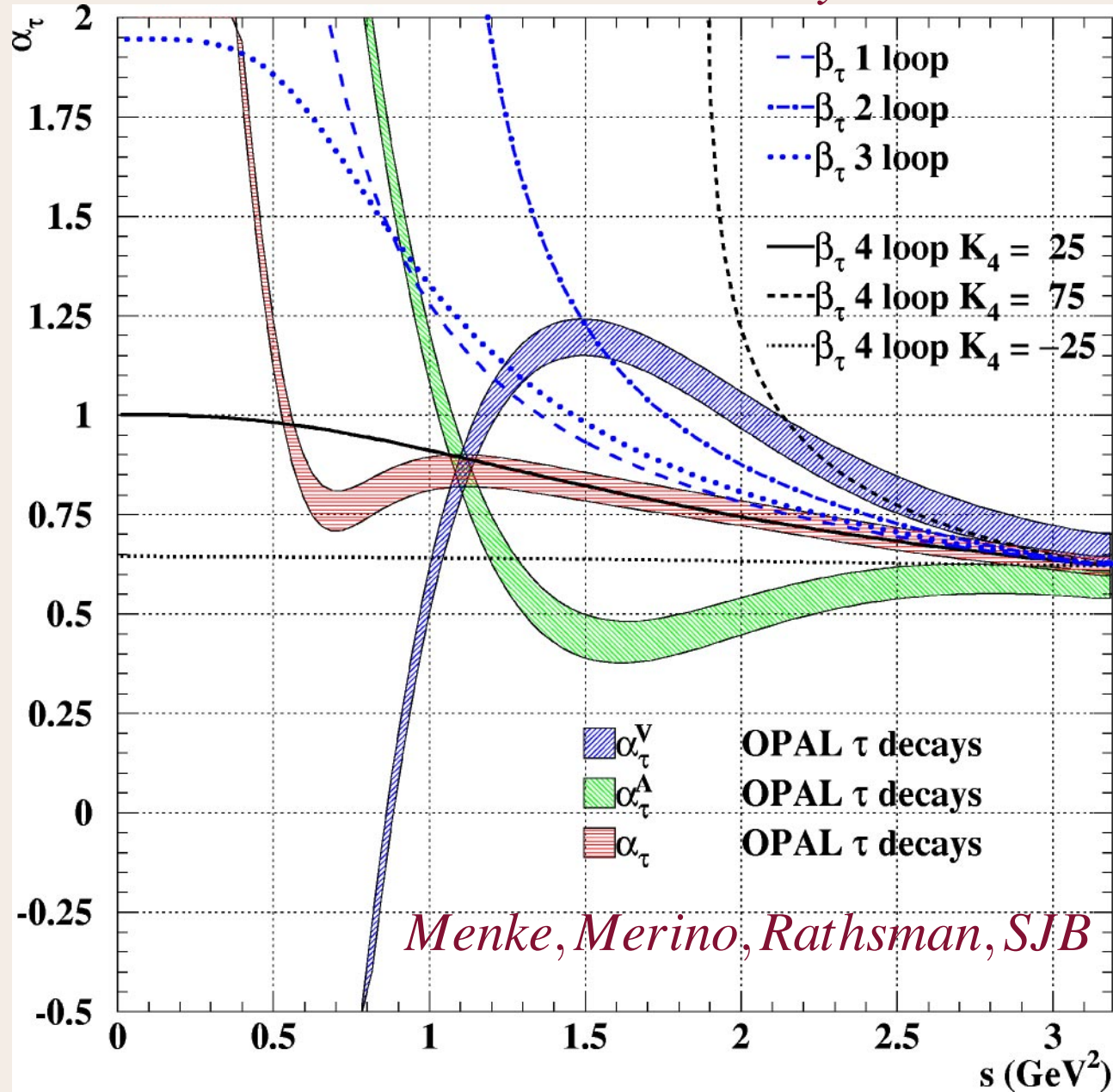
Scaling Laws from PQCD or AdS/CFT

# Why do dimensional counting rules work so well?

- PQCD predicts log corrections from powers of  $\alpha_s$ , logs, pinch contributions
- QCD coupling evaluated in IR regime.
- IR Fixed point! DSE: *Alkofer, von Smekal et al.*
- QED, EW -- define coupling from observable, predict other observable
- Underlying Conformal Symmetry of Semi-Classical QCD Lagrangian -- Apply AdS/CFT



# QCD Effective Coupling from *hadronic $\tau$ decay*



# AdS/CFT and QCD

- Non-Perturbative Derivation of Dimensional Counting Rules (Strassler and Polchinski)
- Light-Front Wavefunctions: Confinement at Long Distances and Conformal Behavior at short distances (de Teramond and Sjb)
- Power-law fall-off at large transverse momentum,  $x \rightarrow 1$
- Hadron Spectra, Regge Trajectories

# QCD Lagrangian and Conformal Symmetry

The diagram shows the QCD Lagrangian  $L_{\text{QCD}}$  enclosed in a red box. Above the box, three labels with arrows point to parts of the equation: 'gluon dynamics' points to the first term, 'quark kinetic energy + quark-gluon dynamics' points to the second term, and 'mass term' points to the third term. Below the box, four labels with arrows point to specific parts of the equation: 'QCD color charge' points to the  $4g^2$  denominator, 'field strength tensor' points to  $G_{\mu\nu}$ , 'covariant derivative' points to  $D_\mu$ , and 'quark field' points to  $\psi_f$ .

$$L_{\text{QCD}} = -\frac{1}{4g^2} \text{Tr}(G^{\mu\nu} G_{\mu\nu}) + \sum_{f=1}^{nf} i \bar{\psi}_f D_\mu \gamma^\mu \psi_f + \sum_{f=1}^{nf} m_f \bar{\psi}_f \psi_f$$

Conformal Symmetry – Property of classical renormalizable Lagrangian

Massless quarks  $\beta = \frac{d\alpha_s(Q^2)}{d \log Q^2} = 0$

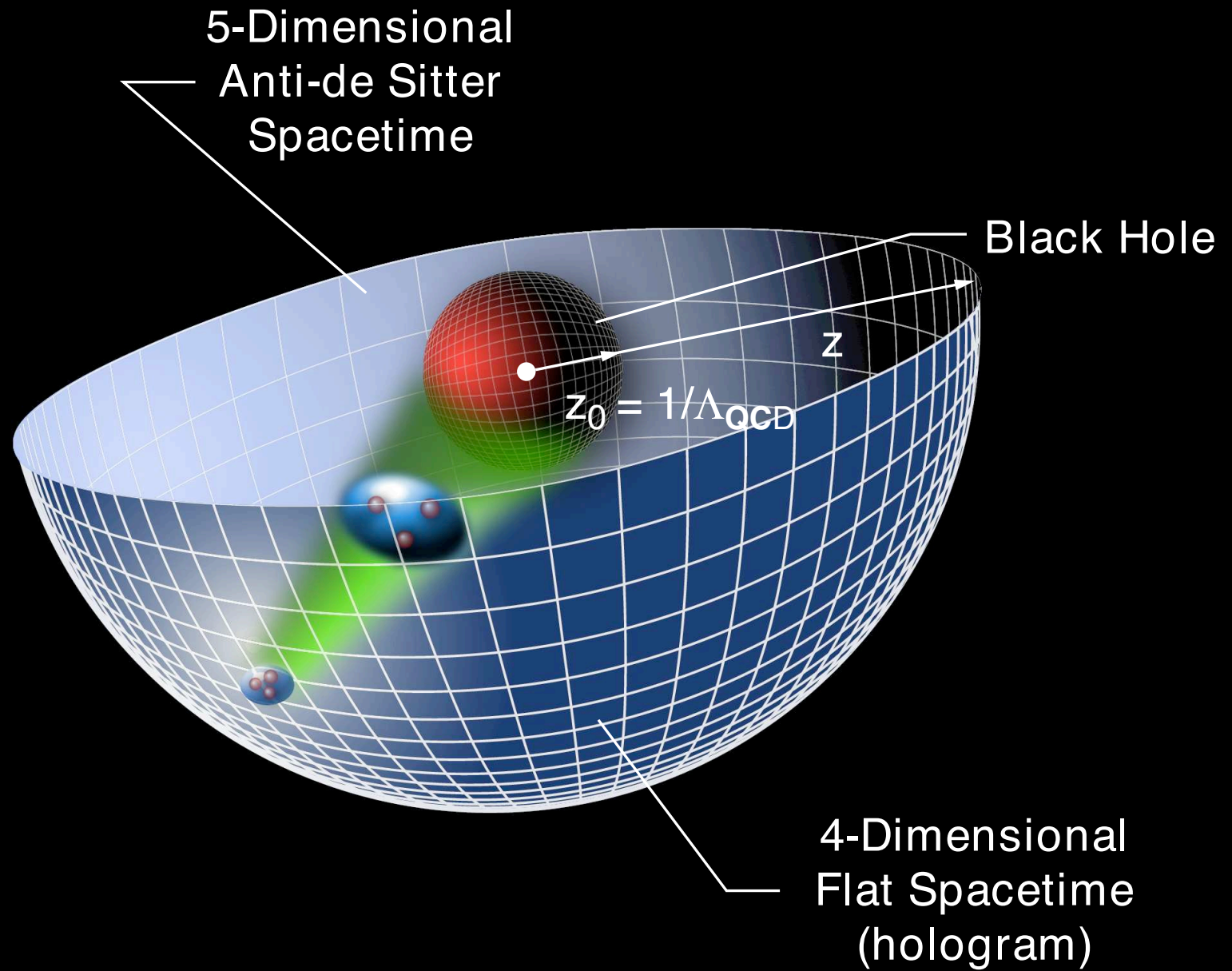
Parisi

Poincare transformations plus

dilatation :  $x^\mu \rightarrow \lambda x^\mu$

plus

conformal transformations : inversion  $[x^\mu \rightarrow -\frac{x^\mu}{x^2}] \times$  translation  $\times$  inversion

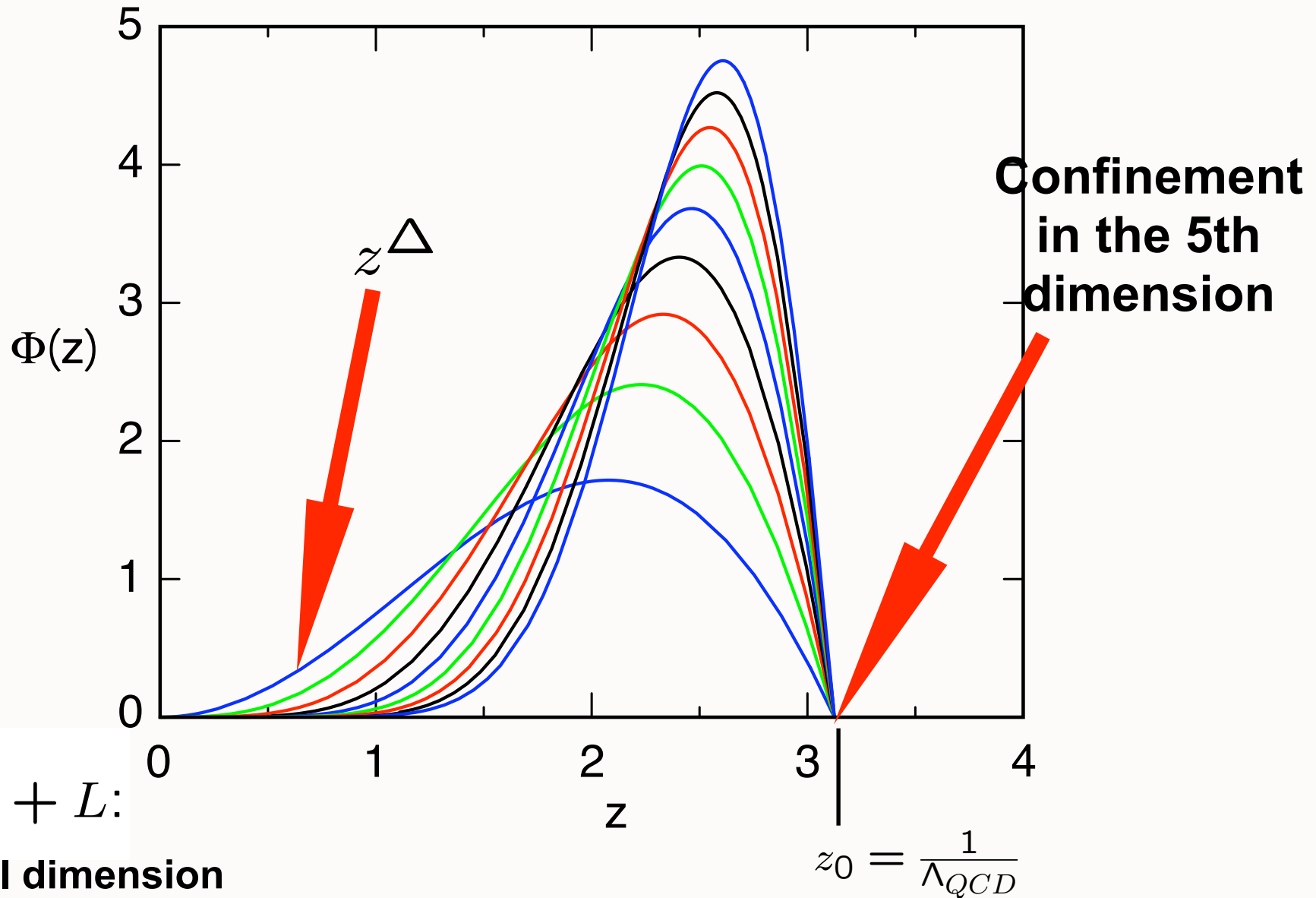


# Features of AdS/QCD

- Semi-Classical Approximation to massless QCD
- Coupling is constant, zero beta function
- Conformal symmetry broken by confinement
- No particle creation, absorption
- Spectrum of Mesons, Baryons, Glueballs
- Light-Front Wavefunctions
- Quark Counting Rules

# Strongly Coupled Conformal QCD and Holography

- Conformal Theories are invariant under the Poincaré and conformal transformations with  $M^{\mu\nu}$ ,  $P^\mu$ ,  $D$ ,  $K^\mu$ , the generators of  $SO(4, 2)$ .
- QCD appears as a nearly-conformal theory in the energy regimes accessible to experiment. Invariance of conformal QCD is broken by quark masses and quantum loops (running coupling). For  $\beta = d\alpha_s(Q^2)/d\ln Q^2 = 0$  (fixed point theory), PQCD is a conformal theory: Parisi, Phys. Lett. B **39**, 643 (1972).
- Phenomenological success of dimensional scaling laws for exclusive processes  $d\sigma/dt \sim 1/s^{n-2}$  (n total number of constituents), implies QCD is a strongly coupled conformal theory at moderate but not asymptotic energies (PQCD predicts powers of  $\alpha_s$  and logs).
- Theoretical and empirical evidence that  $\alpha_s(Q^2)$  has an IR fixed point (constant in the IR): Alkofer, Fischer and Llanes-Estrada, hep-th/0412330; Brodsky, Menke, Merino and Rathsman, hep-ph/0212078; .



$$\Delta = 3 + L:$$

Conformal dimension  
of hadron

Trento  
July 5, 2006

AdS/CFT, QCD, & GSI

Stan Brodsky, SLAC



## Match fall-off at small $z$ to Conformal Dimension of State at short distances

- Pseudoscalar mesons:  $\mathcal{O}_{3+L} = \bar{\psi} \gamma_5 D_{\{\ell_1 \dots \ell_m\}} \psi$  ( $\Phi_\mu = 0$  gauge).
- 4- $d$  mass spectrum from boundary conditions on the normalizable string modes at  $z = z_0$ ,  $\Phi(x, z_0) = 0$ , given by the zeros of Bessel functions  $\beta_{\alpha,k}$ :  $\mathcal{M}_{\alpha,k} = \beta_{\alpha,k} \Lambda_{QCD}$
- Normalizable AdS modes  $\Phi(z)$

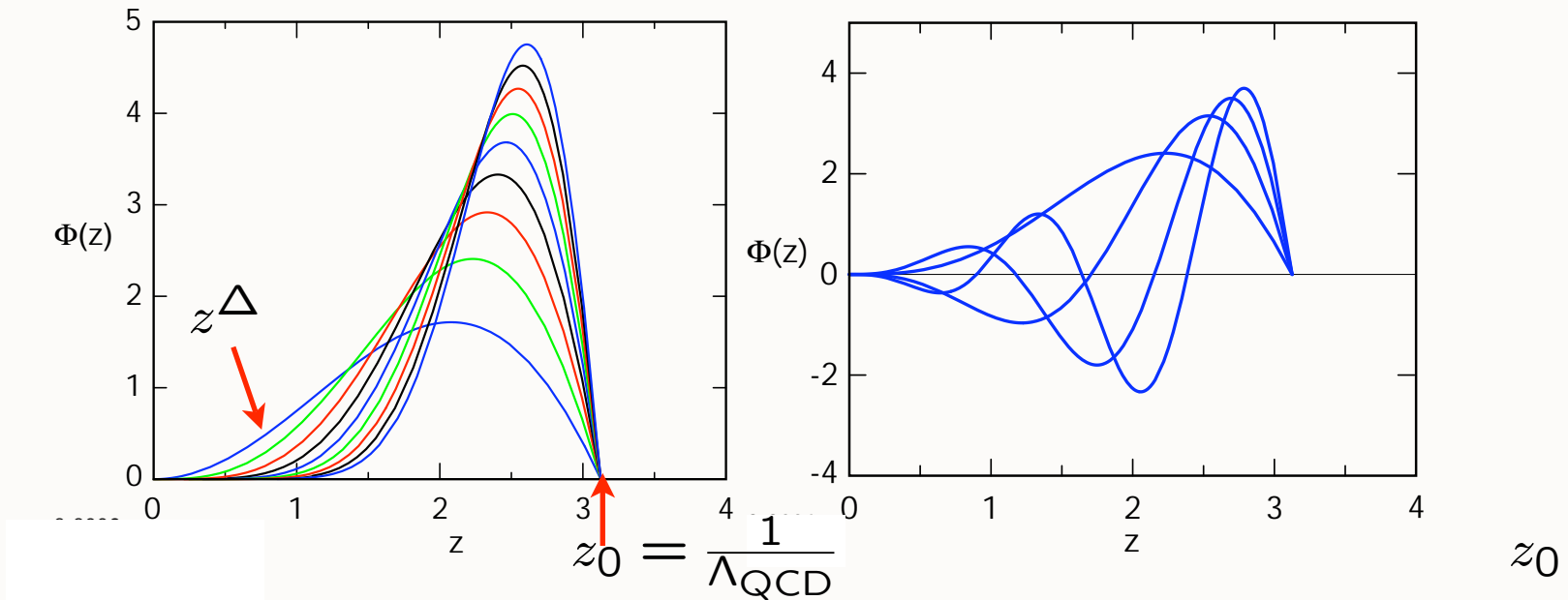


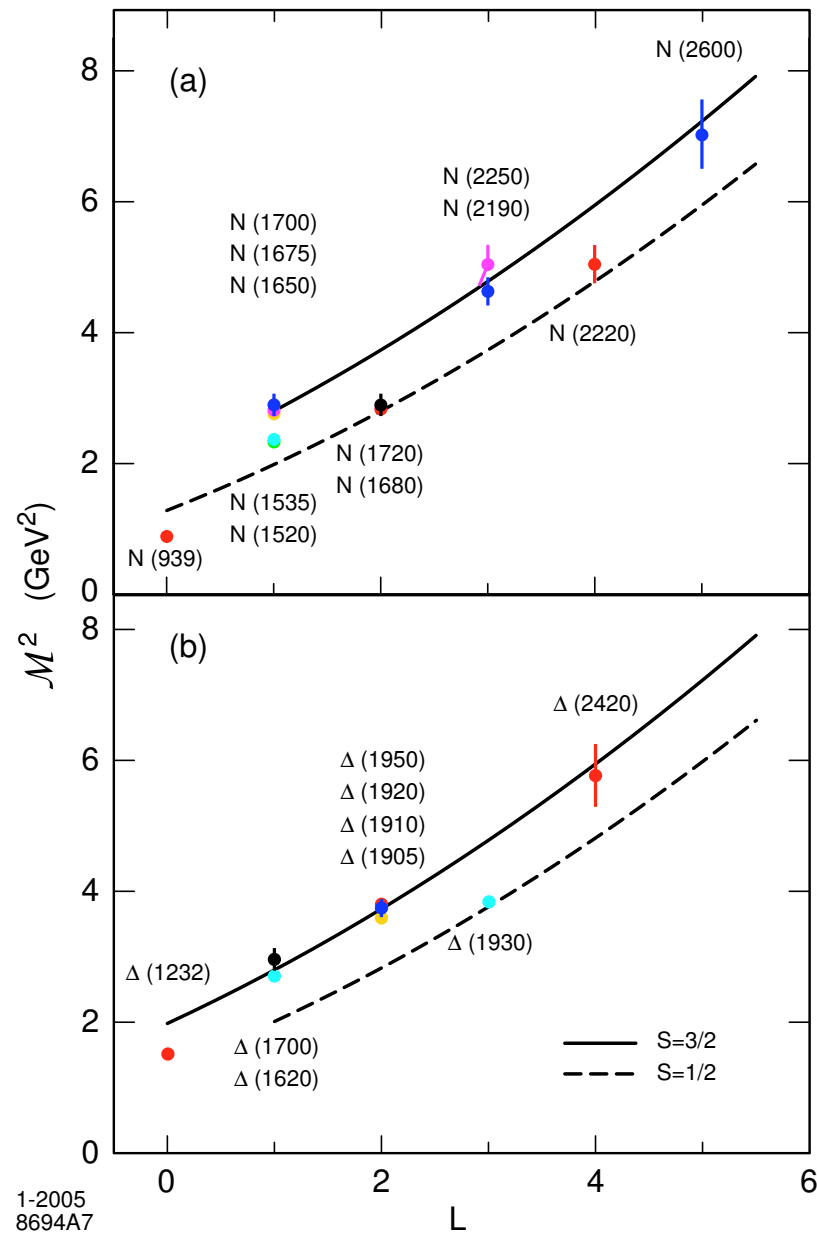
Fig: Meson orbital and radial AdS modes for  $\Lambda_{QCD} = 0.32$  GeV.



# Predictions of AdS/CFT

Only one  
parameter!

Entire  
light  
quark  
baryon  
spectrum



1-2005  
8694A7

Guy de Teramond  
SJB

Phys.Rev.Lett.94:  
201601,2005

hep-th/0501022

Fig: Predictions for the light baryon orbital spectrum for  $\Lambda_{QCD} = 0.22$  GeV

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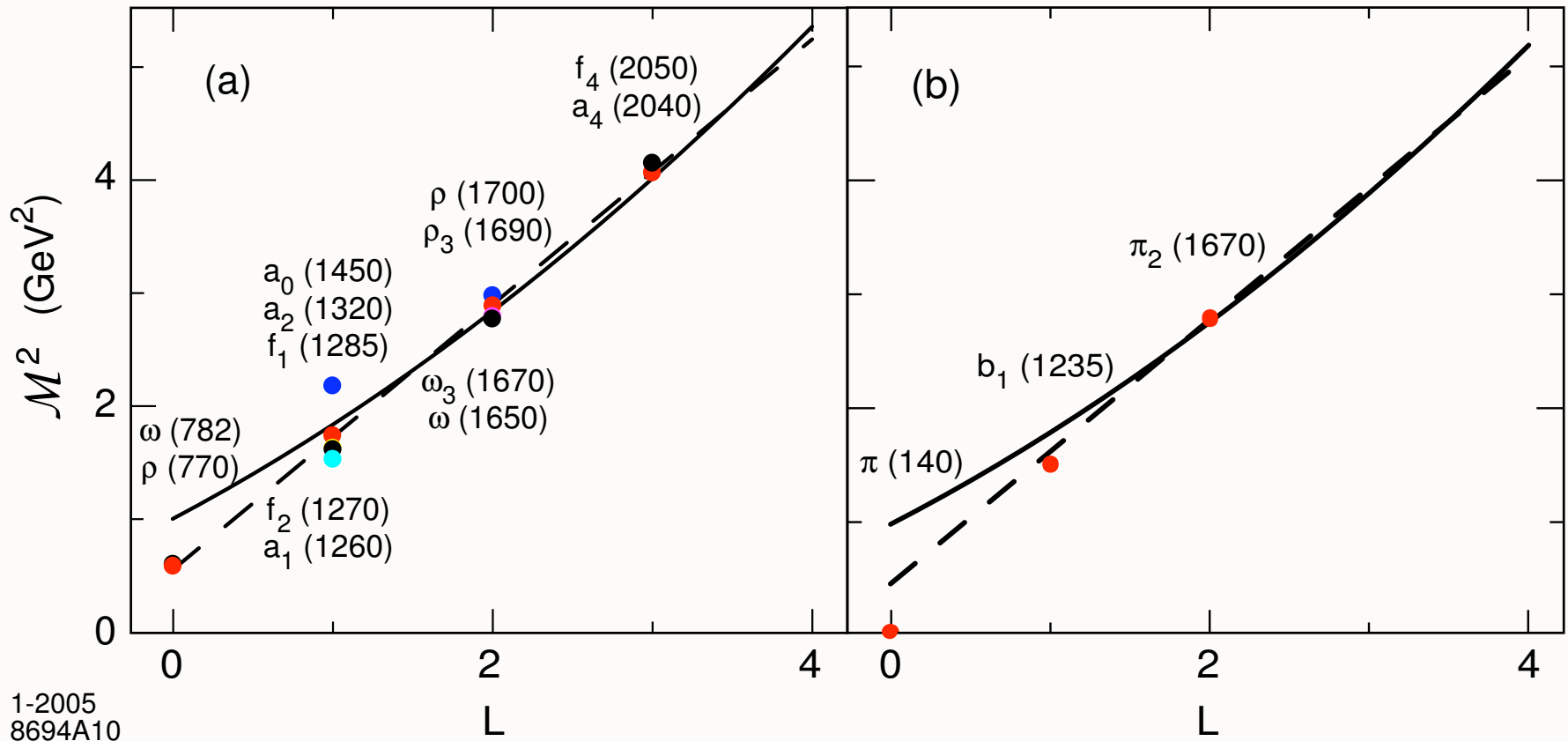
- $SU(6)$  multiplet structure for  $N$  and  $\Delta$  orbital states, including internal spin  $S$  and  $L$ .

$SU(6)$	$S$	$L$	Baryon State
<b>56</b>	$\frac{1}{2}$	0	$N \frac{1}{2}^+$ (939)
	$\frac{3}{2}$	0	$\Delta \frac{3}{2}^+$ (1232)
<b>70</b>	$\frac{1}{2}$	1	$N \frac{1}{2}^-$ (1535) $N \frac{3}{2}^-$ (1520)
	$\frac{3}{2}$	1	$N \frac{1}{2}^-$ (1650) $N \frac{3}{2}^-$ (1700) $N \frac{5}{2}^-$ (1675)
	$\frac{1}{2}$	1	$\Delta \frac{1}{2}^-$ (1620) $\Delta \frac{3}{2}^-$ (1700)
<b>56</b>	$\frac{1}{2}$	2	$N \frac{3}{2}^+$ (1720) $N \frac{5}{2}^+$ (1680)
	$\frac{3}{2}$	2	$\Delta \frac{1}{2}^+$ (1910) $\Delta \frac{3}{2}^+$ (1920) $\Delta \frac{5}{2}^+$ (1905) $\Delta \frac{7}{2}^+$ (1950)
<b>70</b>	$\frac{1}{2}$	3	$N \frac{5}{2}^-$ $N \frac{7}{2}^-$
	$\frac{3}{2}$	3	$N \frac{3}{2}^-$ $N \frac{5}{2}^-$ $N \frac{7}{2}^-$ (2190) $N \frac{9}{2}^-$ (2250)
	$\frac{1}{2}$	3	$\Delta \frac{5}{2}^-$ (1930) $\Delta \frac{7}{2}^-$
<b>56</b>	$\frac{1}{2}$	4	$N \frac{7}{2}^+$ $N \frac{9}{2}^+$ (2220)
	$\frac{3}{2}$	4	$\Delta \frac{5}{2}^+$ $\Delta \frac{7}{2}^+$ $\Delta \frac{9}{2}^+$ $\Delta \frac{11}{2}^+$ (2420)
<b>70</b>	$\frac{1}{2}$	5	$N \frac{9}{2}^-$ $N \frac{11}{2}^-$
	$\frac{3}{2}$	5	$N \frac{7}{2}^-$ $N \frac{9}{2}^-$ $N \frac{11}{2}^-$ (2600) $N \frac{13}{2}^-$

# Features of Holographic Model

de Teramond sjb

- Ratio of proton to Delta trajectories= ratio of zeroes of Bessel functions.
- One scale  $\Lambda_{\text{QCD}}$  determines hadron spectrum (slightly different for mesons and baryons)
- Only quark-antiquark, qqq, and g g hadrons appear at classical level
- Covariant version of bag model: confinement+conformal symmetry



1-2005  
8694A10

Fig: Light meson orbital spectrum: 4-dim states dual to vector fields in the bulk,  $\Lambda_{QCD} = 0.26 \text{ GeV}$

Guy de Teramond  
SJB

Trento  
July 5, 2006

AdS/CFT, QCD, & GSI

Stan Brodsky, SLAC

# Glueball Spectrum

- AdS wave function with effective mass  $\mu$ :

$$\left[ z^2 \partial_z^2 - (d-1)z \partial_z + z^2 \mathcal{M}^2 - (\mu R)^2 \right] f(z) = 0,$$

where  $\Phi(x, z) = e^{-iP \cdot x} f(z)$  and  $P_\mu P^\mu = \mathcal{M}^2$ .

- Glueball interpolating operator with twist -dimension minus spin- two, and conformal dimension  $\Delta = 4 + L$

$$\mathcal{O}_{4+L} = F D_{\{\ell_1 \dots \ell_m\}} F,$$

where  $L = \sum_{i=1}^m \ell_i$  is the total internal space-time orbital momentum.

- Normalizable scalar AdS mode (  $d = 4$ ):

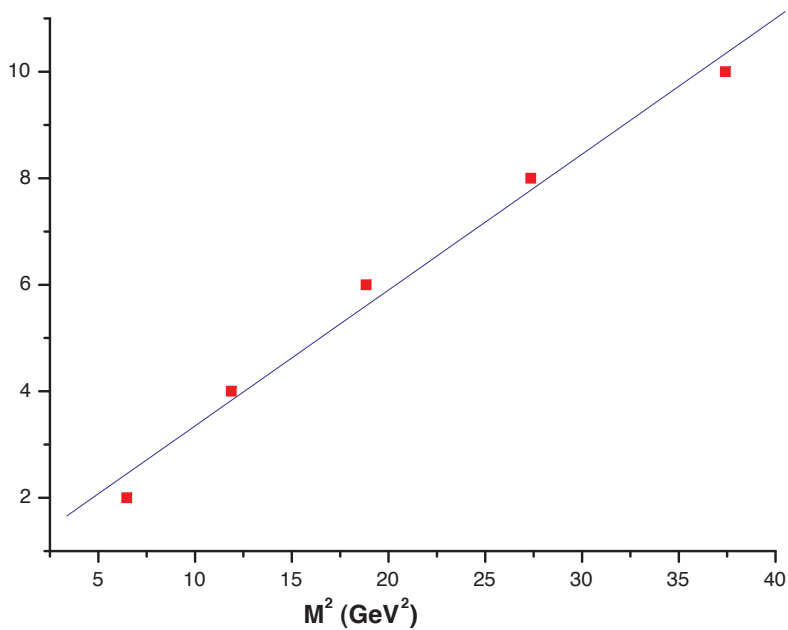
$$\Phi_{\alpha,k}(x, z) = C_{\alpha,k} e^{-iP \cdot x} z^2 J_\alpha (z \beta_{\alpha,a} \Lambda_{QCD})$$

with  $\alpha = 2 + L$  and scaling dimension  $\Delta = 4 + L$ .

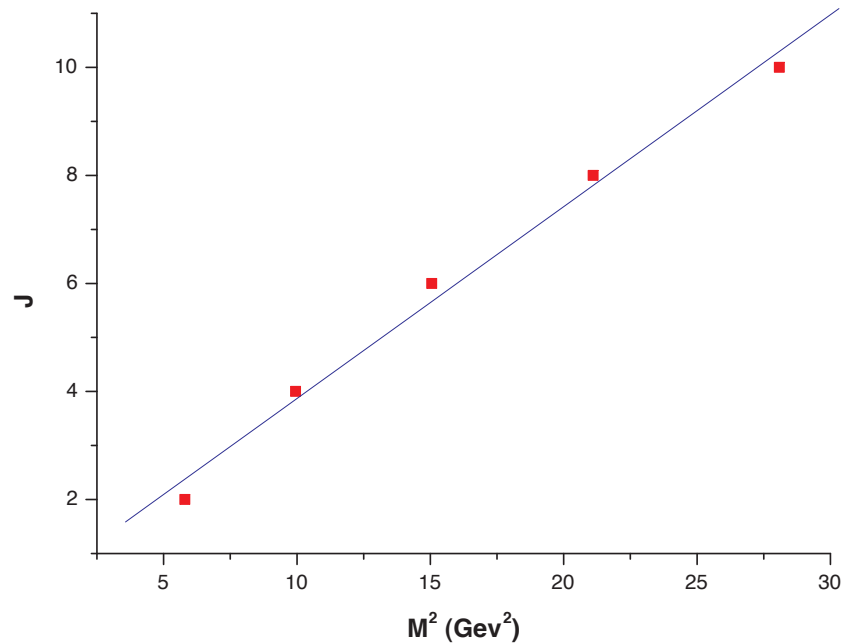
# Glueball Regge trajectories from gauge/string duality and the Pomeron

Henrique Boschi-Filho,<sup>\*</sup> Nelson R. F. Braga,<sup>†</sup> and Hector L. Carrion<sup>‡</sup>

*Instituto de Física, Universidade Federal do Rio de Janeiro,*



Neumann Boundary Conditions



Dirichlet Boundary Conditions

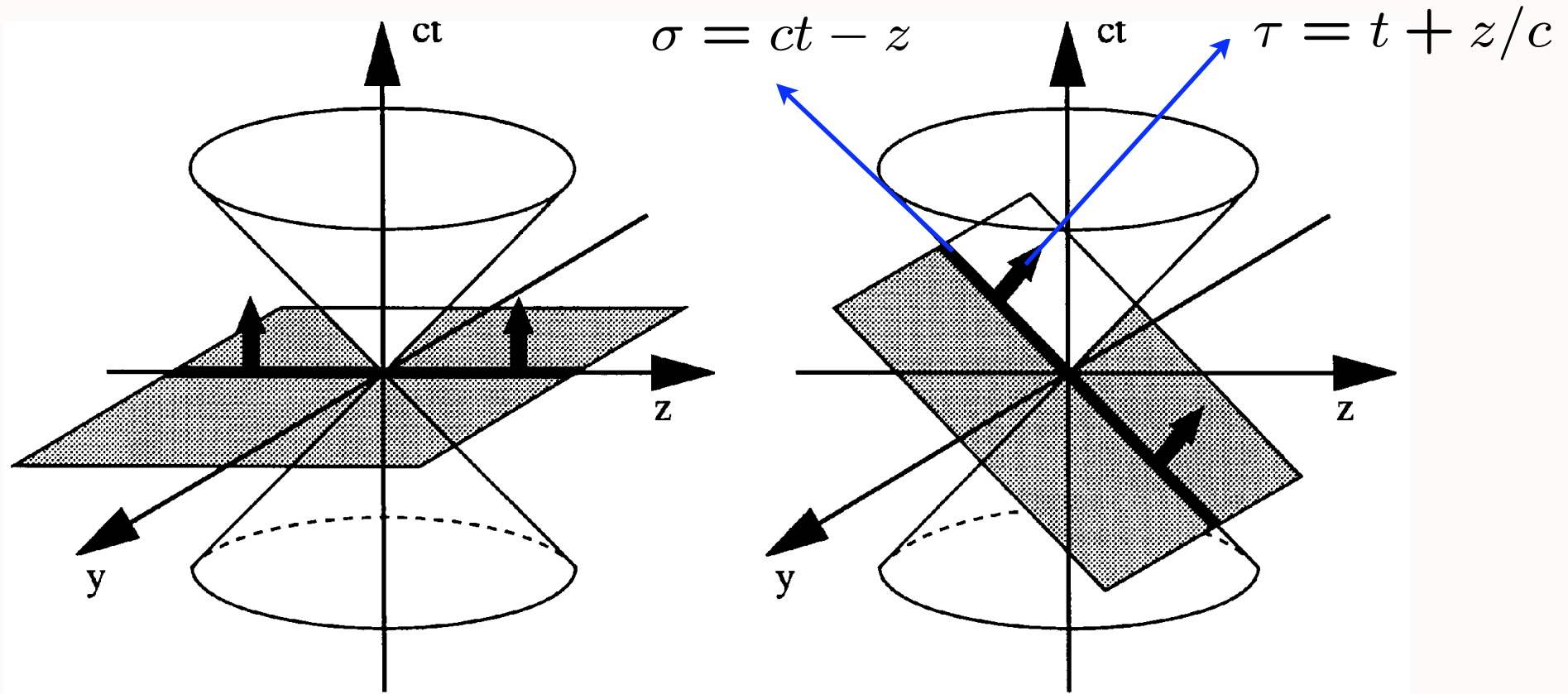
CAQCD  
5-12-06

**LF Wavefunctions and QCD  
Amplitudes from AdS/CFT**

Stan Brodsky, SLAC

# Dirac's Amazing Idea: The "Front Form"

Evolve in  
light-front time!



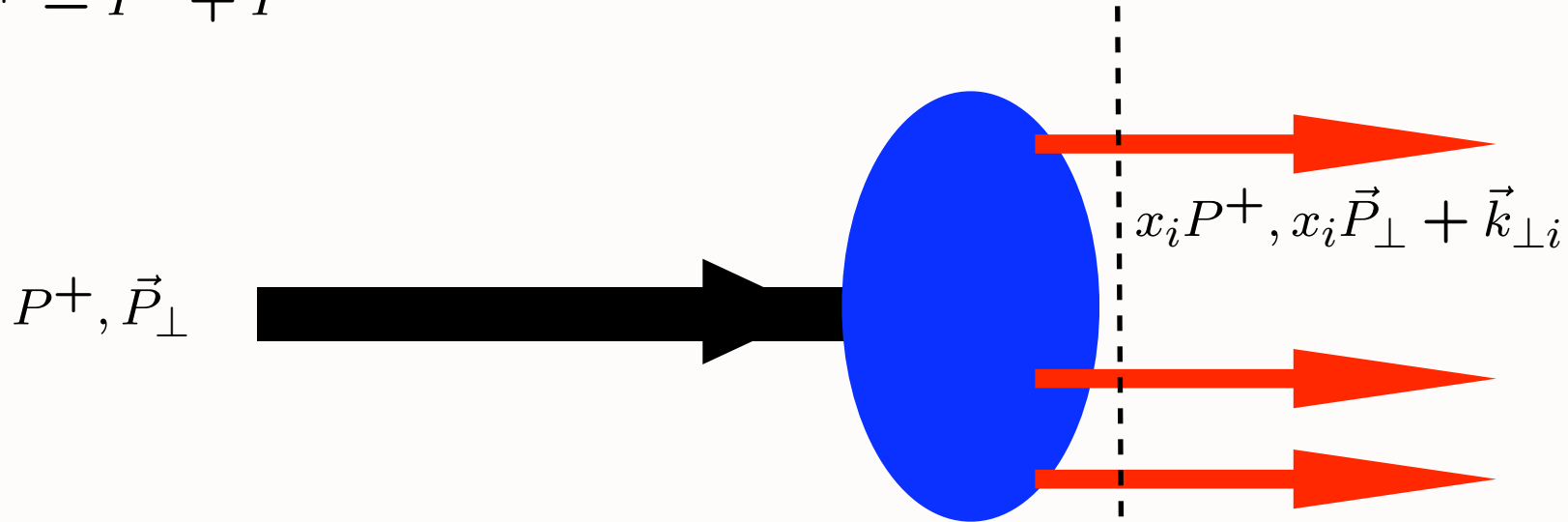
Instant Form

Front Form

# Light-Front Wavefunctions

$$P^+ = P^0 + P^z$$

Fixed  $\tau = t + z/c$



$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

$$\sum_i^n x_i = 1$$

$$\sum_i^n \vec{k}_{\perp i} = \vec{0}_\perp$$

*Invariant under boosts! Independent of  $P^\mu$*



# Angular Momentum on the Light-Front

$$J^z = \sum_{i=1}^n s_i^z + \sum_{j=1}^{n-1} l_j^z.$$

Conserved  
LF Fock state by Fock State

$$l_j^z = -i \left( k_j^1 \frac{\partial}{\partial k_j^2} - k_j^2 \frac{\partial}{\partial k_j^1} \right)$$

n-1 orbital angular momenta

Nonzero Anomalous Moment --> Nonzero orbital angular momentum

# Mapping between LF(3+1) and AdS<sub>5</sub>

*LF(3+1)*

*AdS<sub>5</sub>*

$$\psi(x, \vec{b}_\perp)$$

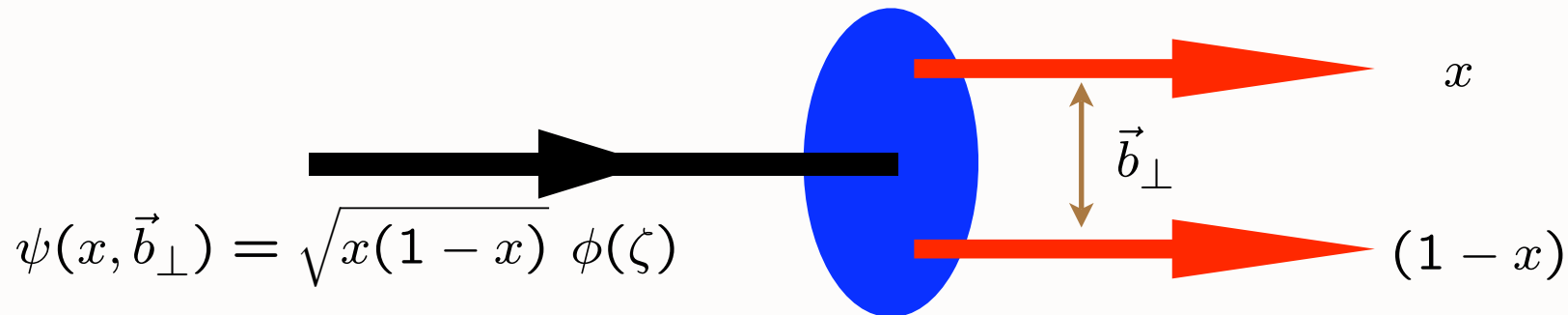


$$\phi(z)$$

$$\zeta = \sqrt{x(1-x)} \vec{b}_\perp^2$$



$$z$$



## Map AdS/CFT to 3+1 LF Theory

Effective radial equation:

$$\left[ -\frac{d^2}{d\zeta^2} + V(\zeta) \right] \phi(\zeta) = \mathcal{M}^2 \phi(\zeta)$$

$$\zeta^2 = x(1-x)\mathbf{b}_\perp^2.$$

Effective conformal potential:

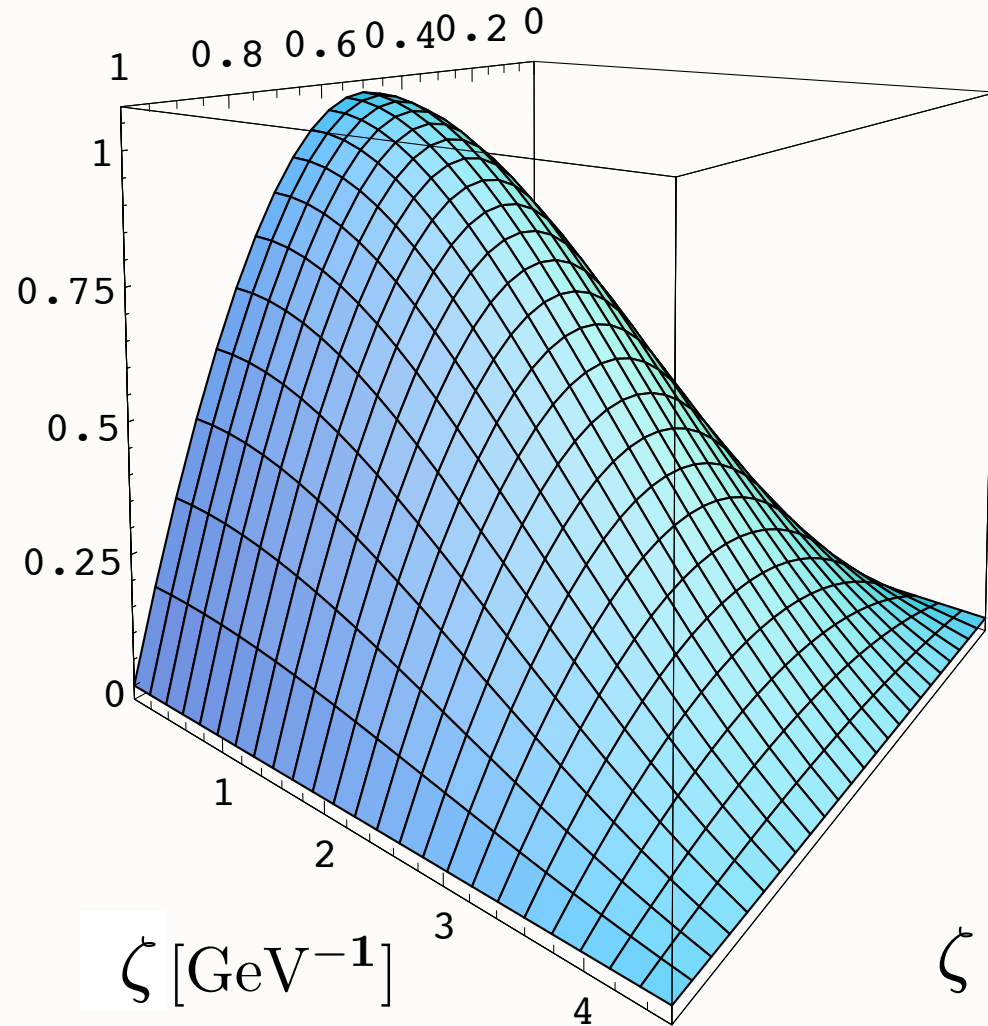
$$V(\zeta) = -\frac{1-4L^2}{4\zeta^2}.$$

General solution:

$$\tilde{\psi}_{L,k}(x, \vec{b}_\perp) = B_{L,k} \sqrt{x(1-x)}$$

$$J_L \left( \sqrt{x(1-x)} |\vec{b}_\perp| \beta_{L,k} \Lambda_{\text{QCD}} \right) \theta \left( \vec{b}_\perp^2 \leq \frac{\Lambda_{\text{QCD}}^{-2}}{x(1-x)} \right),$$

$\psi(\mathbf{x}, \mathbf{b})$



AdS/CFT  
prediction for  
meson LFWF

Holographic Model

Guy de Teramond  
SJB

$$\zeta = b\sqrt{x(1-x)}$$

Two-parton ground state LFWF in impact space  $\psi(x, b)$  for a for  $n = 2, \ell = 0, k = 1$ .

# Hadron Distribution Amplitudes

Lepage; SJB  
Efremov, Radyuskin

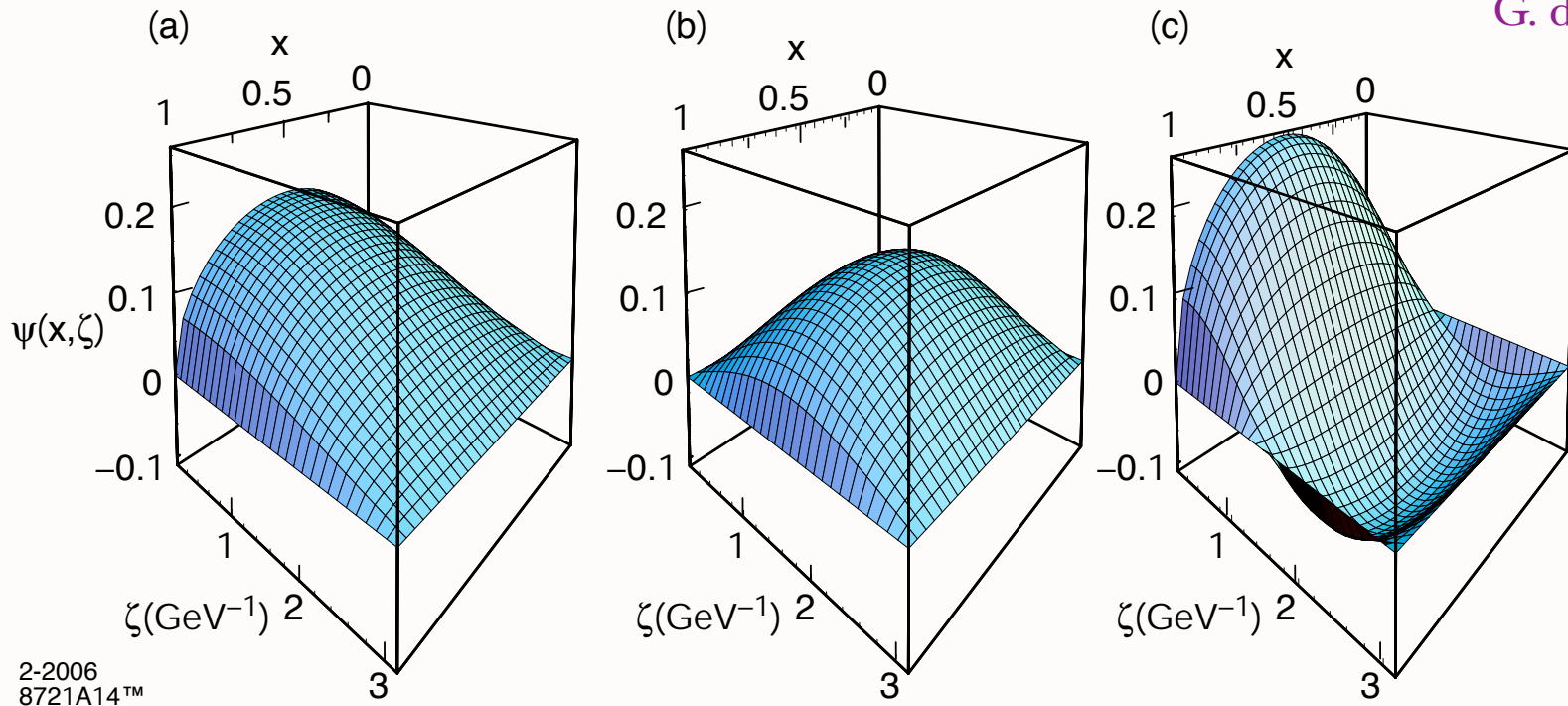
$$\phi(x_i, Q) \equiv \prod_{i=1}^{n-1} \int^Q d^2\vec{k}_\perp \psi_n(x_i, \vec{k}_\perp)$$

- Fundamental measure of valence wavefunction
- Gauge Invariant (includes Wilson line)
- Evolution Equations, OPE
- Conformal Expansion
- Hadronic Input in Factorization Theorems

$$**AdS/CFT:** \quad \phi(x, Q_0) \propto \sqrt{x(1-x)}$$

# AdS/CFT Prediction for Meson LFWF

G. de Teramond  
SJB



Two-parton holographic LFWF in impact space  $\tilde{\psi}(x, \zeta)$  for  $\Lambda_{QCD} = 0.32$  GeV: (a) ground state  $L = 0, k = 1$ ; (b) first orbital excited state  $L = 1, k = 1$ ; (c) first radial excited state  $L = 0, k = 2$ . The variable  $\zeta$  is the holographic variable  $z = \zeta = |b_{\perp}| \sqrt{x(1-x)}$ .

$$\tilde{\psi}(x, \zeta) = \frac{\Lambda_{QCD}}{\sqrt{\pi} J_1(\beta_{0,1})} \sqrt{x(1-x)} J_0(\zeta \beta_{0,1} \Lambda_{QCD}) \theta(z \leq \Lambda_{QCD}^{-1})$$

# Hadronic Form Factor in Space and Time-Like Regions

SJB and GdT in preparation

- The form factor in AdS/QCD is the overlap of the normalizable modes dual to the incoming and outgoing hadron  $\Phi_I$  and  $\Phi_F$  and the non-normalizable mode  $J$ , dual to the external source (hadron spin  $\sigma$ ):

$$\begin{aligned} F(Q^2)_{I \rightarrow F} &= R^{3+2\sigma} \int_0^\infty \frac{dz}{z^{3+2\sigma}} e^{(3+2\sigma)A(z)} \Phi_F(z) J(Q, z) \Phi_I(z) \\ &\simeq R^{3+2\sigma} \int_0^{z_0} \frac{dz}{z^{3+2\sigma}} \Phi_F(z) J(Q, z) \Phi_I(z), \end{aligned}$$

- $J(Q, z)$  has the limiting value 1 at zero momentum transfer,  $F(0) = 1$ , and has as boundary limit the external current,  $A^\mu = \epsilon^\mu e^{iQ \cdot x} J(Q, z)$ . Thus:

$$\lim_{Q \rightarrow 0} J(Q, z) = \lim_{z \rightarrow 0} J(Q, z) = 1.$$

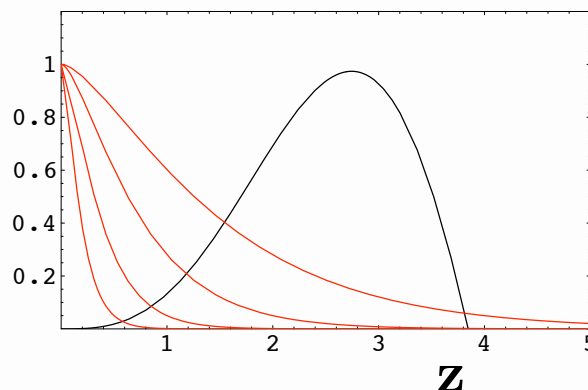
- Solution to the AdS Wave equation with boundary conditions at  $Q = 0$  and  $z \rightarrow 0$ :

$$J(Q, z) = zQ K_1(zQ).$$

Polchinski and Strassler, hep-th/0209211; Hong, Yong and Strassler, hep-th/0409118.

- Propagation of external perturbation suppressed inside AdS.
- At large enough  $Q \sim r/R^2$ , the interaction occurs in the large- $r$  conformal region. Important contribution to the FF integral from the boundary near  $z \sim 1/Q$ .

$\mathbf{J(Q, z), \Phi(z)}$



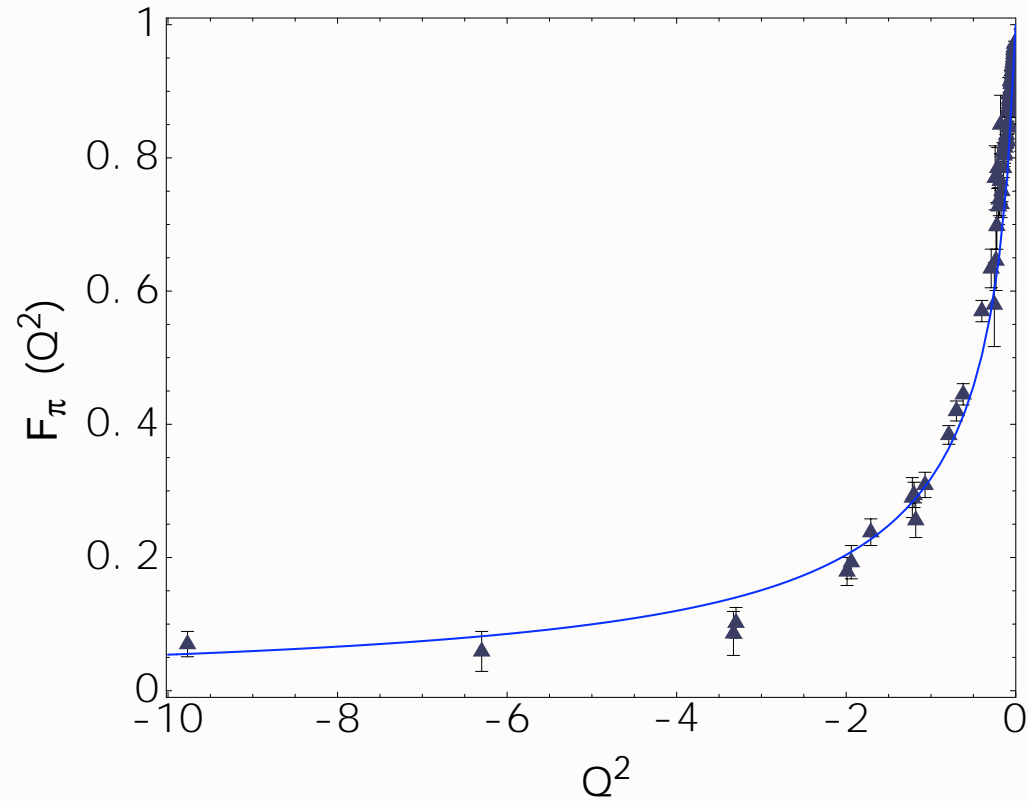
- Consider a specific AdS mode  $\Phi^{(n)}$  dual to an  $n$  partonic Fock state  $|n\rangle$ . At small  $z$ ,  $\Phi^{(n)}$  scales as  $\Phi^{(n)} \sim z^{\Delta_n}$ . Thus:

$$F(Q^2) \rightarrow \left[ \frac{1}{Q^2} \right]^{\tau-1},$$

General result from  
AdS/CFT

where  $\tau = \Delta_n - \sigma_n$ ,  $\sigma_n = \sum_{i=1}^n \sigma_i$ . The twist is equal to the number of partons,  $\tau = n$ .

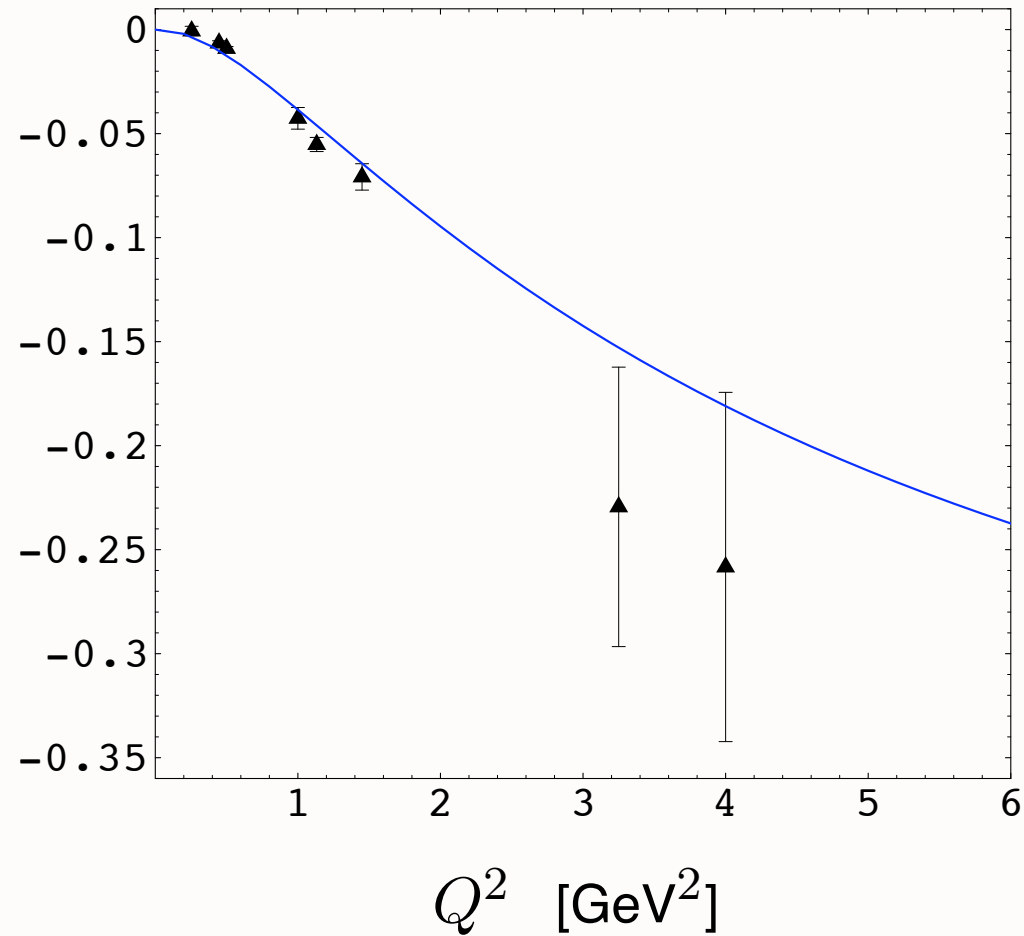




Space-like pion form factor in holographic model for  $\Lambda_{QCD} = 0.2$  GeV.

$Q^4 F_1^n(Q^2)$  [GeV<sup>4</sup>]

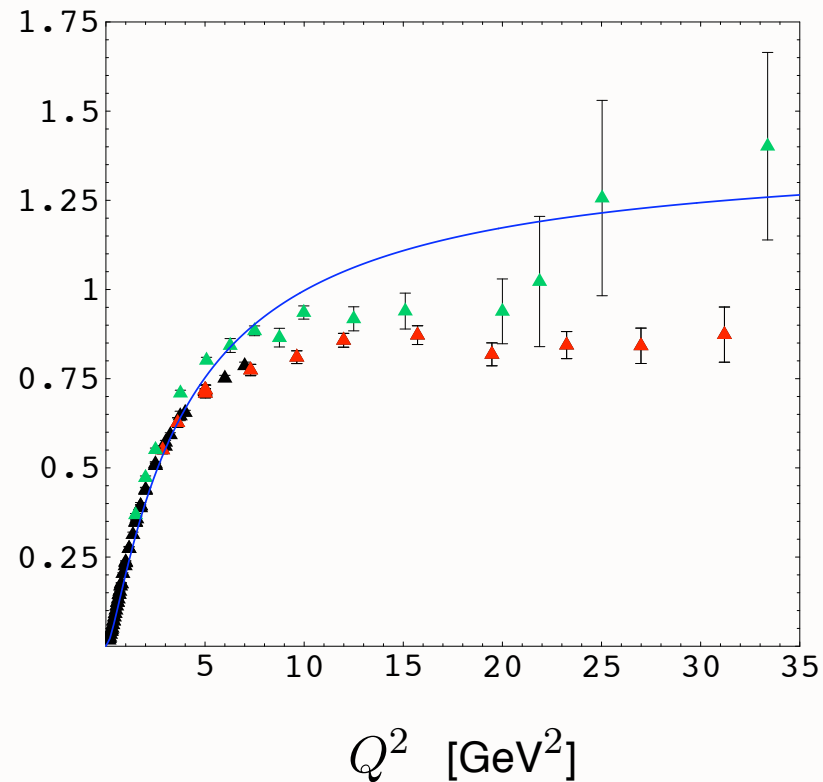
Dirac Neutron Form Factor  $F_1^n$



Prediction for  $Q^4 F_1^n(Q^2)$  for  $\Lambda_{\text{QCD}} = 0.21$  GeV in the infinite wall approximation.

# Dirac Proton Form Factor $F_1^p$

$$Q^4 F_1^p(Q^2) \text{ [GeV}^4\text{]}$$



Prediction for  $Q^4 F_1^p(Q^2)$  for  $\Lambda_{\text{QCD}} = 0.21 \text{ GeV}$  in the infinite wall approximation

from Kirk (superimposed green points assuming  $G_E^p = G_M^p$ ): P. N. Kirk *et al.*, Phys. Rev. D **8** (1973) 63.

# New Perspectives on QCD from AdS/CFT

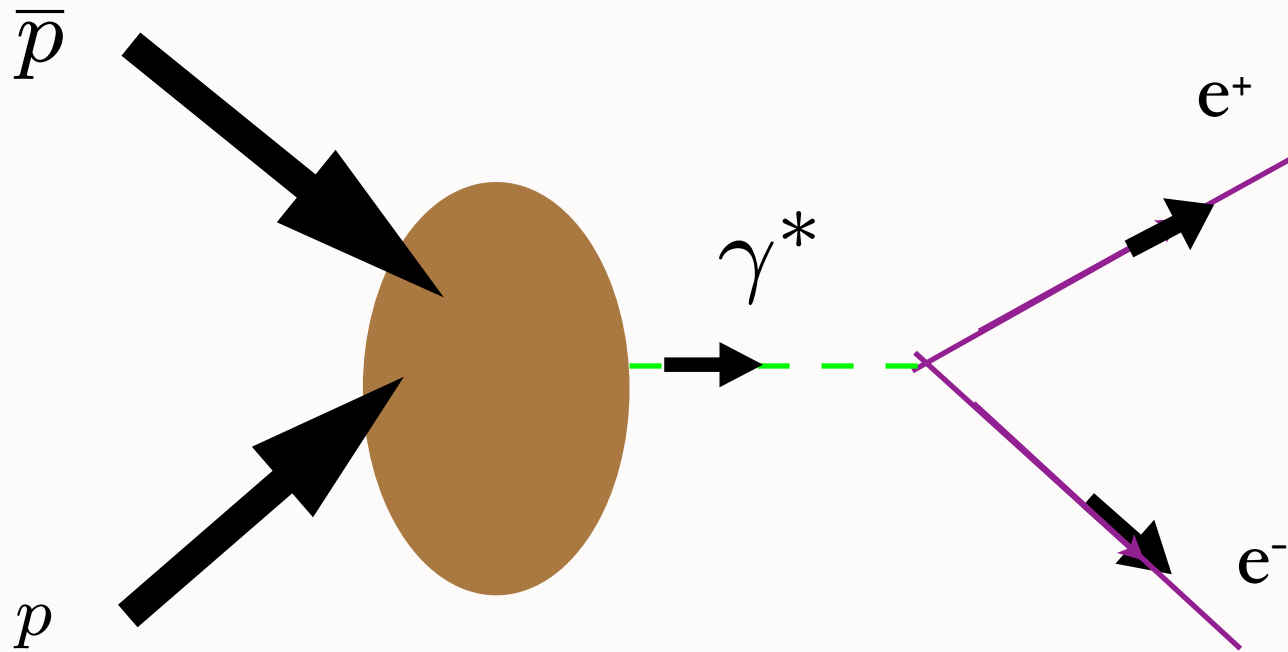
- Holographic Model from AdS/CFT : Confinement at large distances and conformal behavior at short distances
- AdS/CFT predicts Light-front wavefunctions:  
Fundamental description of hadrons at amplitude level
- AdS/CFT: gluonium ( $gg$ ) , meson ( $q \bar{q}$ ), and baryon ( $qqq$ ) spectra
- No  $ggg$  bound states -- No Odderon!
- Quark-interchange dominates scattering amplitudes !!

- **Polchinski & Strassler:** AdS/CFT builds in conformal symmetry at short distances, counting, rules for form factors and hard exclusive processes; non-perturbative derivation
- **Goal:** Use AdS/CFT to provide models of hadron structure: confinement at large distances, near conformal behavior at short distances
- **Holographic Model:** Initial “classical” approximation to QCD: Remarkable agreement with light hadron spectroscopy
- Use AdS/CFT wavefunctions as expansion basis for diagonalizing  $H^{\text{LF}}_{\text{QCD}}$ ; variational methods

# Consequences of AdS/CFT for Antiproton physics

- Analytic form for form factors, distribution amplitude
- Matrix elements and LFWFs for baryon scattering amplitudes: Quark Counting Rules!
- Orbital angular momentum in baryon wavefunction for Pauli form factor, SSAs
- Dominance of quark interchange at short distances
- Effective Regge trajectories

# Measurement of hadron time-like form factors angular distributions



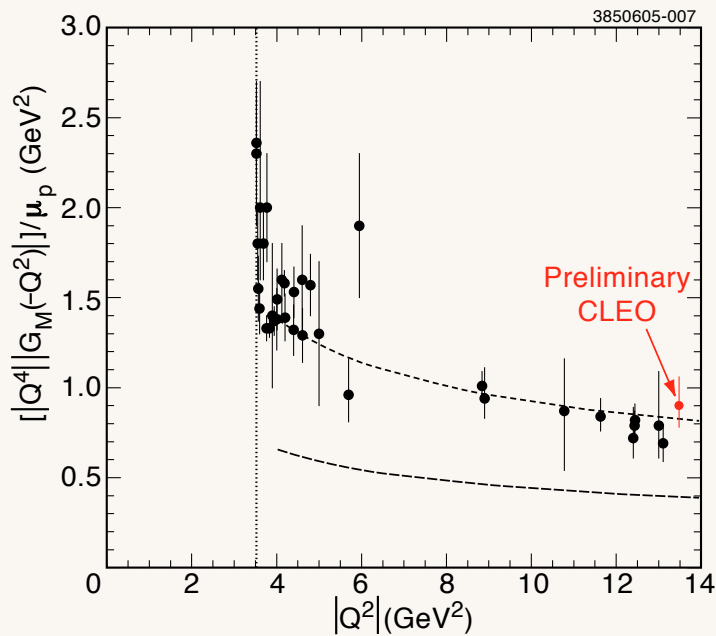
**Separate  $F_1, F_2$**

Leading power in  
QCD

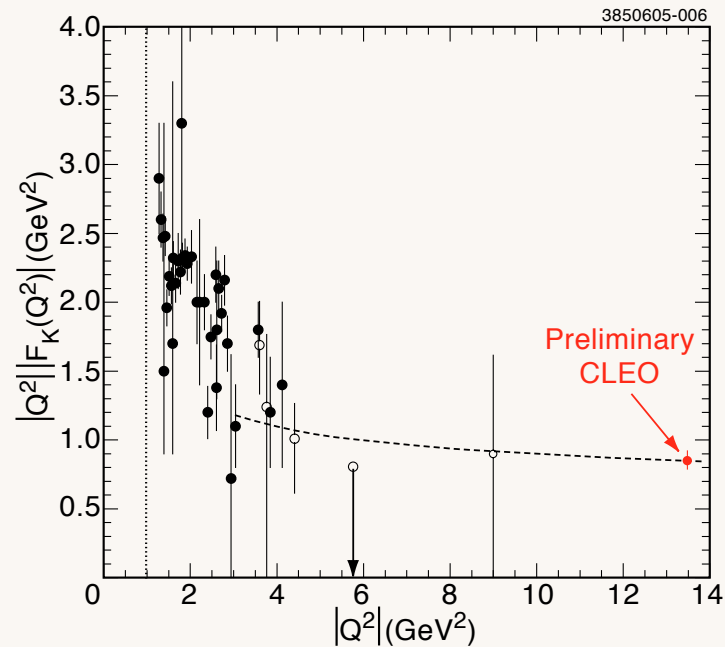
$$F_H(s) \propto \left[\frac{1}{s}\right]^{n_H-1}$$

*Test QCD Counting Rules  
Conformal Symmetry: AdS/CFT  
Hadron Helicity Conservation*

$$\sum_{\text{initial}} \lambda_H - \sum_{\text{total}} \lambda_H = 0,$$



Proton timelike form factor.



Kaon timelike form factor.

## New results from CLEO

$$Q^2 |F_K(13.48 \text{ GeV}^2)| = 0.85 \pm 0.05(\text{stat}) \pm 0.02(\text{syst}) \text{ GeV}^2$$

$$Q^4 |G_M^p(13.48 \text{ GeV}^2)| = 2.54 \pm 0.36(\text{stat}) \pm 0.16(\text{syst}) \text{ GeV}^4$$

The proton magnetic form factor result agrees with that measured in the reverse reaction  $p\bar{p} \rightarrow e^+e^-$  at Fermilab. **The kaon form factor measurement is the first ever direct measurement at  $|Q^2| > 4 \text{ GeV}^2$ .**



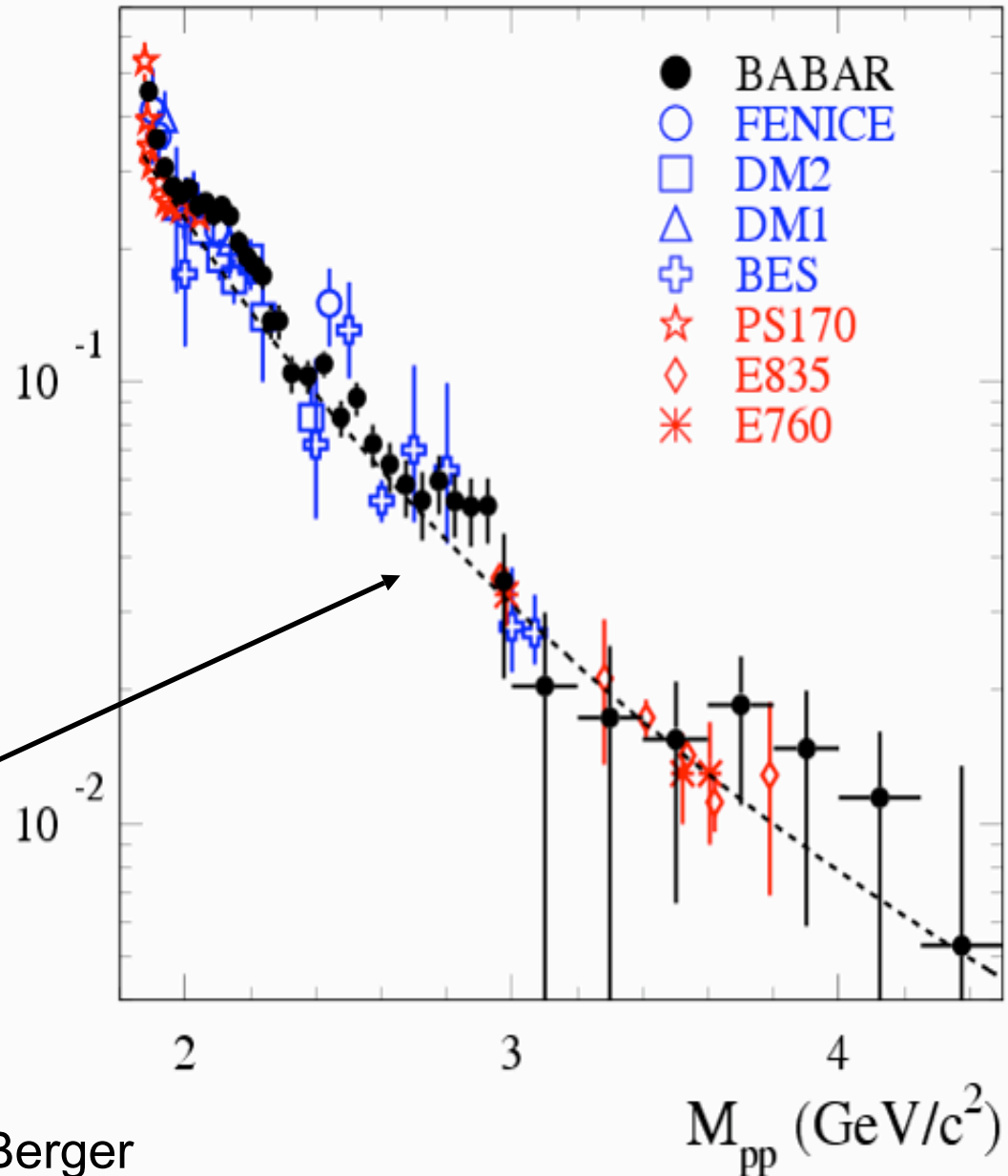
# Timelike Proton Form Factor

- Define “Effective” form factor by

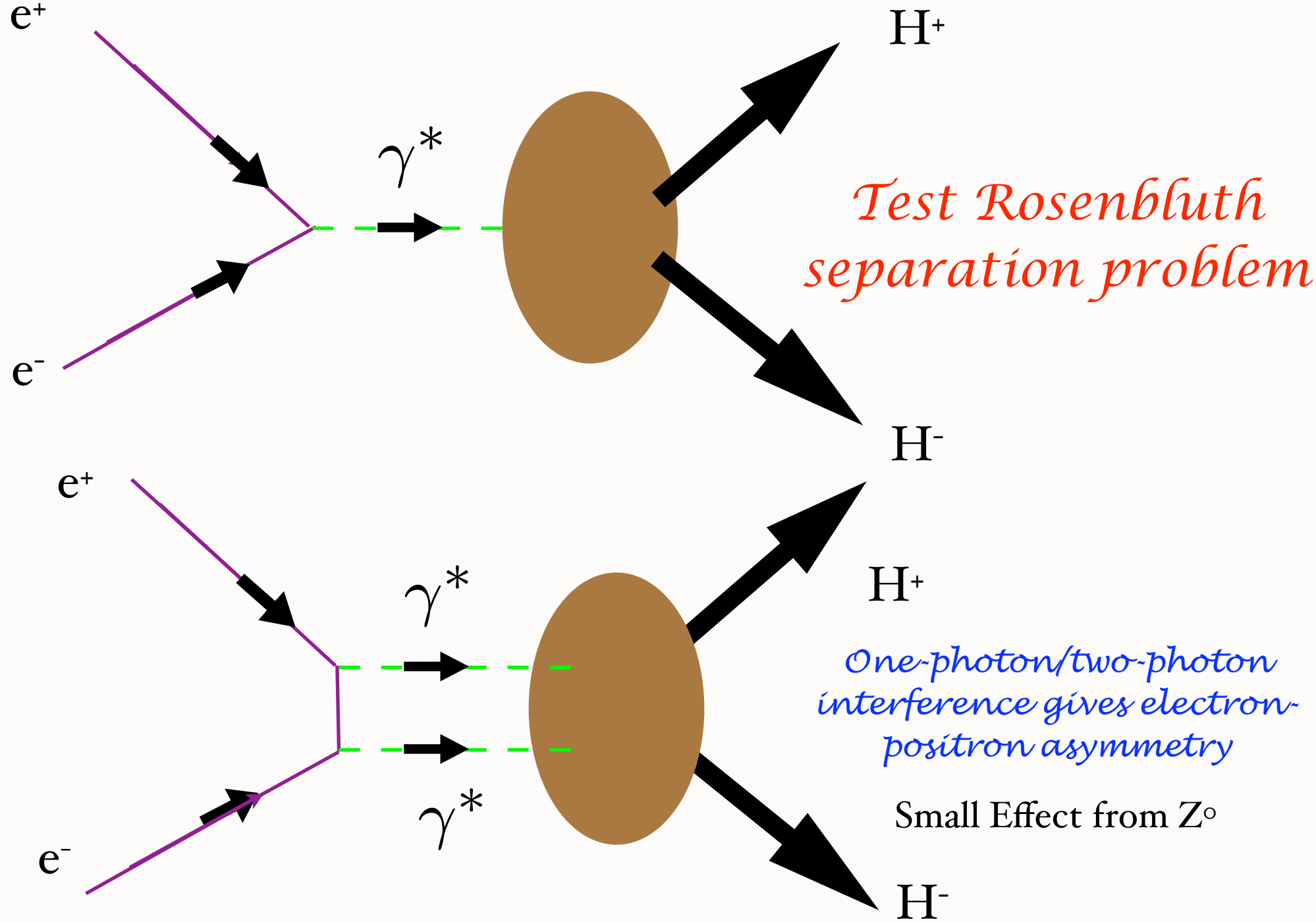
$$\sigma = \frac{4\pi\alpha^2\beta C}{3m_{p\bar{p}}^2} |F|^2, \quad |F| = \sqrt{|G_M|^2 + \frac{2m_p^2}{m_{p\bar{p}}^2} |G_E|^2}.$$

- Peak at threshold, sharp dips at 2.25 GeV, 3.0 GeV.
- Good fit to pQCD prediction for high  $m_{p\bar{p}}$ .

Proton form factor

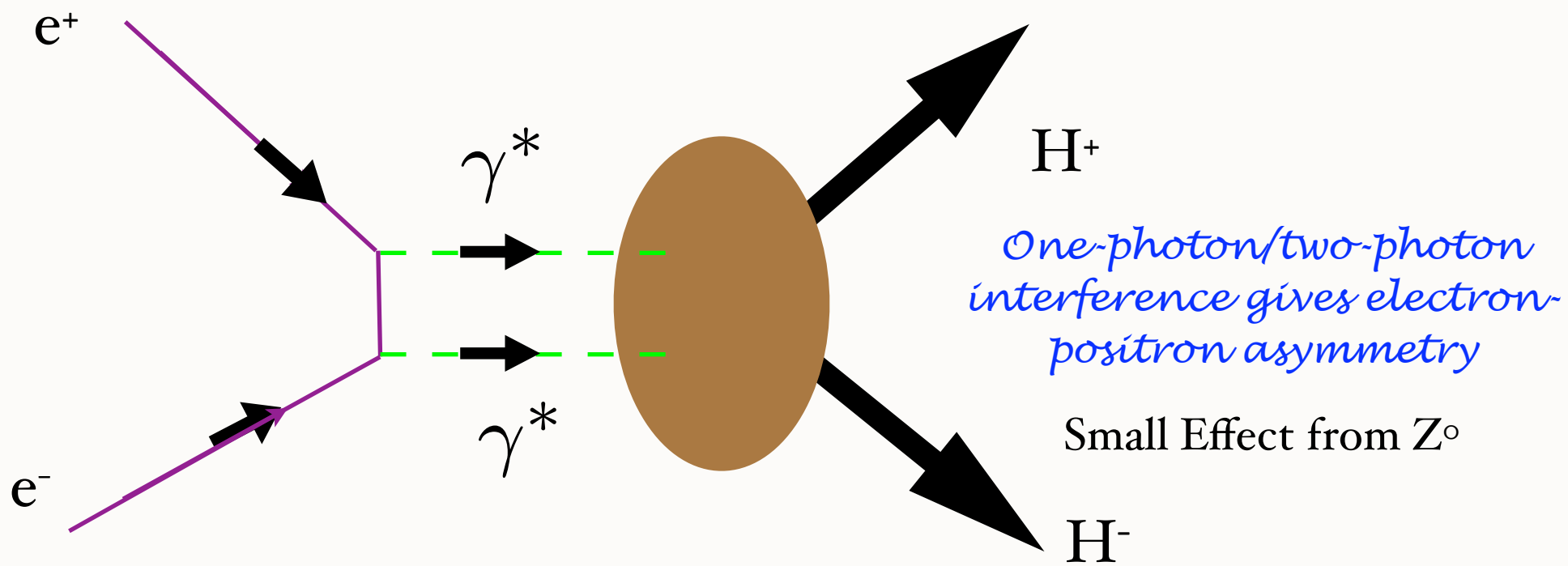


$$F(s) \propto \frac{\log^{-2} \frac{s}{\Lambda^2}}{s^2}$$



- Two-photon exchange correction, elastic and inelastic nucleon channels, give significant interference with one-photon exchange, destroys Rosenbluth method

Blunden, Melnitchouk; Afanasev, Chen, Carlson, Vanderhaegen, sjb



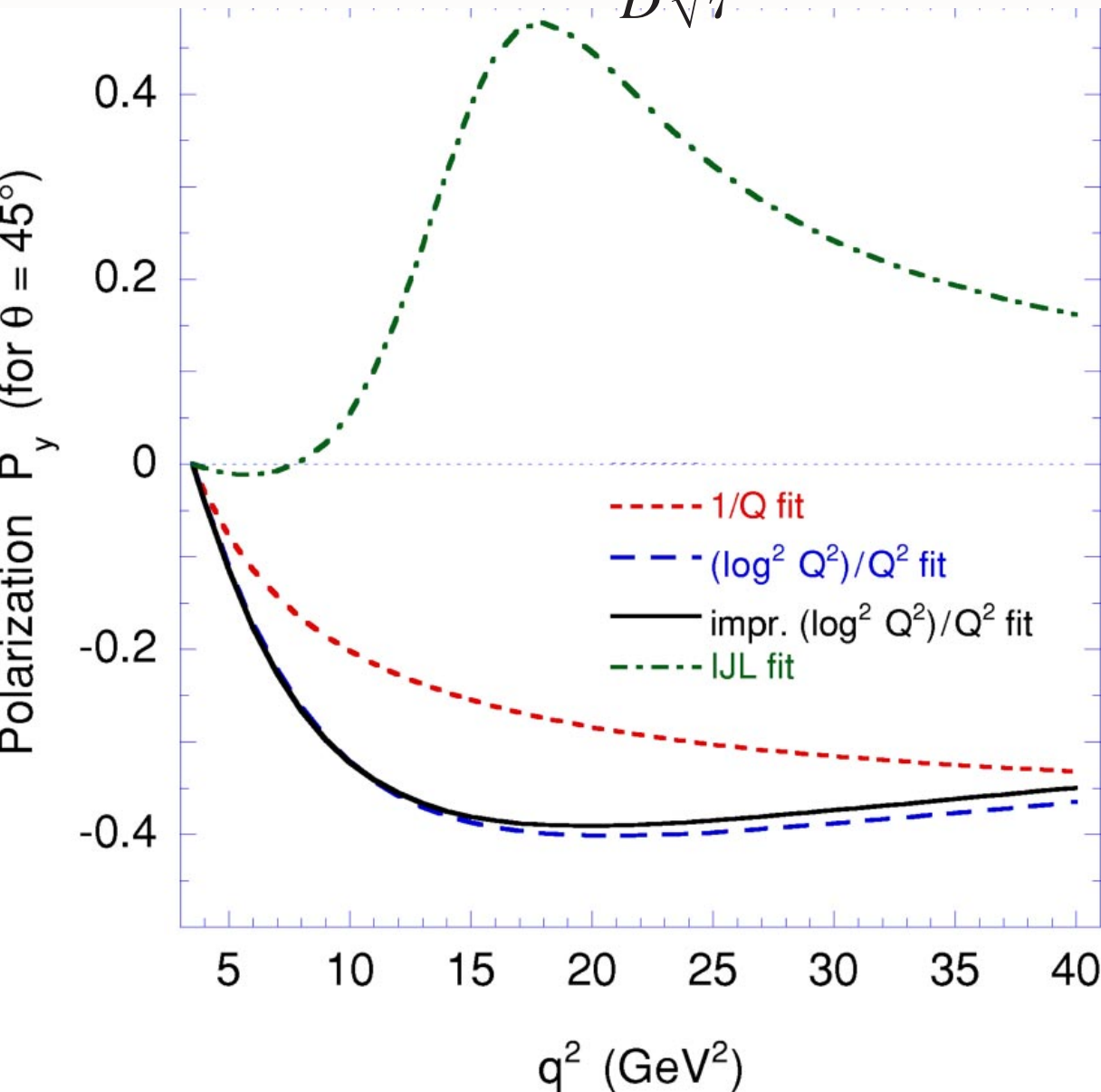
# Single-spin polarization effects and the determination of timelike proton form factors

Carlson, Hiller,  
Hwang, sjb

$$\mathcal{P}_y = \frac{\sin 2\theta \operatorname{Im} G_E^* G_M}{D\sqrt{\tau}} = \frac{(\tau-1)\sin 2\theta \operatorname{Im} F_2^* F_1}{D\sqrt{\tau}}$$

$$D = |G_M|^2(1 + \cos^2\theta) + \frac{1}{\tau}|G_E|^2\sin^2\theta;$$

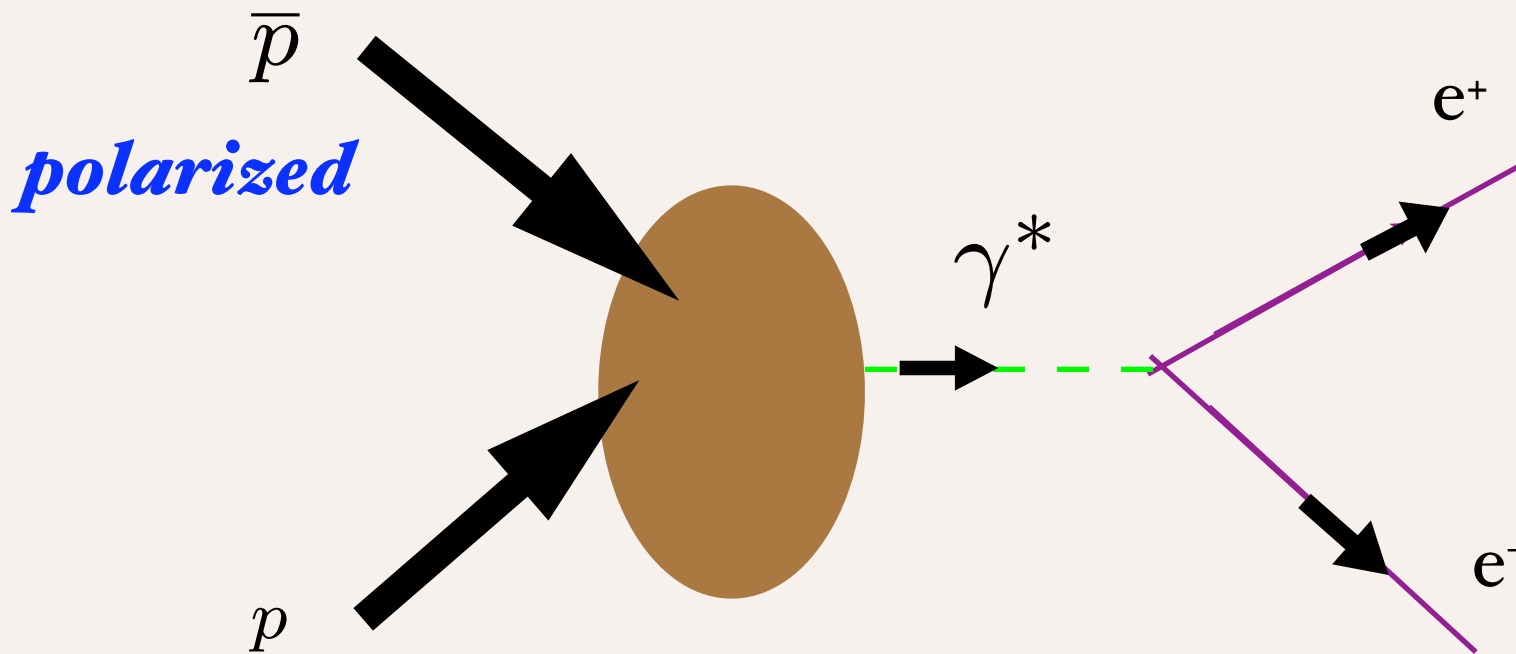
$$\tau \equiv q^2/4m_B^2$$



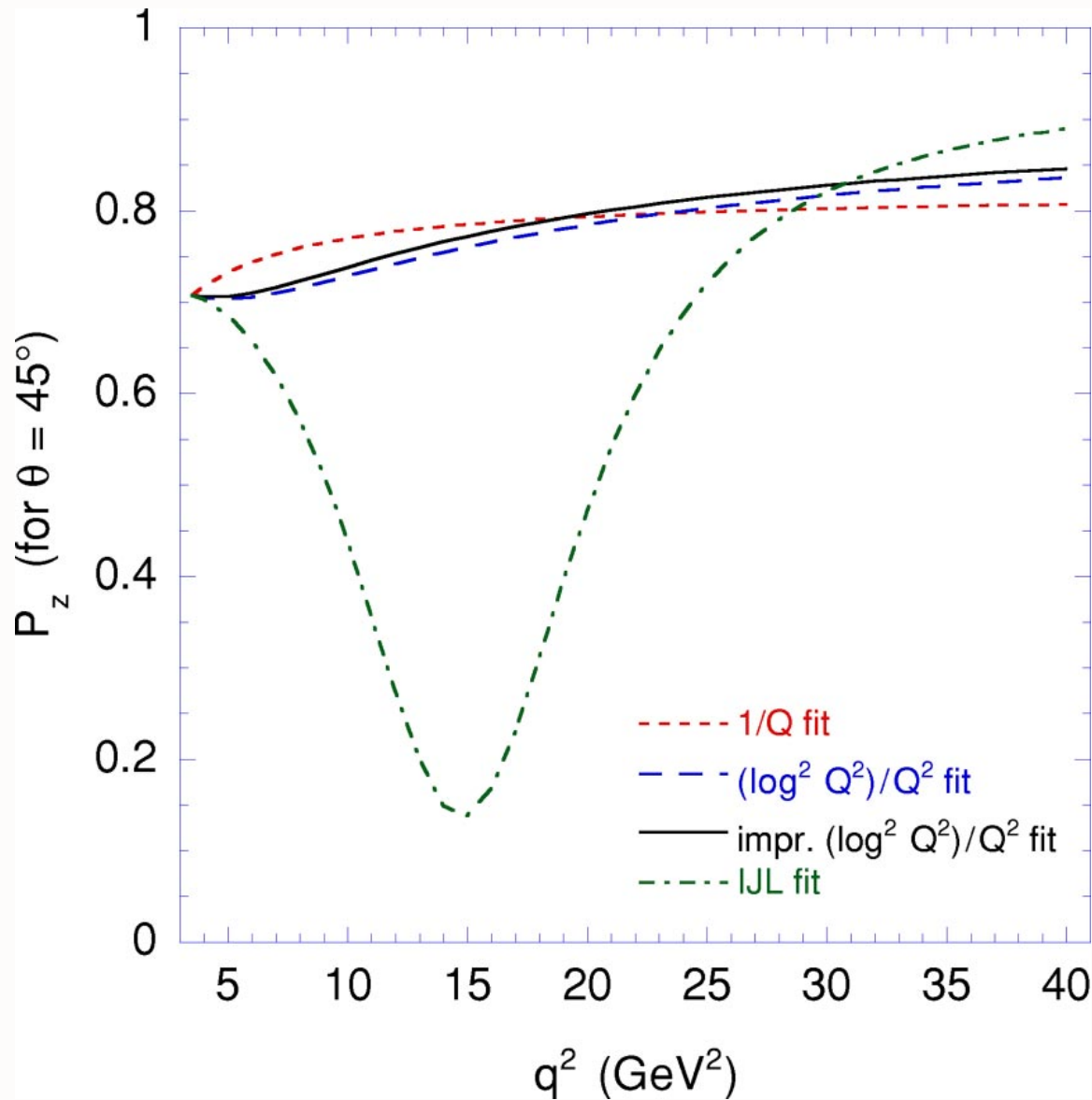
*Measure interference  
of form factors*

# Key QCD Experiment at GSI

$$\mathcal{P}_y = \frac{\sin 2\theta \operatorname{Im} G_E^* G_M}{D\sqrt{\tau}} = \frac{(\tau - 1) \sin 2\theta \operatorname{Im} F_2^* F_1}{D\sqrt{\tau}}$$



# Single-spin polarization effects and the determination of timelike proton form factors



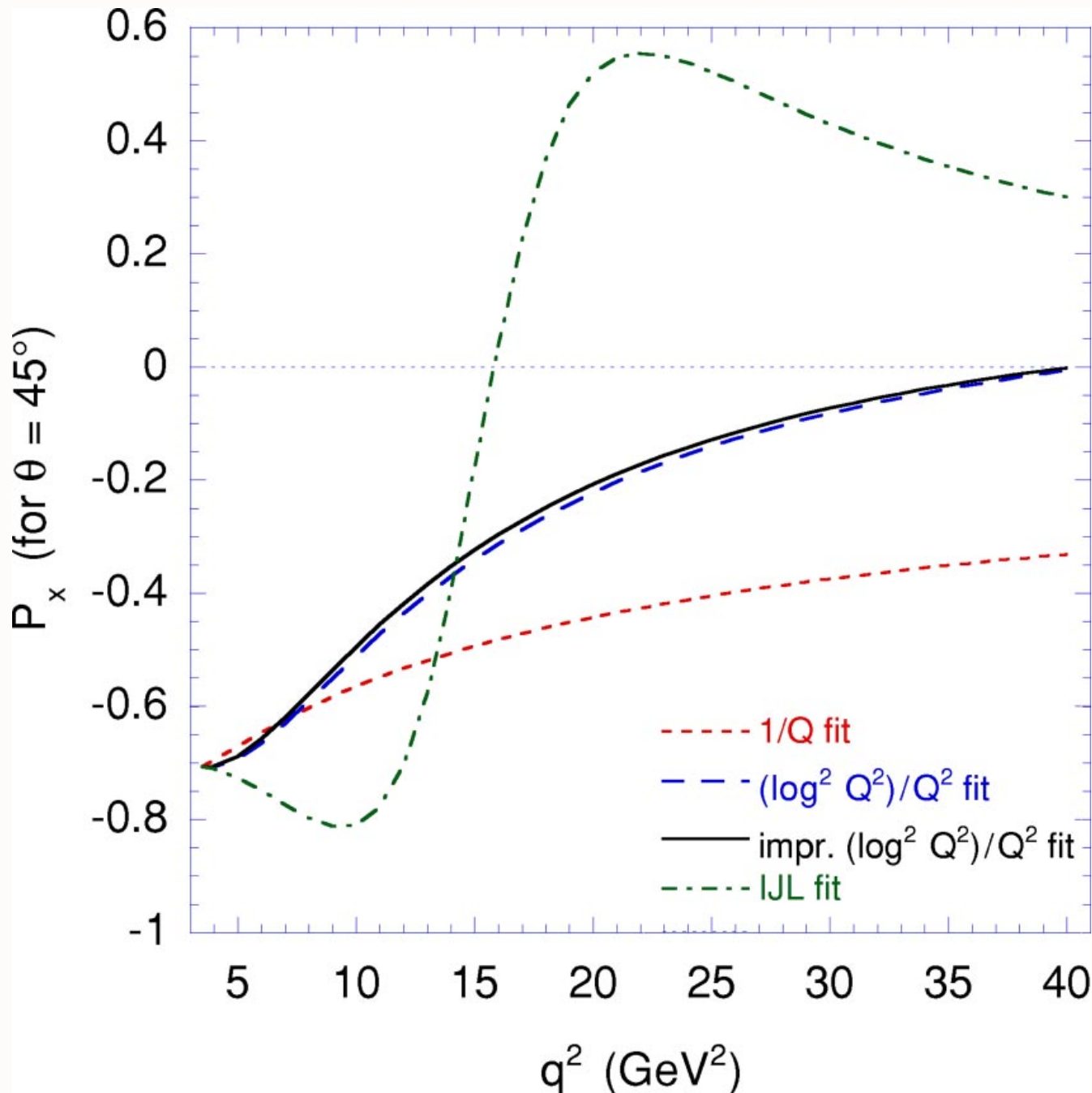
Carlson, Hiller,  
Hwang, sjb

$$\mathcal{P}_z = P_e \frac{2 \cos \theta |G_M|^2}{D}$$

$$D = |G_M|^2 (1 + \cos^2 \theta) + \frac{1}{\tau} |G_E|^2 \sin^2 \theta;$$

*Requires beam and lepton polarization*

# Single-spin polarization effects and the determination of timelike proton form factors



Carlson, Hiller,  
Hwang, sjb

$$\mathcal{P}_x = -P_e \frac{2 \sin \theta \operatorname{Re} G_E^* G_M}{D \sqrt{\tau}}$$

$$D = |G_M|^2 (1 + \cos^2 \theta) + \frac{1}{\tau} |G_E|^2 \sin^2 \theta;$$

*Requires beam and lepton polarization*

*Super B III  
June 15, 2006*

**Novel Tests of QCD at Super B**

# Key QCD Experiment at GSI

$$\frac{d\sigma}{dt}(\bar{p}p \rightarrow \bar{p}p) \text{ at large } p_T$$

Test PQCD AdS/CFT conformal scaling:  
twist = dimension - spin = 12

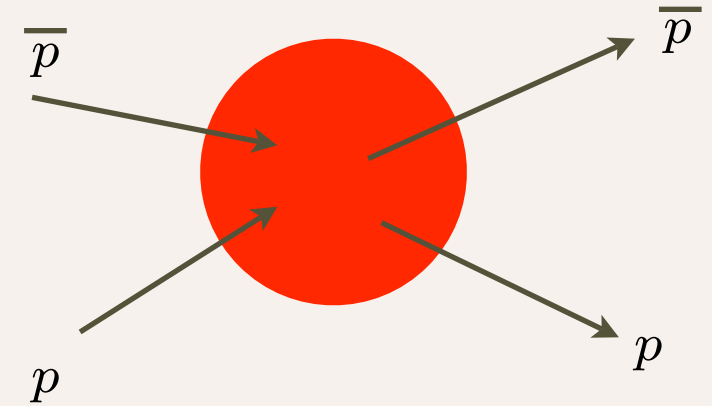
$$\frac{d\sigma}{dt}(\bar{p}p \rightarrow \bar{p}p) \sim \frac{|F(t/s)|^2}{s^{10}}$$

Test Quark Interchange Mechanism

Single-spin asymmetry  $A_N$

Exclusive Transversity  $A_{NN}$

Test color transparency



$$M(s, t) \sim \frac{F(t/s)}{s^4}$$

$$M \propto \frac{1}{s^2 u^2}$$

*Study Fundamental Aspects of  
Nuclear Force*



$$\frac{d\sigma}{dt}(pp \rightarrow pp) = \frac{F(t/s)}{s^{9.7 \pm 0.5}}$$

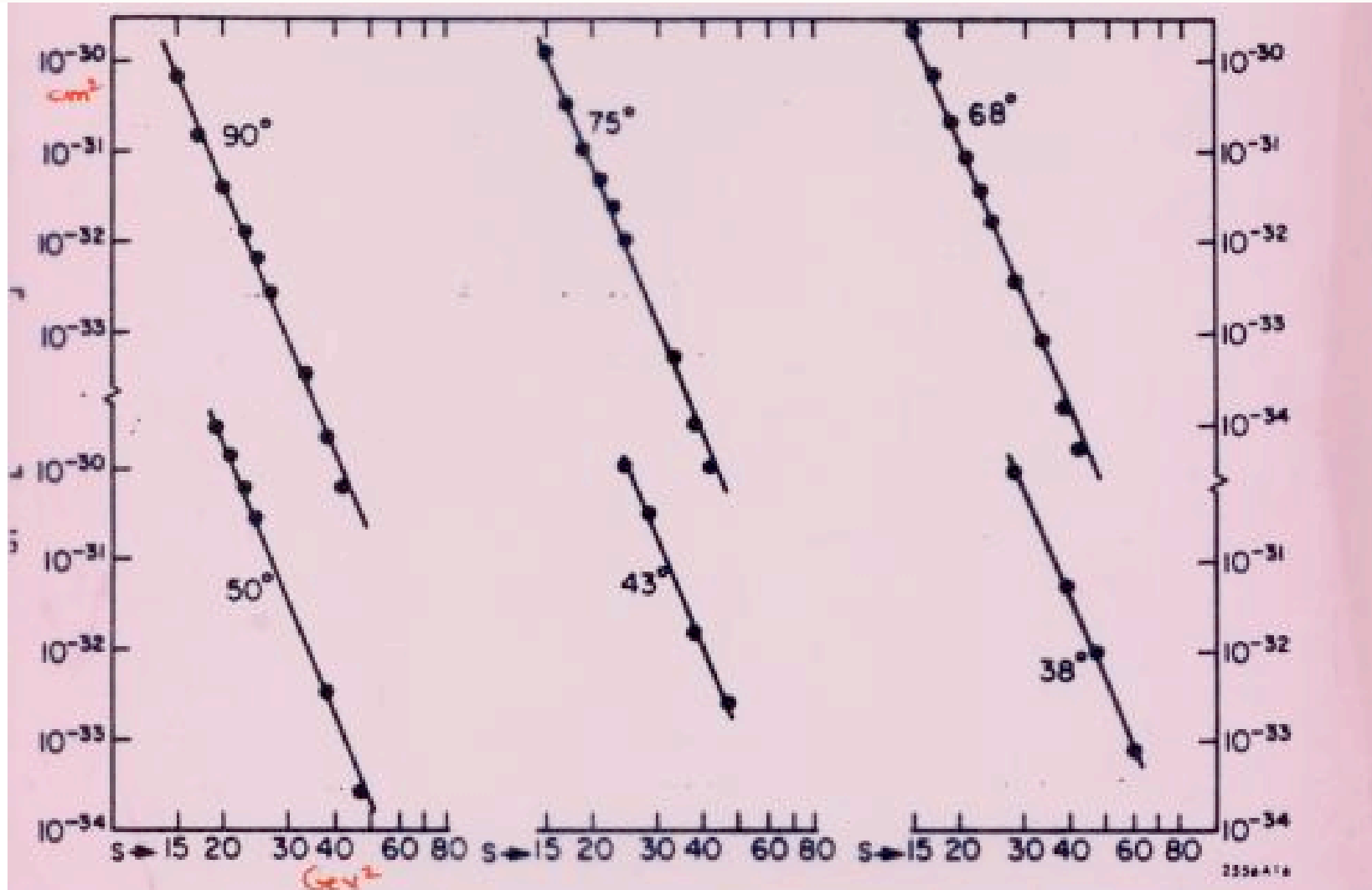
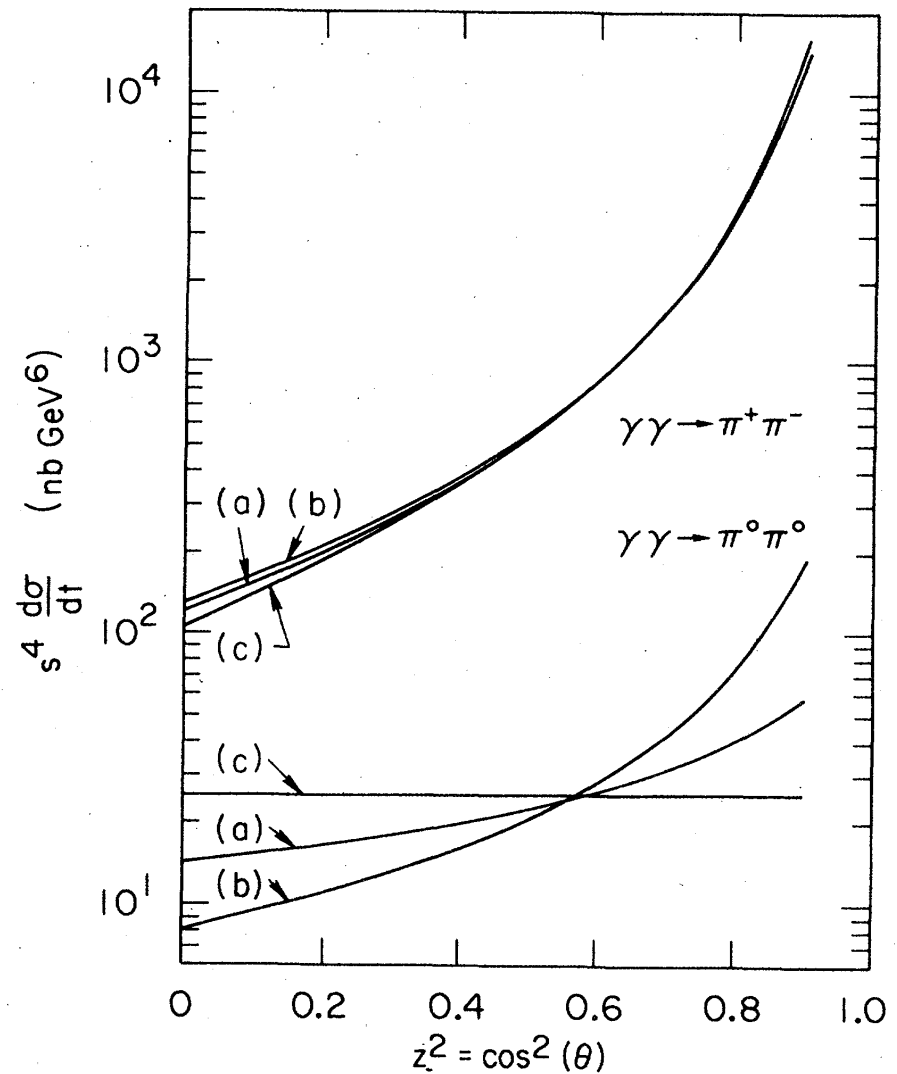
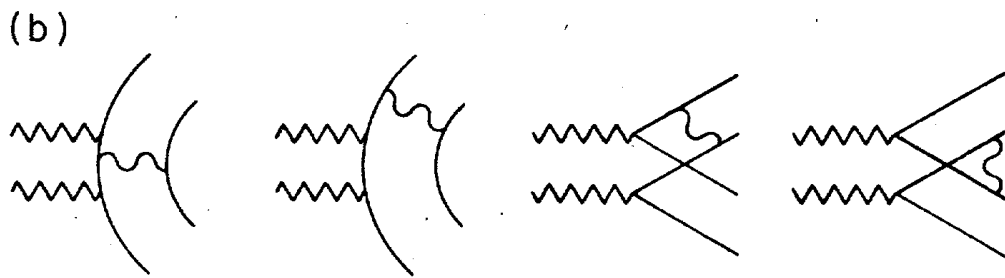
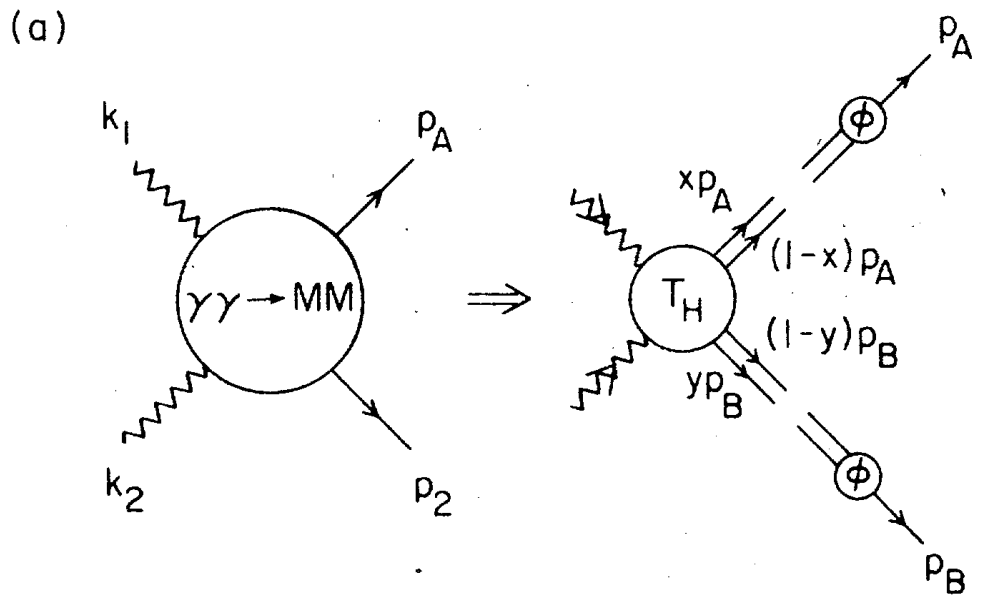


Figure 22. Test of fixed  $\theta_{CM}$  scaling for elastic  $pp$  scattering. The data compilation is Landshoff and Polkinghorne.

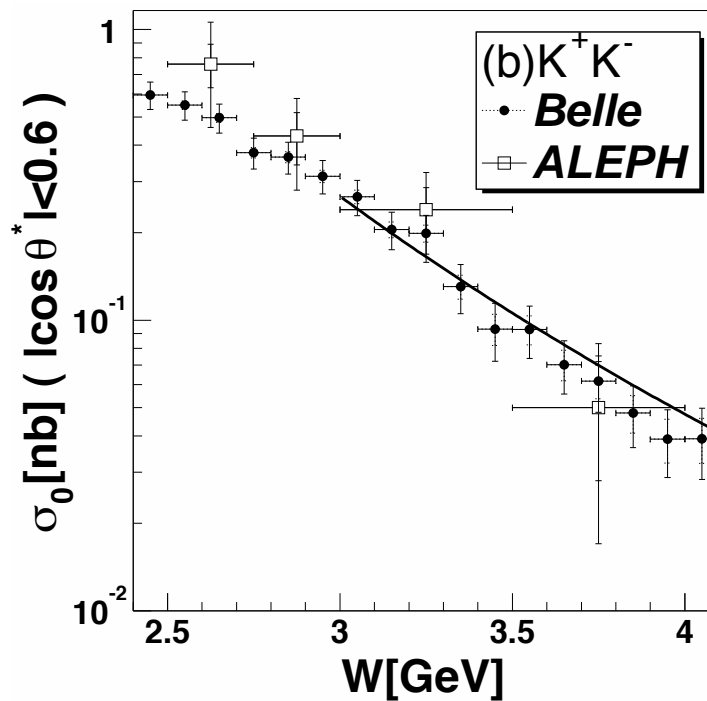
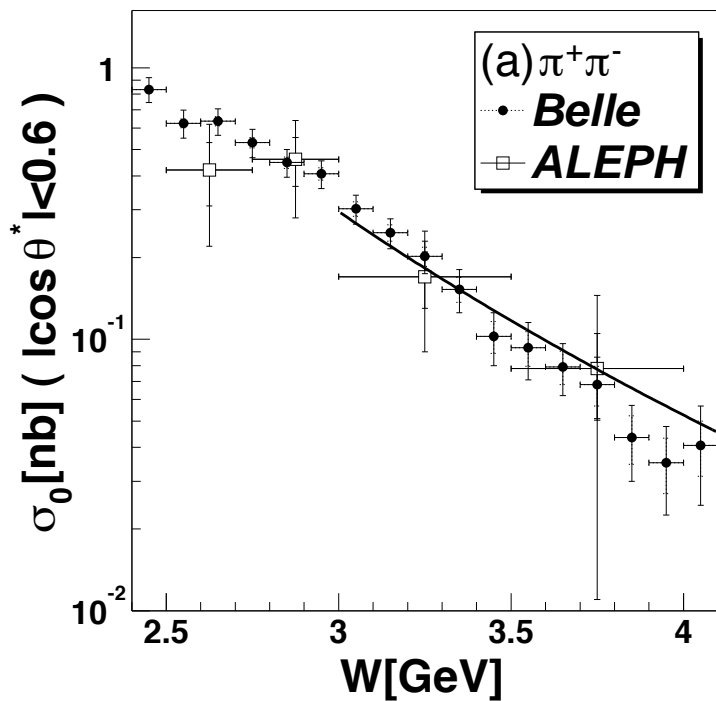
But: Oscillations, Anomalous  $A_N$ ,  $A_{NN}$



Lepage & sjb

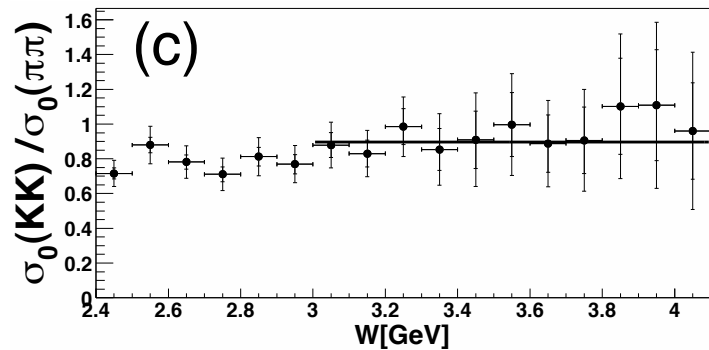
$$\frac{\frac{d\sigma}{dt}(\gamma\gamma \rightarrow \pi^+\pi^-)}{\frac{d\sigma}{dt}(\gamma\gamma \rightarrow \mu^+\mu^-)} \sim \frac{4 |F_\pi(s)|^2}{1 - \cos^4 \theta_{\text{c.m.}}}$$

**Ratio: Crucial test of Kroll's handbag model**



Two Photon Reactions

Hard Exclusive Processes:  
Fixed angle



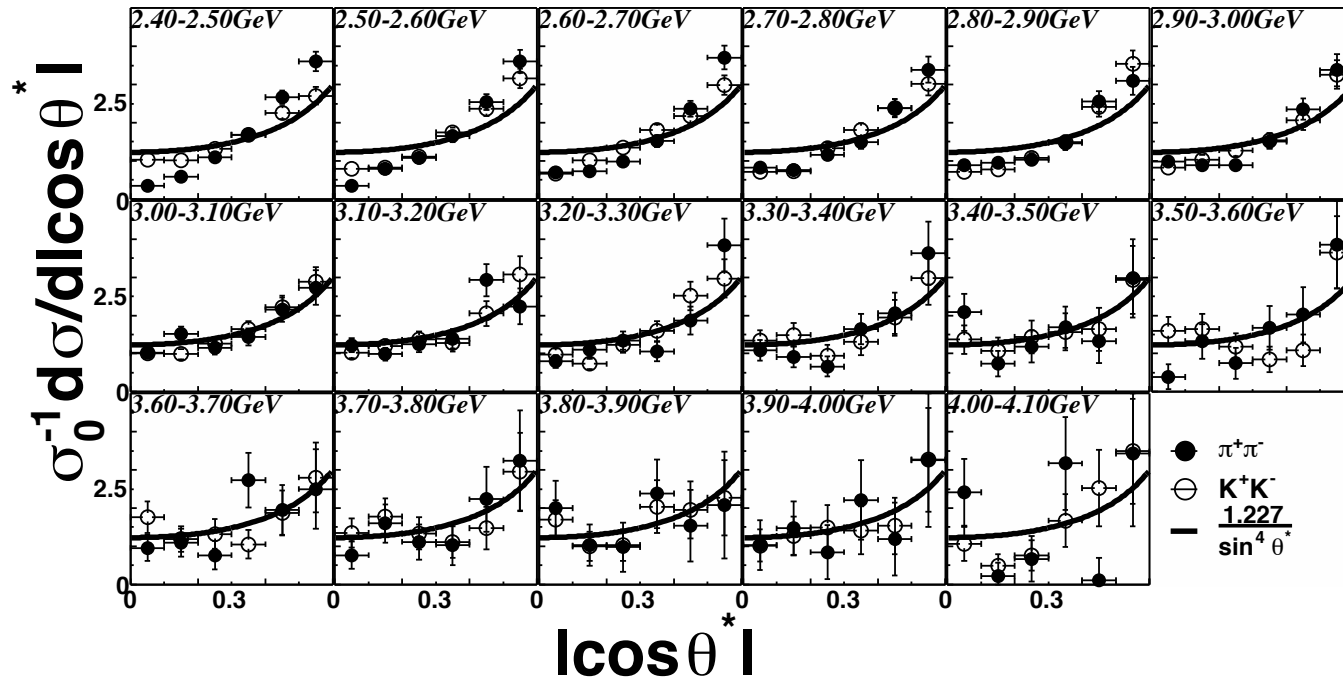
PQCD, AdS/CFT:

$$\Delta\sigma(\gamma\gamma \rightarrow \pi^+\pi^-, K^+, K^-) \sim 1/W^6$$

$$|\cos(\theta_{CM})| < 0.6$$

Fig. 5. Cross section for (a)  $\gamma\gamma \rightarrow \pi^+\pi^-$ , (b)  $\gamma\gamma \rightarrow K^+K^-$  in the c.m. angular region  $|\cos \theta^*| < 0.6$  together with a  $W^{-6}$  dependence line derived from the fit of  $s|R_M|$ . (c) shows the cross section ratio. The solid line is the result of the fit for the data above 3 GeV. The errors indicated by short ticks are statistical only.

PQCD: 
$$\frac{d\sigma}{d|\cos\theta^*|}(\gamma\gamma \rightarrow M^+M^-) \approx \frac{16\pi\alpha^2}{s} \frac{|F_M(s)|^2}{\sin^4\theta^*},$$



4. Angular dependence of the cross section,  $\sigma_0^{-1}d\sigma/d|\cos\theta^*|$ , for the  $\pi^+\pi^-$  (closed circles) and  $K^+K^-$  (open circles) processes. The curves are  $1.227 \times \sin^{-4}\theta^*$ . The errors are statistical only.

Measurement of the  $\gamma\gamma \rightarrow \pi^+\pi^-$  and  $\gamma\gamma \rightarrow K^+K^-$  processes at energies of 2.4–4.1 GeV

Belle Collaboration

Trento  
July 5, 2006

AdS/CFT, QCD, & GSI  
80

Stan Brodsky, SLAC

# Key QCD Experiment at GSI

*Measure all antiproton + proton exclusive channels*

$$\bar{p}p \rightarrow \gamma\gamma$$

PQCD: No handbag dominance  
for real photons

$J = 0$  fixed pole from  
local  $q\bar{q} \rightarrow \gamma\gamma$  interactions

$$\bar{p}p \rightarrow \gamma\pi^0$$

$$\bar{p}p \rightarrow K^+K^-$$

# Remarkable prediction of AdS/CFT: Dominance of quark interchange

Example:  $M(K^+p \rightarrow K^+p) \propto \frac{1}{ut^2}$

Exchange of common  $u$  quark

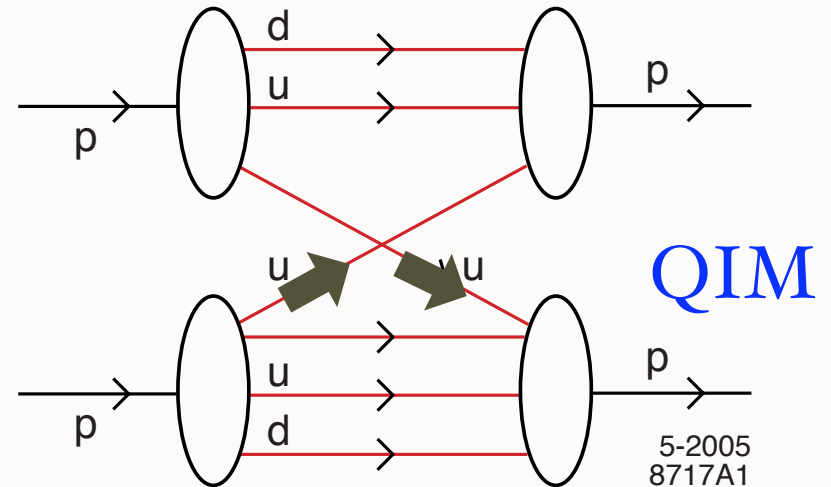
$$M_{QIM} = \int d^2k_{\perp} dx \psi_C^{\dagger} \psi_D^{\dagger} \Delta \psi_A \psi_B$$

Holographic model (Classical level):

Hadrons enter 5th dimension of  $AdS_5$

Quarks travel freely within cavity as long as separation  $z < z_0 = \frac{1}{\Lambda_{QCD}}$

LFWFs obey conformal symmetry producing quark counting rules.

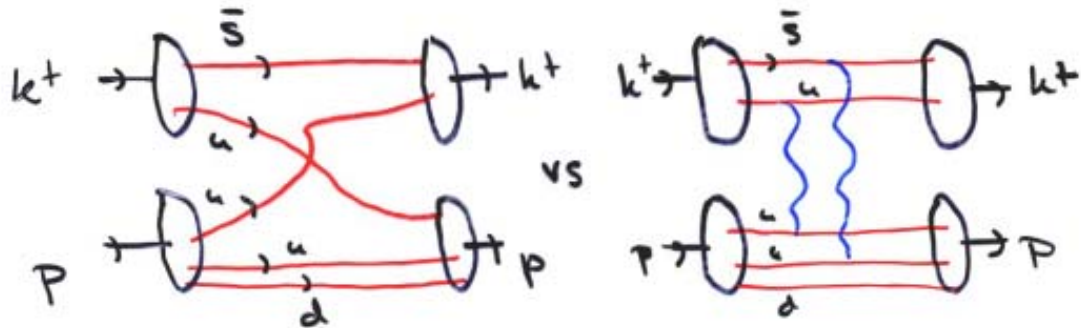


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Angular Distribution  $-t/s = \frac{1}{2}(1 - \cos\theta_{cm})$

$$\frac{d\sigma}{dt} = \frac{1}{s^{n_{TOT}-2}} F(t/s)$$

determined by scattering mechanism



Quark Interchange

gluon exchange

↑  
Analogous to spin exchange  
in atom-atom scattering

Van der Waals

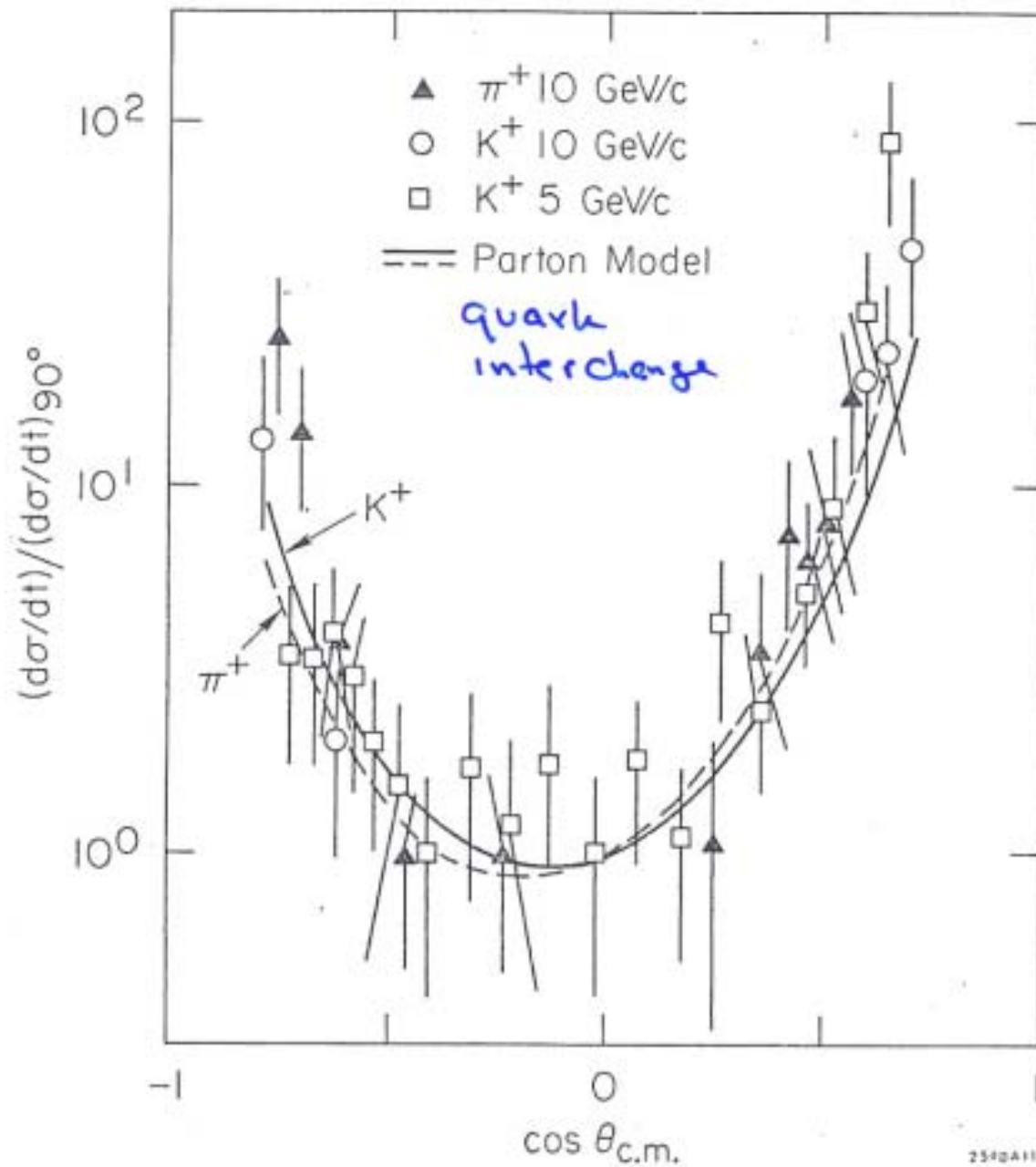
Large  $N_c$ : Quark Interchange Dominant

$$\mathcal{M} \sim \frac{1}{s} \frac{1}{t^2}$$

→ 't Hooft limit, AdS/CFT

Blankenbecler, Gunion, sjb

MIT Bag Model  
predicts dominance of quark  
interchange: deTar



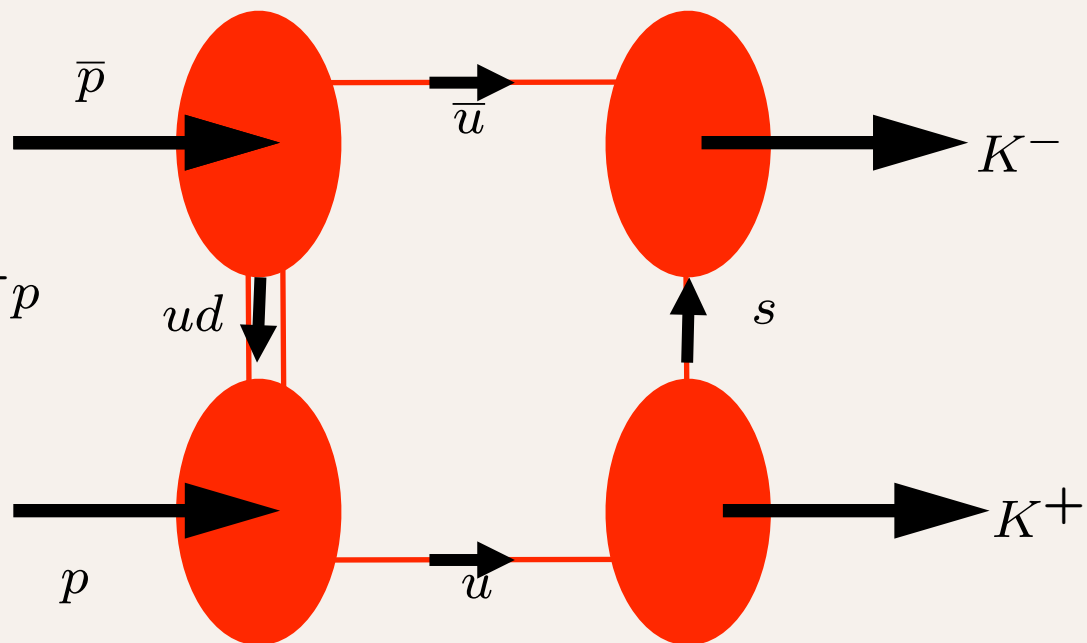


# Key QCD Experiment at GSI

$$\bar{p}p \rightarrow K^+ K^-$$

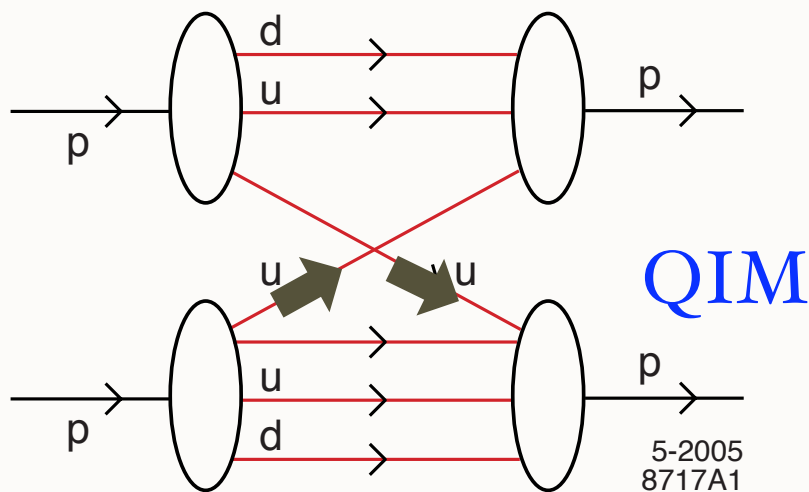
$s \leftrightarrow t \quad t \leftrightarrow u$  crossing of  $K^+ p \rightarrow K^+ p$

$$M(\bar{p}p \rightarrow K^+ K^-) \propto \frac{1}{ts^2}$$



$$\frac{d\sigma}{dt} \propto \frac{1}{s^6 t^2}$$

at large  $t, u$



$$\frac{d\sigma}{dt}(pp \rightarrow pp) = C \frac{F_p^2(t) F_p^2(u)}{s^2}$$

$$\frac{d\sigma}{dt} = \frac{1}{s^{10}} f(\theta_{\text{c.m.}}), \quad f(\theta_{\text{c.m.}}) \sim \left( \frac{1}{1 - \cos^2 \theta} \right)^4$$

The biggest failure of the interchange mechanism is in the spin correlation. For all angles we predict from Table I

$$A_{nn} = \frac{1}{3} \frac{1 - \left(\frac{3}{31}\right)^2 \chi^2}{1 + \frac{1}{3} \left(\frac{3}{31}\right)^2 \chi^2}, \quad (3.11)$$

where

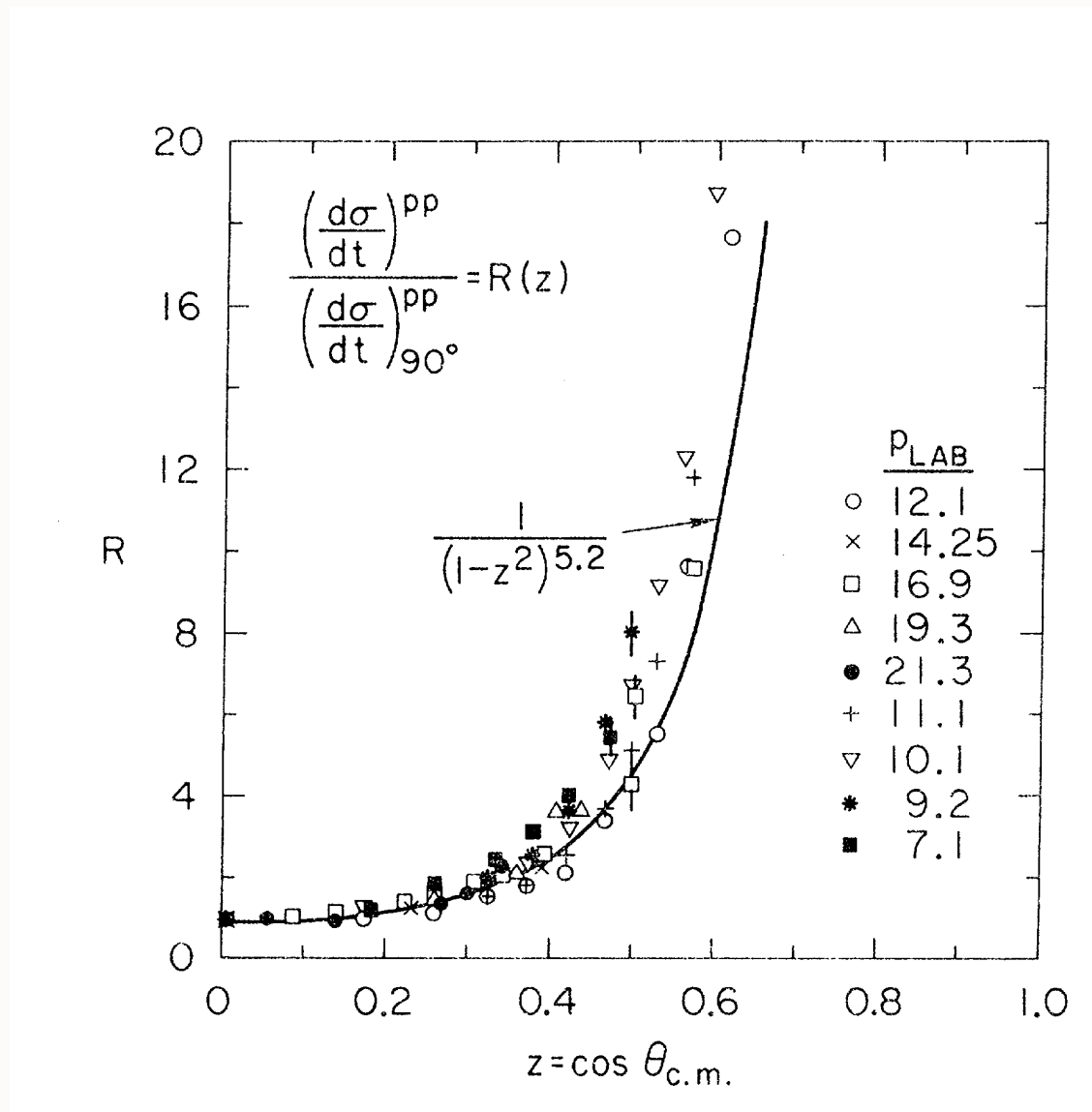
$$\chi = \frac{f(\theta) - f(\pi - \theta)}{f(\theta) + f(\pi - \theta)}$$

Thus  $A_{nn}$  is predicted to be within 2% of  $\frac{1}{3}$  even when  $\chi = 1$  [ $\chi = 0$  for the form in Eq. (3.6)]. The data clearly indicate that  $A_{nn}$  is not a constant near  $\frac{1}{3}$ .

Our expectation, then, is that there is an additional amplitude which strongly interferes with the quark-interchange contributions at Argonne energies; most plausibly, the quark-interchange contribution is dominant at asymptotic  $t$  and  $u$ , and the interfering amplitude is most important at low  $t$  and  $u$ . As we shall discuss below, the behavior of  $A_{ll}$  and  $A_{ss}$  in the interference region can play an important role in sorting out the possible sub-asymptotic contributions.

These results for the quark-interchange model have also been obtained by Farrar, Gottlieb, Sivers, and Thomas,<sup>12</sup> who also consider the possibility that nonperturbative effects (quark-quark scattering via instantons) can explain the data.

# Test of Quark Interchange Mechanism in QCD



## Comparison of Exclusive Reactions at Large $t$

B. R. Baller,<sup>(a)</sup> G. C. Blazey,<sup>(b)</sup> H. Courant, K. J. Heller, S. Heppelmann,<sup>(c)</sup> M. L. Marshak,  
E. A. Peterson, M. A. Shupe, and D. S. Wahl<sup>(d)</sup>  
*University of Minnesota, Minneapolis, Minnesota 55455*

D. S. Barton, G. Bunce, A. S. Carroll, and Y. I. Makdisi  
*Brookhaven National Laboratory, Upton, New York 11973*

and

S. Gushue<sup>(e)</sup> and J. J. Russell

*Southeastern Massachusetts University, North Dartmouth, Massachusetts 02747*

(Received 28 October 1987; revised manuscript received 3 February 1988)

Cross sections or upper limits are reported for twelve meson-baryon and two baryon-baryon reactions for an incident momentum of 9.9 GeV/c, near 90° c.m.:  $\pi^\pm p \rightarrow p\pi^\pm, p\rho^\pm, \pi^+\Delta^\pm, K^+\Sigma^\pm, (\Lambda^0/\Sigma^0)K^0, K^\pm p \rightarrow pK^\pm; p^\pm p \rightarrow pp^\pm$ . By studying the flavor dependence of the different reactions, we have been able to isolate the quark-interchange mechanism as dominant over gluon exchange and quark-antiquark annihilation.

$$\pi^\pm p \rightarrow p\pi^\pm,$$

$$K^\pm p \rightarrow pK^\pm,$$

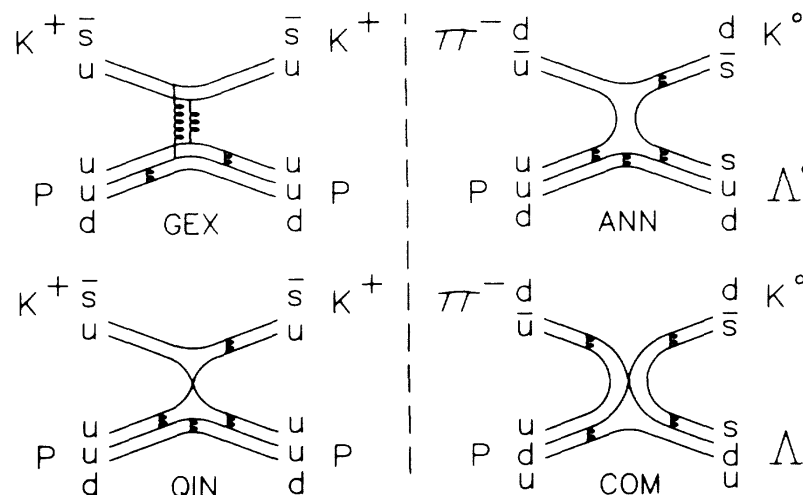
$$\pi^\pm p \rightarrow p\rho^\pm,$$

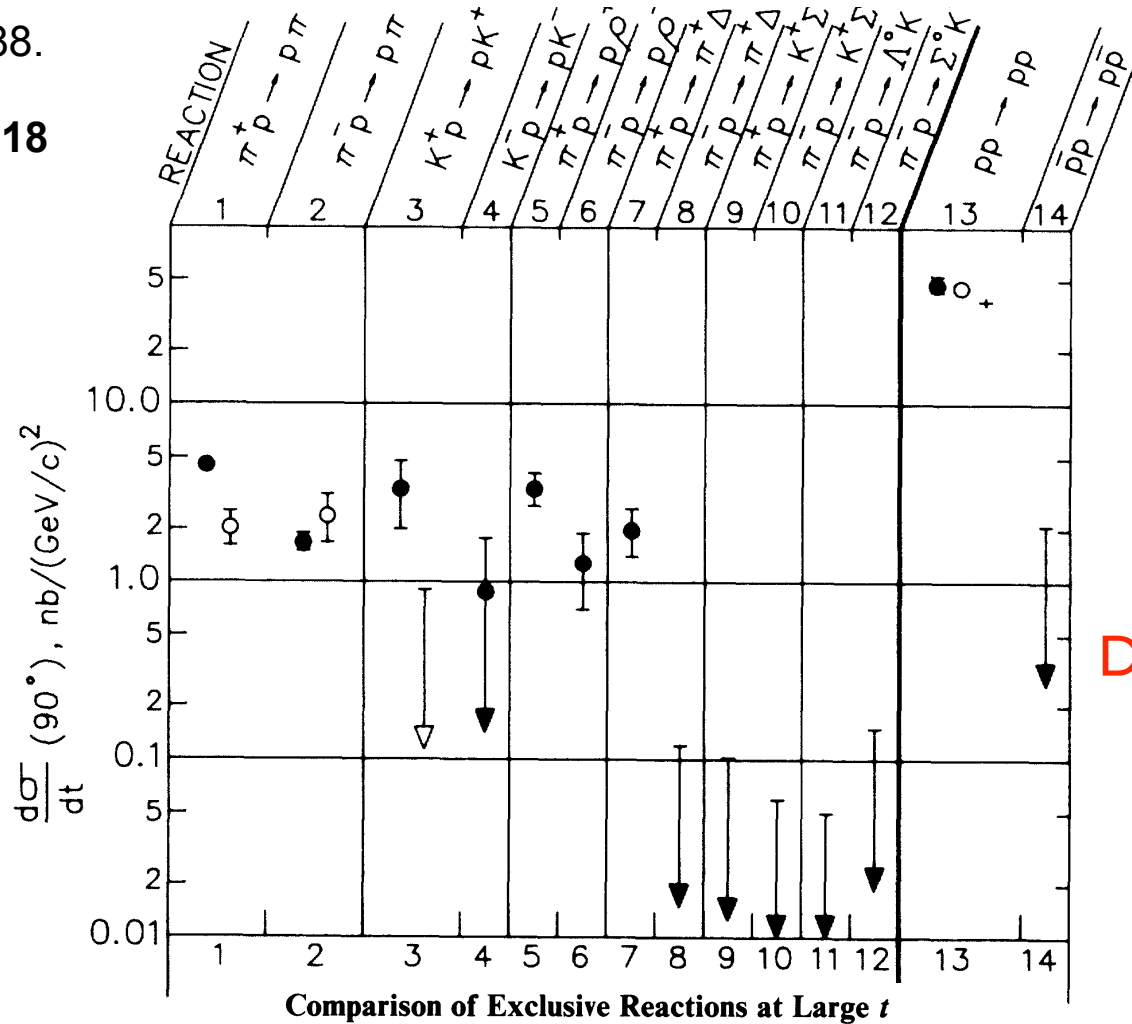
$$\pi^\pm p \rightarrow \pi^+\Delta^\pm,$$

$$\pi^\pm p \rightarrow K^+\Sigma^\pm,$$

$$\pi^- p \rightarrow \Lambda^0 K^0, \Sigma^0 K^0,$$

$$p^\pm p \rightarrow pp^\pm.$$





Quark Interchange:  
 Dominant Dynamics at  
 large  $t, u$

Relative Rates Correct

The cross section and upper limits (90% confidence level) measured by this experiment are indicated by the filled circles and arrowheads. Values from this experiment and from previous measurements represent an average over the angular region of  $-0.05 < \cos\theta_{c.m.} < 0.10$ . The other measurements were obtained from the following references:  $\pi^+ p$  and  $K^+ p$  elastic, Ref. 5;  $\pi^- p \rightarrow p\pi^-$ , Ref. 6;  $pp \rightarrow pp$ , Ref. 7; Allaby, open circle; Akerlof, cross. Values for the cross sections [(Reaction), cross section in nb/(GeV/c)<sup>2</sup>] are as follows: (1),  $4.6 \pm 0.3$ ; (2),  $1.7 \pm 0.2$ ; (3),  $3.4 \pm 1.4$ ; (4),  $0.9 \pm 0.7$ ; (5),  $3.4 \pm 0.7$ ; (6),  $1.3 \pm 0.6$ ; (7),  $2.0 \pm 0.6$ ; (8),  $< 0.12$ ; (9),  $< 0.1$ ; (10),  $< 0.06$ ; (11),  $< 0.05$ ; (12),  $< 0.15$ ; (13),  $48 \pm 5$ ; (14),  $< 2.1$ .

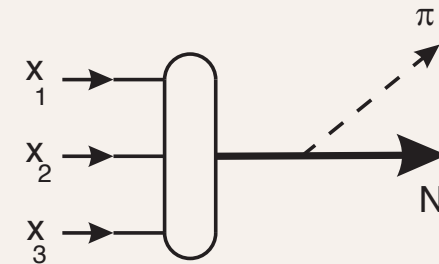
# Key QCD Experiment at GSI

P. V. Pobylitsa, V. Polyakov

and M. Strikman,

“Soft pion theorems for hard near-threshold pion production,”

Phys. Rev. Lett. **87**, 022001 (2001)



Small  $p\pi$  invariant mass; low relative velocity

Soft-pion theorem relates near-threshold pion production to the nucleon distribution amplitude.

$$\frac{d\sigma}{dt}(\bar{p}p \rightarrow (\pi\bar{p})p) = \frac{F(\theta_{cm})}{s^{10}}$$

No extra fall-off

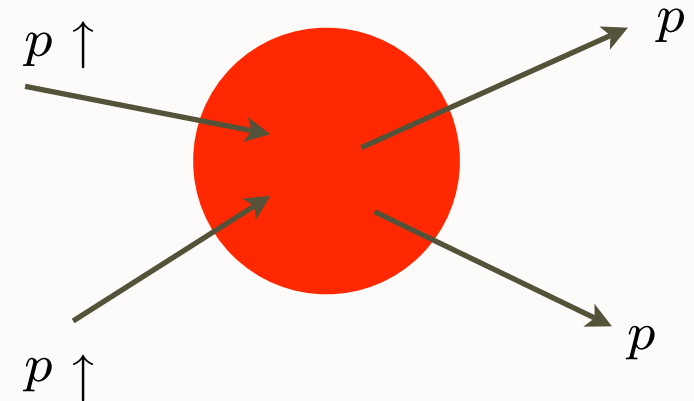
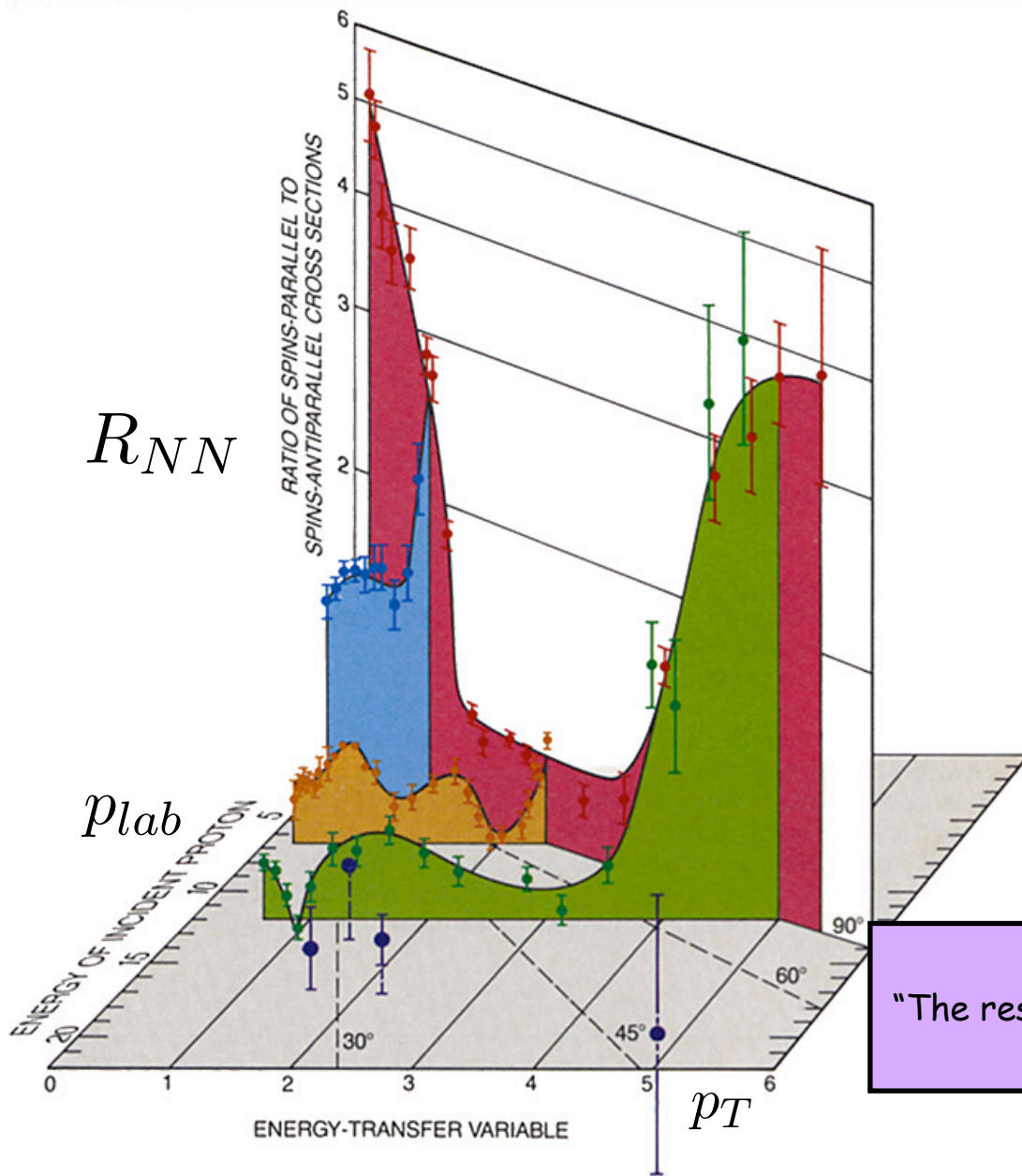
Same scaling as

$$\frac{d\sigma}{dt}(\bar{p}p \rightarrow \bar{p}p) = \frac{F(\theta_{cm})}{s^{10}}$$

# *The remarkable anomalies of proton-proton scattering*

- Double spin correlations
- Single spin correlations
- **Color transparency**

# Spin Correlations in Elastic $p - p$ Scattering



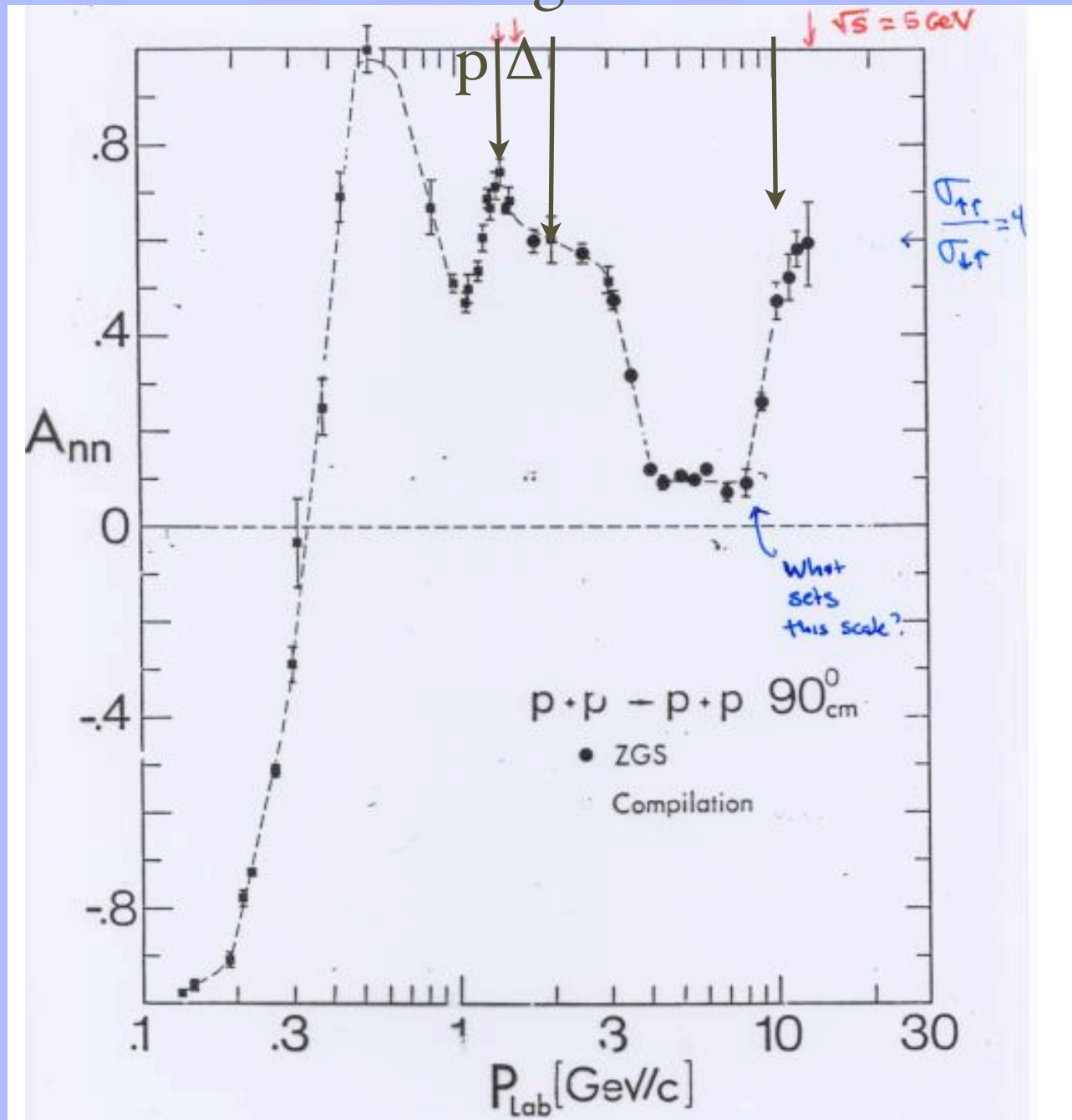
polarization normal to scattering plane

Ratio reaches 4:1 !

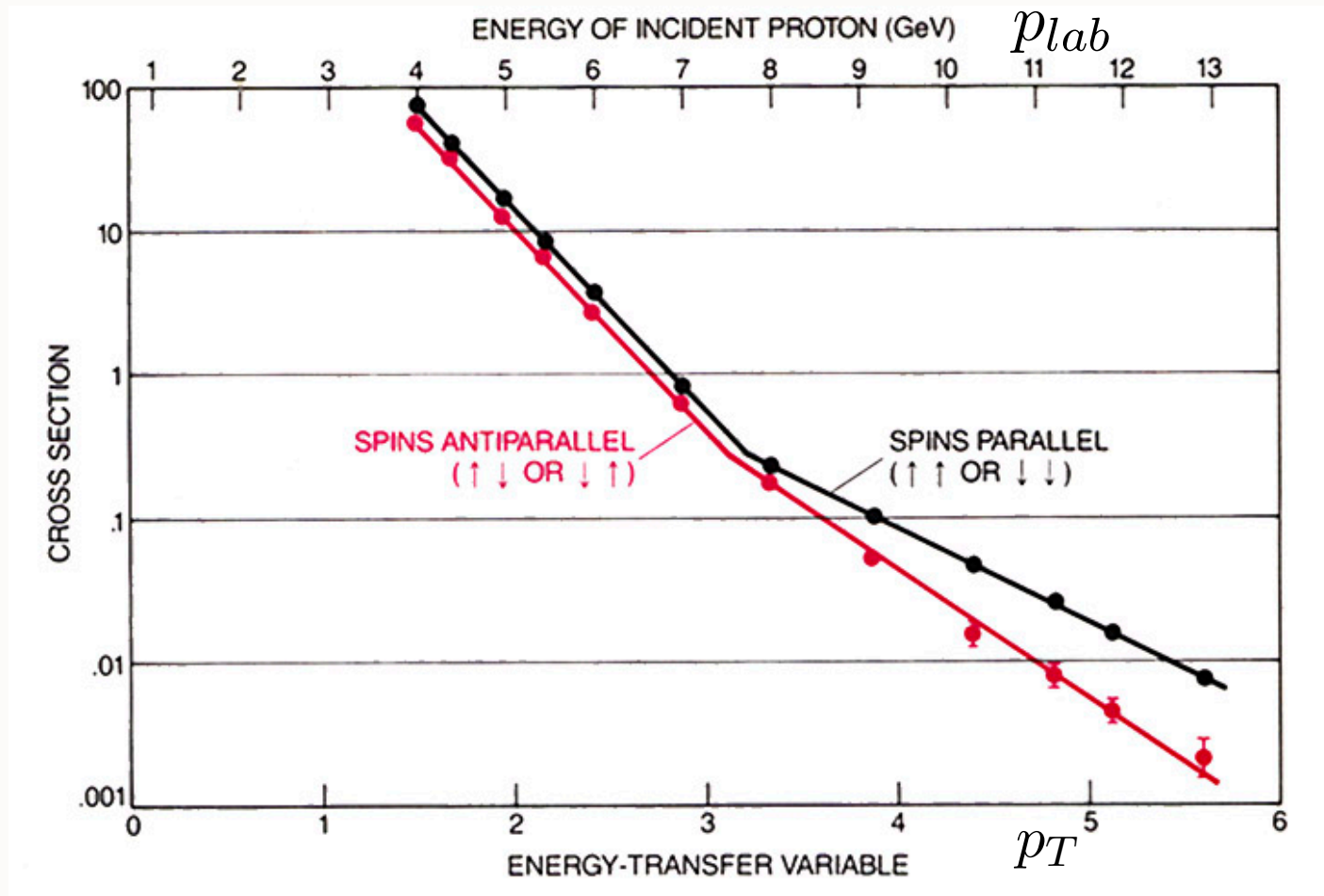
A. Krisch, Sci. Am. 257 (1987)  
 "The results challenge the prevailing theory that describes the proton's structure and forces"



# Strangeness Charm



$$\frac{d\sigma_{\uparrow\uparrow}}{dt}(pp \rightarrow pp) \text{ at } \theta_{CM} = \pi/2$$



Collisions Between Spinning Protons (A. D. Krisch)  
 Scientific American, 255, 42-50 (August, 1987).

## What causes the Krisch Effect?

Largest spin-spin correlation in hadron physics!

An outstanding problem confronting QCD

### Carlson, Lipkin, SJB:

Complete analysis of spin correlations

Interference of QIM and  
Landshoff “Pinch” (triple scattering)  
contributions

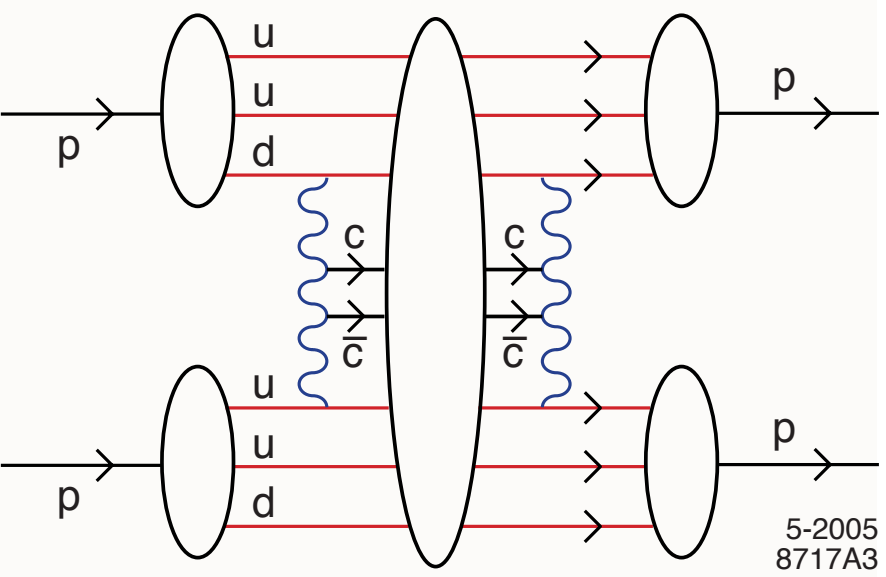
### de Teramond, SJB:

Peaks in  $R_{NN}$  associated with  
 $p\Delta$ , strangeness, charm thresholds

Predict significant strangeness production  
 $\sigma(pp \rightarrow sX) \sim 1 \text{ mb}$  just above threshold

Predict significant charm production  
 $\sigma(pp \rightarrow cX) \sim 1 \text{ } \mu\text{b}$  just above threshold

Spin, Coherence at heavy quark thresholds



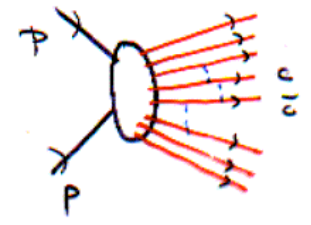
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QCD

Schwinger - Sommerfeld  
Enhancement

Hebecker, Kuhn, sjb

$P\bar{P} \rightarrow Q\bar{Q} X$



Strong distortion at threshold  $\text{Re} \epsilon \sim 0$

$\sqrt{s}_{\text{th}} = 3 + 2 \approx 5 \text{ GeV}$

$PP \rightarrow c\bar{c} X$

8 quarks in s-wave odd parity!

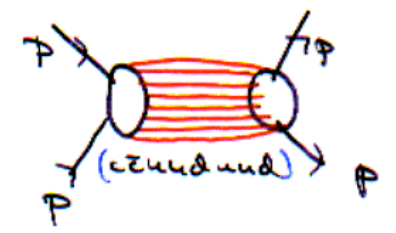
$J = L = S = 1$  for  $PP$

$B = 2$

resonance near threshold?

sjb + determined

$\frac{d\sigma}{dt} (PP \rightarrow PP)$   
 $\sqrt{s} \sim 5 \text{ GeV}$



$A_{NN} = 1$  for  $J=L=S=1$   $PP \rightarrow PP$  only

Expect increase of  $A_{NN}$  at  $\sqrt{s} = 3, 5, 12 \text{ GeV}$   
 $\theta_{cm} = 90^\circ$

S. J. Brodsky and G. F. de Teramond, "Spin Correlations, QCD Color Transparency And Heavy Quark Thresholds In Proton Proton Scattering," Phys. Rev. Lett. **60**, 1924 (1988).

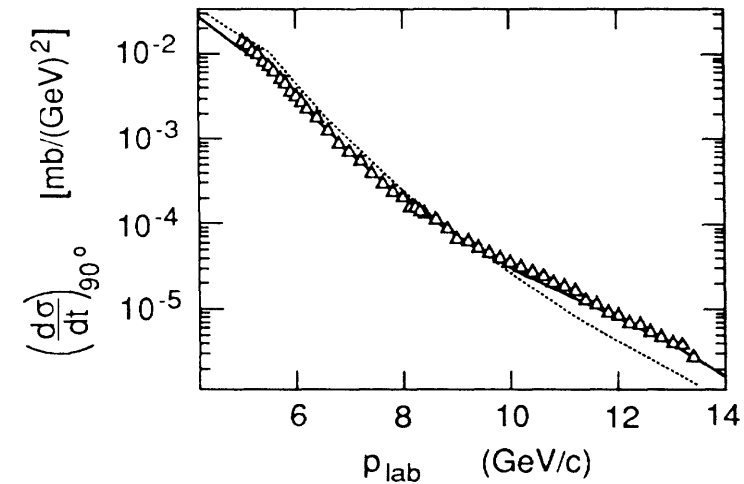
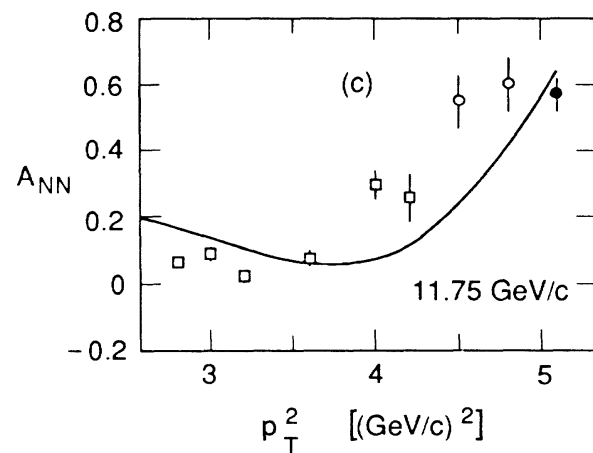
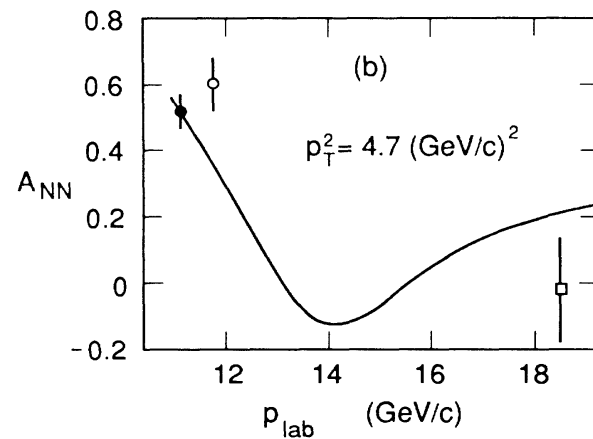
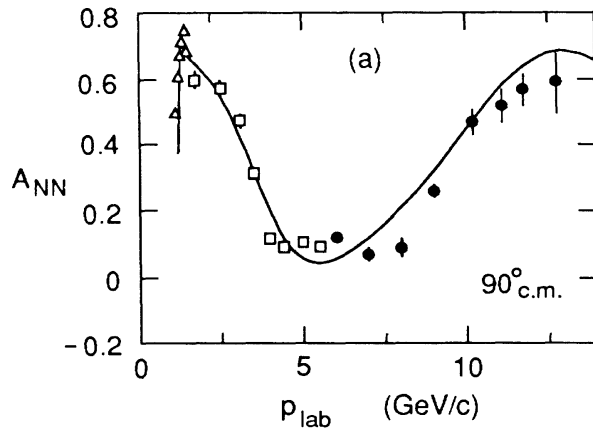
## Quark Interchange + 8-Quark Resonance

$|uud\bar{u}udc\bar{c}\rangle$  Strange and Charm Octoquark!

$M = 3 \text{ GeV}, M = 5 \text{ GeV}.$

$J = L = S = 1, B = 2$

$$A_{NN} = \frac{d\sigma(\uparrow\uparrow) - d\sigma(\uparrow\downarrow)}{d\sigma(\uparrow\uparrow) + d\sigma(\uparrow\downarrow)}$$



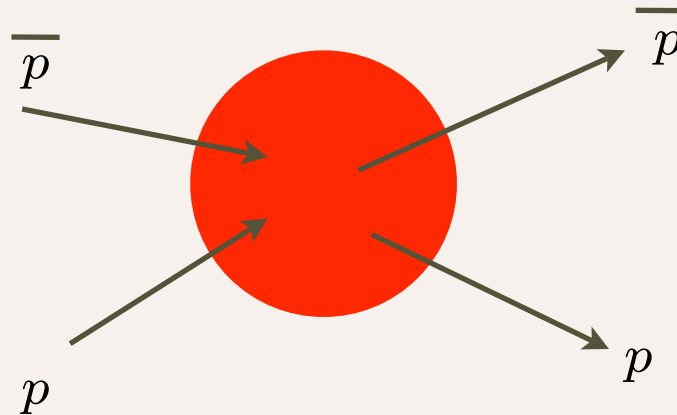
- New QCD physics in proton-proton elastic scattering at the charm threshold
- Anomalously large charm production at threshold!!?
- Octoquark resonances?
- Color Transparency disappears at charm threshold
- Key physics at GSI: second charm threshold

$$\bar{p}p \rightarrow \bar{p}p J/\psi$$

$$\bar{p}p \rightarrow \bar{p}\Lambda_c D$$

# Key QCD Experiment at GSI

$A_{NN}$  for  $\bar{p}p \rightarrow \bar{p}p$



# Key QCD Experiment at GSI

Total open charm cross section at threshold

$$\sigma(\bar{p}p \rightarrow cX) \simeq 1\mu b$$

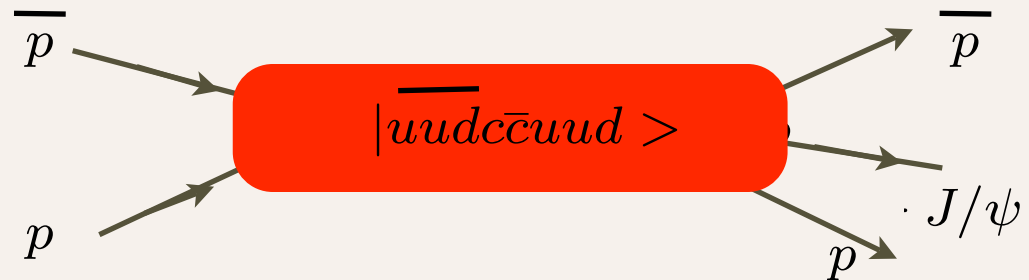
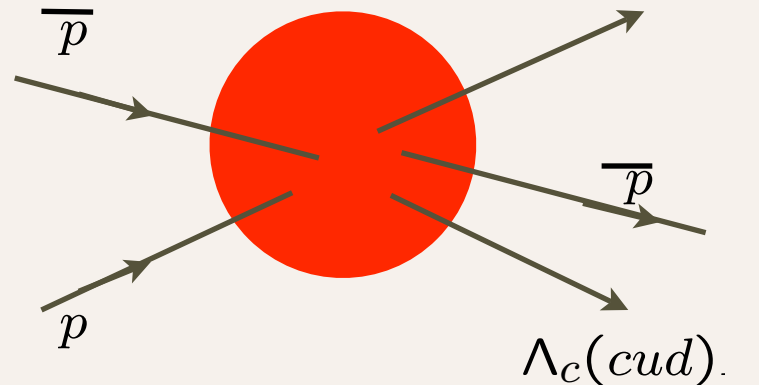
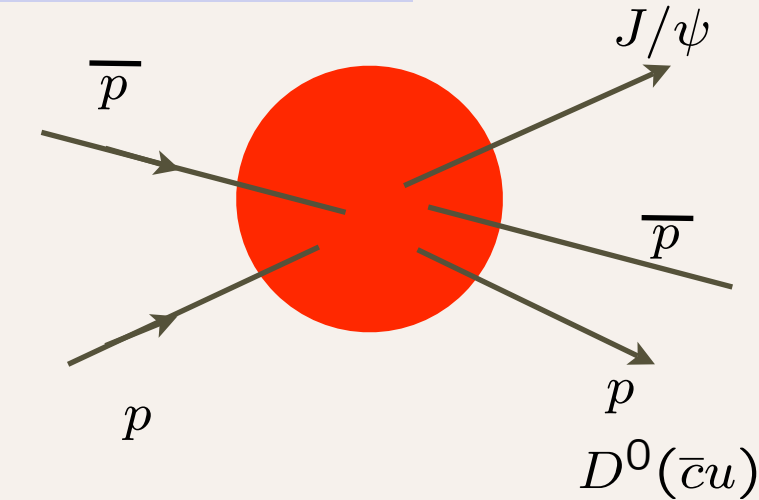
needed to explain Krisch  $A_{NN}$

$$\bar{p}p \rightarrow \bar{p} + J/\psi + p$$

$$\bar{p}p \rightarrow \bar{p} + \eta_c + p$$

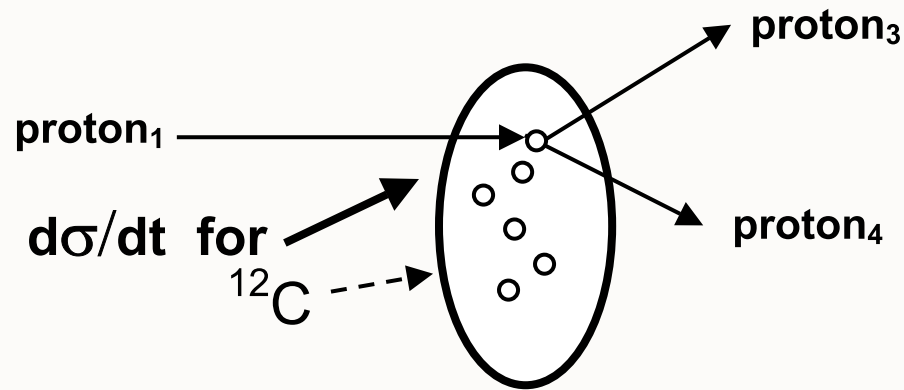
$$\bar{p}p \rightarrow \bar{\Lambda}_c(\bar{c}\bar{u}d)D^0(\bar{c}u)p$$

Octoquark:  $|\bar{u}udc\bar{c}uud\rangle$

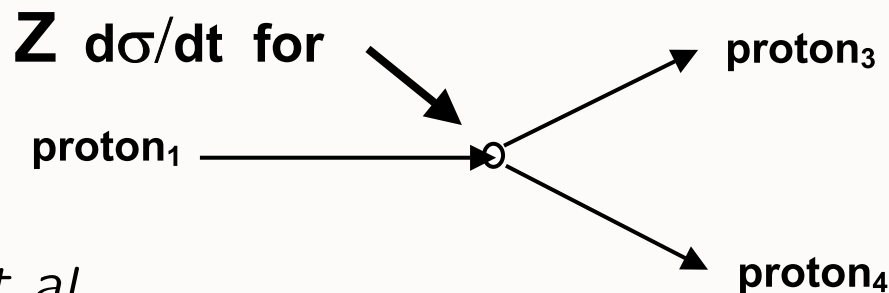




# Color Transparency Ratio



$$T_{pp} =$$

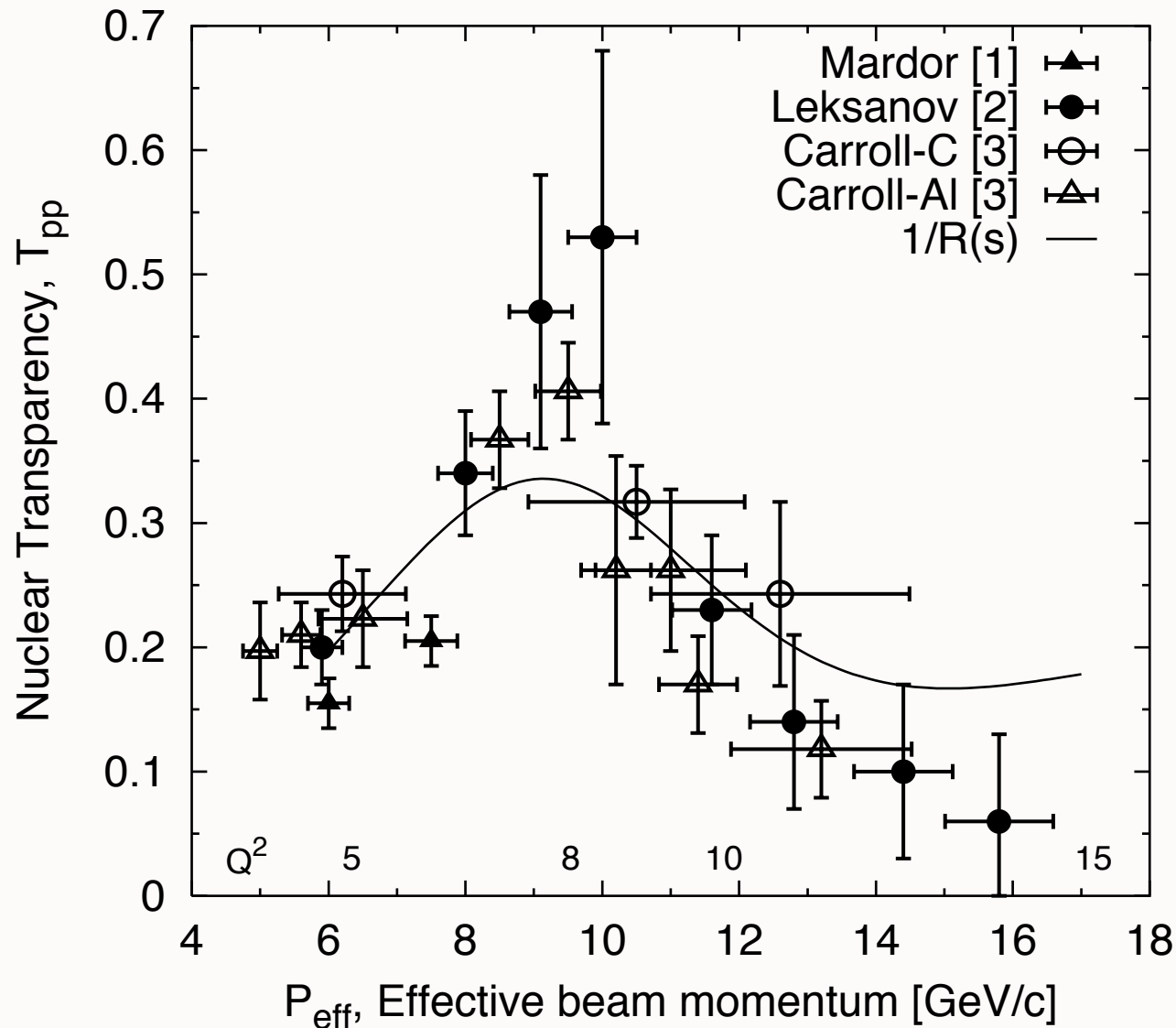


J. L. S. Aclander *et al.*,

“Nuclear transparency in  $\theta_{CM} = 90^\circ$   
quasielastic  $A(p, 2p)$  reactions,”

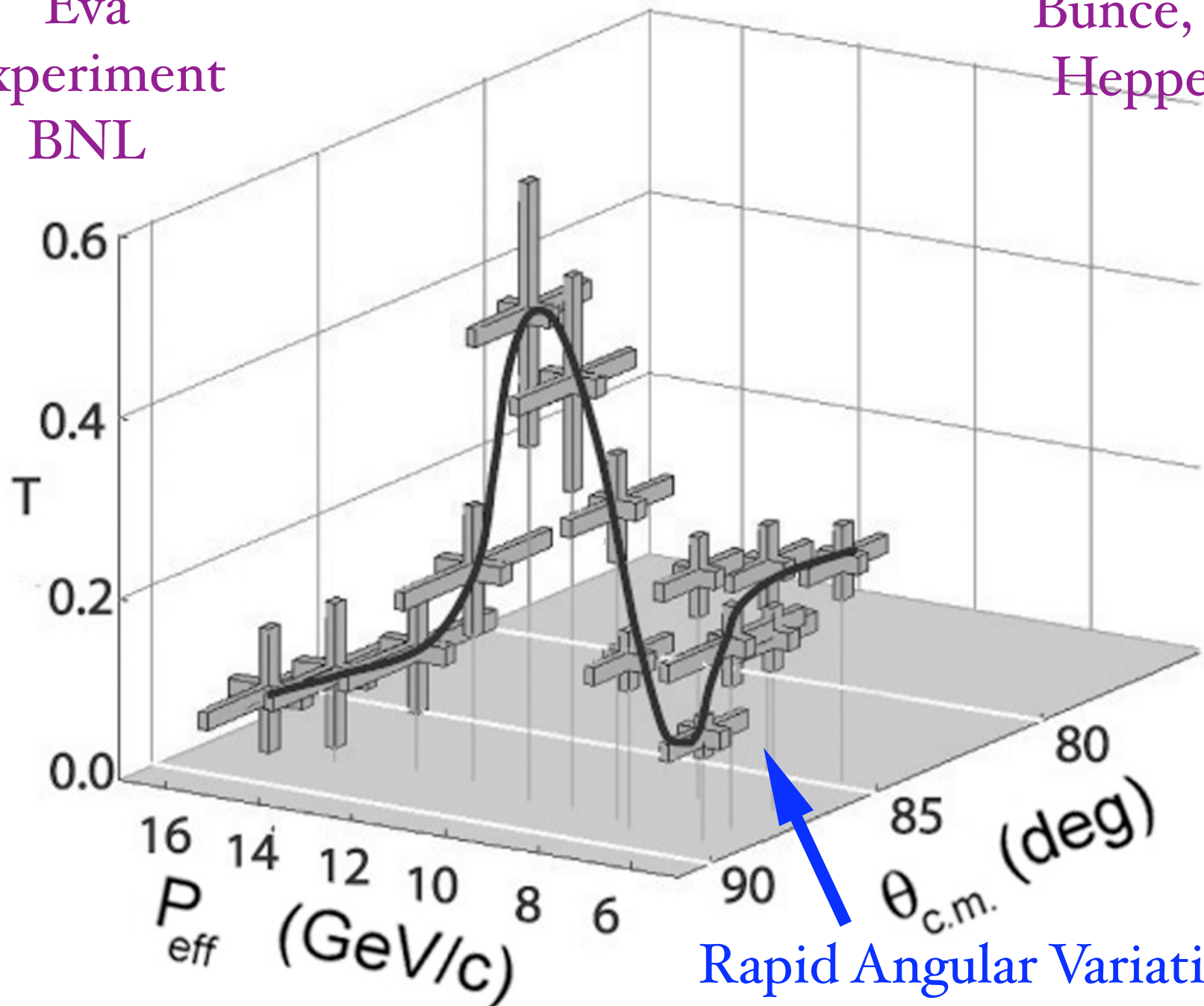
Phys. Rev. C **70**, 015208 (2004), [arXiv:nucl-  
ex/0405025].

# Color Transparency fails when $A_m$ is large



Eva  
Experiment  
BNL

Bunce, Carroll,  
Heppelman...



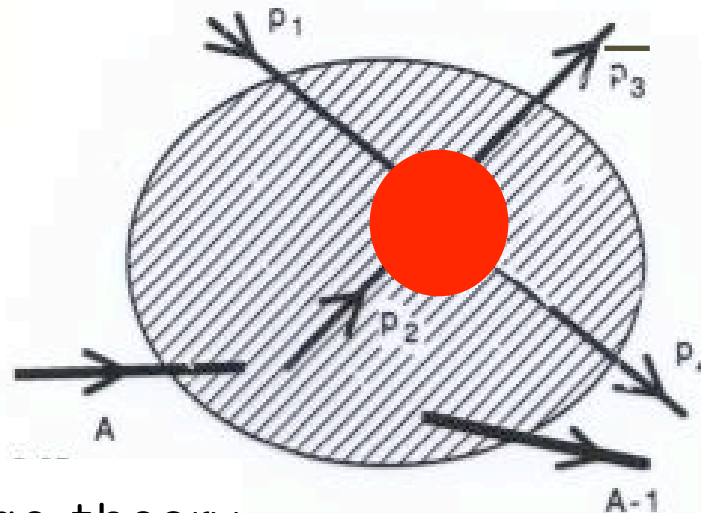
Rapid Angular Variation!

# Key QCD Experiment at GSI

## Test Color Transparency

$$\frac{d\sigma}{dt}(\bar{p}A \rightarrow \bar{p}p(A-1)) \rightarrow Z \times \frac{d\sigma}{dt}(\bar{p}p \rightarrow \bar{p}p)$$

No absorption of small color dipole  
at high  $p_T$



Key test of local gauge theory

Traditional Glauber Theory:  $\sigma_A \sim Z^{1/3}\sigma_p$

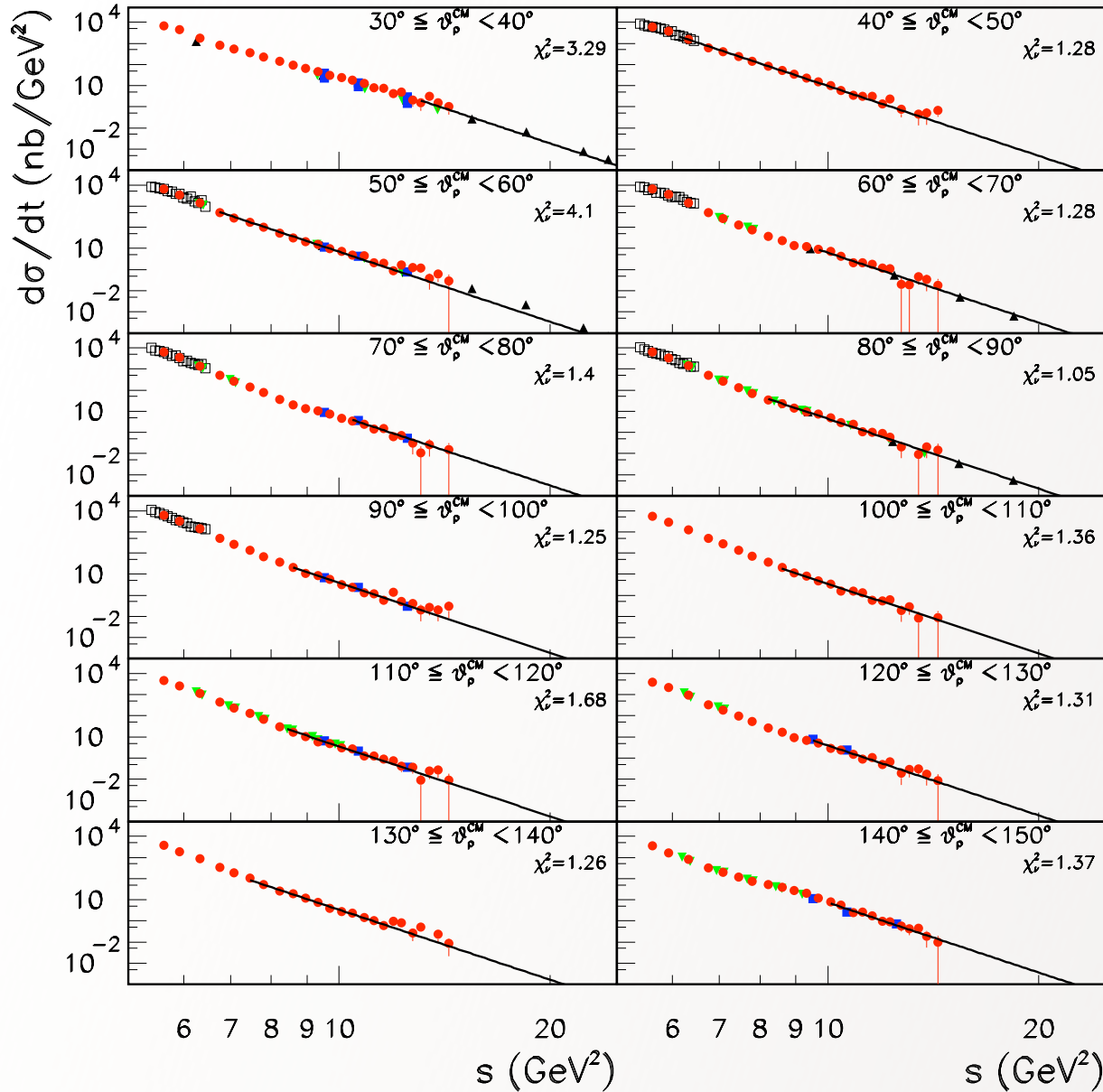
A.H. Mueller, SJB

Trento  
July 5, 2006

AdS/CFT, QCD, & GSI

Stan Brodsky, SLAC

# Deuteron Photodisintegration & Dimensional Counting Rules



PQCD and AdS/CFT:

$$s^{n_{tot}-2} \frac{d\sigma}{dt} (A + B \rightarrow C + D) = F_{A+B \rightarrow C+D}(\theta_{CM})$$

$$s^{11} \frac{d\sigma}{dt} (\gamma d \rightarrow np) = F(\theta_{CM})$$

$$n_{tot} - 2 = (1 + 6 + 3 + 3) - 2 = 11$$

- Remarkable Test of Quark Counting Rules
- Deuteron Photo-Disintegration  $\gamma d \rightarrow np$

- $$\frac{d\sigma}{dt} = \frac{F(t/s)}{s^{n_{tot}-2}}$$

- $$n_{tot} = 1 + 6 + 3 + 3 = 13$$

Scaling characteristic of  
scale-invariant theory at short distances

Conformal symmetry

**Hidden color:** 
$$\frac{d\sigma}{dt}(\gamma d \rightarrow \Delta^{++}\Delta^{-}) \simeq \frac{d\sigma}{dt}(\gamma d \rightarrow pn)$$
  
at high  $p_T$

# QCD Prediction for Deuteron Form Factor

$$F_d(Q^2) = \left[ \frac{\alpha_s(Q^2)}{Q^2} \right]^5 \sum_{m,n} d_{mn} \left( \ln \frac{Q^2}{\Lambda^2} \right)^{-\gamma_n^d - \gamma_m^d} \left[ 1 + \mathcal{O} \left( \alpha_s(Q^2), \frac{m}{Q} \right) \right]$$

Define “Reduced” Form Factor

$$f_d(Q^2) \equiv \frac{F_d(Q^2)}{F_N^2(Q^2/4)} .$$

Same large momentum transfer behavior as pion form factor

$$f_d(Q^2) \sim \frac{\alpha_s(Q^2)}{Q^2} \left( \ln \frac{Q^2}{\Lambda^2} \right)^{-(2/5) C_F/\beta}$$

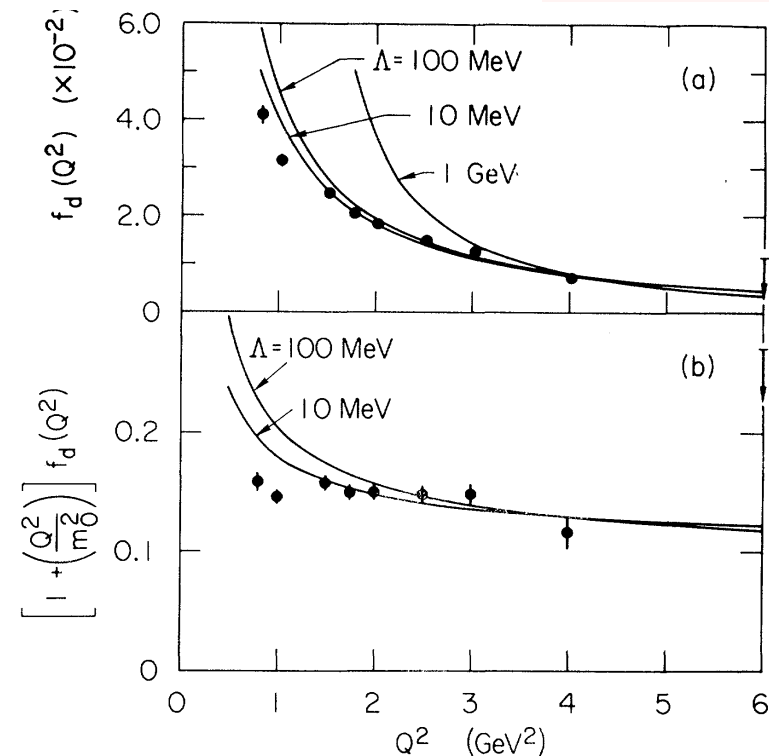
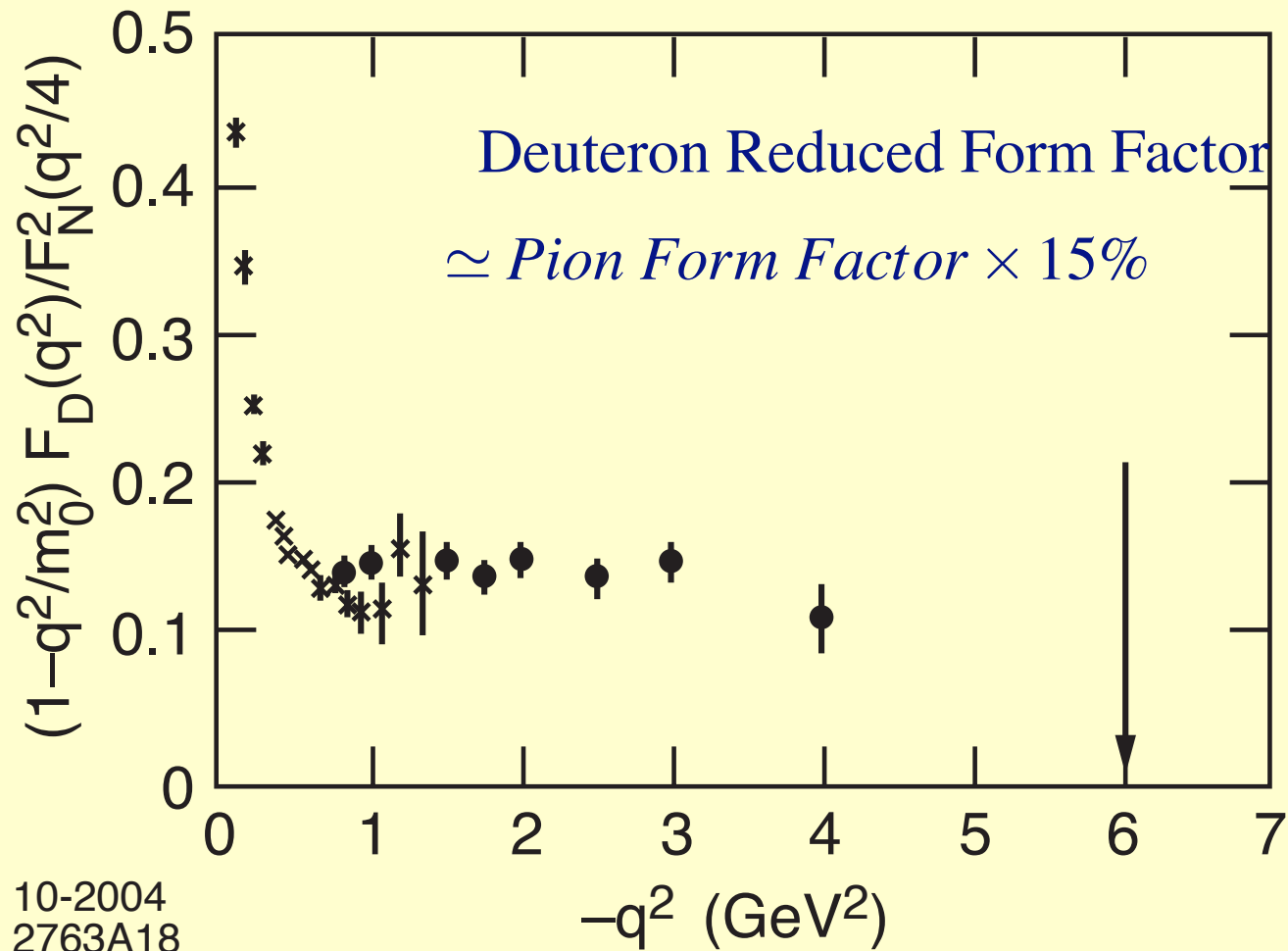


FIG. 2. (a) Comparison of the asymptotic QCD prediction  $f_d(Q^2) \propto (1/Q^2) [\ln(Q^2/\Lambda^2)]^{-1-(2/5)C_F/\beta}$  with finite data of Ref. 10 for the reduced deuteron form factor where  $F_N(Q^2) = [1 + Q^2/(0.71 \text{ GeV}^2)]^{-2}$ . The normalization is fixed at the  $Q^2 = 4 \text{ GeV}^2$  data point. (b) Comparison of the prediction  $[1 + (Q^2/m_0^2)] f_d(Q^2) \propto [\ln(Q^2/\Lambda^2)]^{-1-(2/5)C_F/\beta}$  with the above data. The value  $m_0^2 = 0.28 \text{ GeV}^2$  is used (Ref. 8).



- 15% Hidden Color in the Deuteron



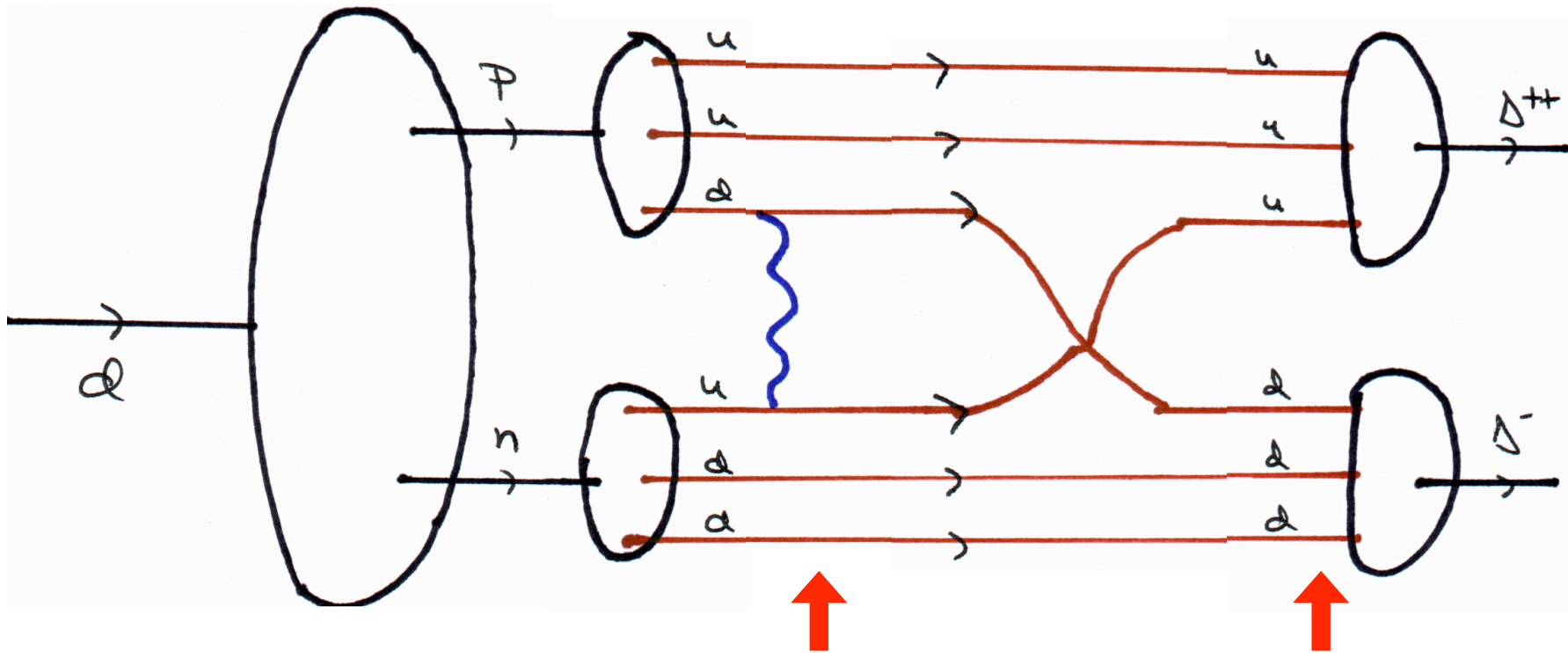
# Hidden Color in QCD

Lepage, Ji, sjb

- Deuteron six quark wavefunction:
- 5 color-singlet combinations of 6 color-triplets -- one state is  $|\ln p\rangle$
- Components evolve towards equality at short distances
- Hidden color states dominate deuteron form factor and photodisintegration at high momentum transfer
- Predict  $\frac{d\sigma}{dt}(\gamma d \rightarrow \Delta^{++}\Delta^{-}) \simeq \frac{d\sigma}{dt}(\gamma d \rightarrow pn)$  at high  $Q^2$

Ratio = 2/5 for asymptotic wf

# Structure of Deuteron in QCD



Hidden Color  
Fock State

Delta-Delta  
Fock State

The evolution equation for six-quark systems in which the constituents have the light-cone longitudinal momentum fractions  $x_i$  ( $i=1,2,\dots,6$ ) can be obtained from a generalization of the proton (three-quark) case.<sup>2</sup> A nontrivial extension is the calculation of the color factor,  $C_d$ , of six-quark systems<sup>5</sup> (see below). Since in leading order only pairwise interactions, with transverse momentum  $Q$ , occur between quarks, the evolution equation for the six-quark system becomes  $\{[dy]=\delta(1-\sum_{i=1}^6 y_i)\prod_{i=1}^6 dy_i$ ,  $C_F=(n_c^2-1)/2n_c=4/3$ ,  $\beta=11-\frac{2}{3}n_f$ , and  $n_f$  is the effective number of flavors}

$$\prod_{k=1}^6 x_k \left[ \frac{\partial}{\partial \xi} + \frac{3C_F}{\beta} \right] \tilde{\Phi}(x_i, Q) = - \frac{C_d}{\beta} \int_0^1 [dy] V(x_i, y_i) \tilde{\Phi}(y_i, Q),$$

$$\xi(Q^2) = \frac{\beta}{4\pi} \int_{Q_0^2}^{Q^2} \frac{dk^2}{k^2} \alpha_s(k^2) \sim \ln \left( \frac{\ln(Q^2/\Lambda^2)}{\ln(Q_0^2/\Lambda^2)} \right).$$

$$V(x_i, y_i) = 2 \prod_{k=1}^6 x_k \sum_{i \neq j}^6 \theta(y_i - x_i) \prod_{l \neq i, j}^6 \delta(x_l - y_l) \frac{y_j}{x_j} \left( \frac{\delta_{h_i \bar{h}_j}}{x_i + x_j} + \frac{\Delta}{y_i - x_i} \right)$$

where  $\delta_{h_i \bar{h}_j} = 1$  (0) when the helicities of the constituents  $\{i, j\}$  are antiparallel (parallel). The infrared singularity at  $x_i = y_i$  is cancelled by the factor  $\Delta \tilde{\Phi}(y_i, Q) = \tilde{\Phi}(y_i, Q) - \tilde{\Phi}(x_i, Q)$  since the deuteron is a color singlet.

## Hidden Color of Deuteron

Deuteron six-quark state has five color - singlet configurations,  
only one of which is n-p.

Asymptotic Solution has Expansion

$$\psi_{[6]\{33\}} = \left(\frac{1}{9}\right)^{1/2} \psi_{NN} + \left(\frac{4}{45}\right)^{1/2} \psi_{\Delta\Delta} + \left(\frac{4}{5}\right)^{1/2} \psi_{CC}$$

Look for strong transition to Delta-Delta

Fit of  $d\sigma/dt$  data for  
the central angles and  
 $P_T \geq 1.1 \text{ GeV}/c$  with

$$A s^{-11}$$

For all but two of the fits

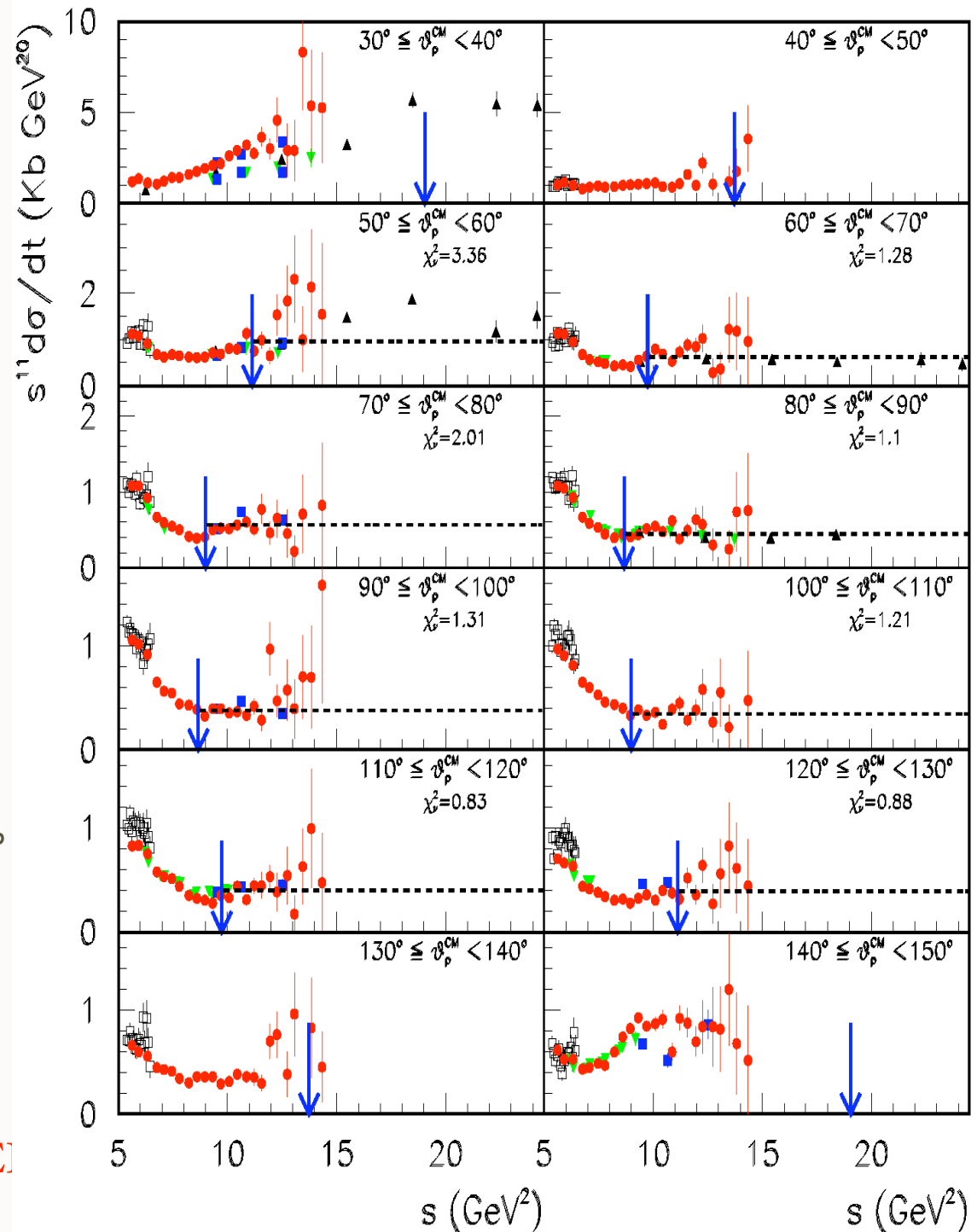
$$\chi^2 \leq 1.34$$

- Better  $\chi^2$  at  $55^\circ$  and  $75^\circ$  if different data sets are renormalized to each other
- No data at  $P_T \geq 1.1 \text{ GeV}/c$  at forward and backward angles
- Clear  $s^{-11}$  behaviour for last 3 points at  $35^\circ$

Data consistent with CCR

Trento  
July 5, 2006

AdS/C



# Quantum Chromodynamic Predictions for the Deuteron Form Factor

$$F_d(Q^2) = \int_0^1 [dx][dy] \varphi_d^\dagger(y, Q) \times T_H^{6q+\gamma^* \rightarrow 6q}(x, y, Q) \varphi_d(x, Q), \quad (1)$$

where the hard-scattering amplitude

$$T_H^{6q+\gamma^* \rightarrow 6q} = [\alpha_s(Q^2)/Q^2]^5 t(x, y) \times [1 + O(\alpha_s(Q^2))] \quad (2)$$

gives the probability amplitude for scattering six quarks collinear with the initial to the final deuteron momentum and

$$\varphi_d(x_i, Q) \propto \int^{k_{\perp i} < Q} [d^2 k_{\perp}] \psi_{qqq qq} (x_i, \vec{k}_{\perp i}) \quad (3)$$

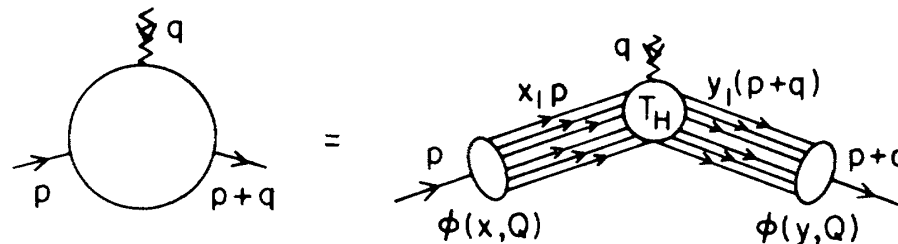


FIG. 1. The general structure of the deuteron form factor at large  $Q^2$ .

Ji, Lepage, sjb

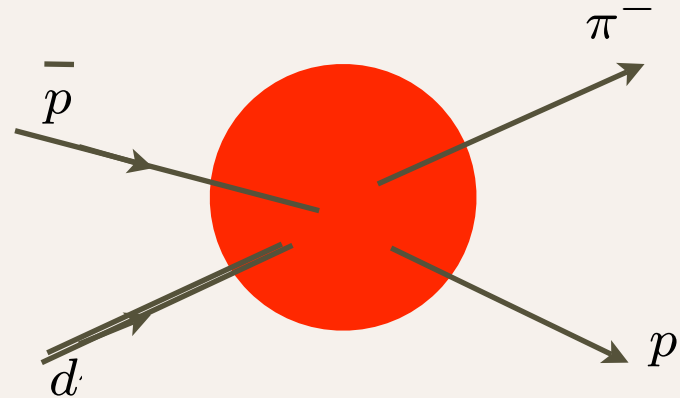
# Key QCD Experiment at GSI

Test QCD scaling in hard exclusive nuclear amplitudes

Manifestations of Hidden Color in Deuteron Wavefunction

$$\bar{p}d \rightarrow \pi^- p$$

$$\bar{p}d \rightarrow \bar{p}d$$



Conformal Scaling, AdS/CFT

$$\frac{d\sigma}{dt}(\bar{p}d \rightarrow \pi^- p) = \frac{F(\theta_{cm})}{s^{12}}$$

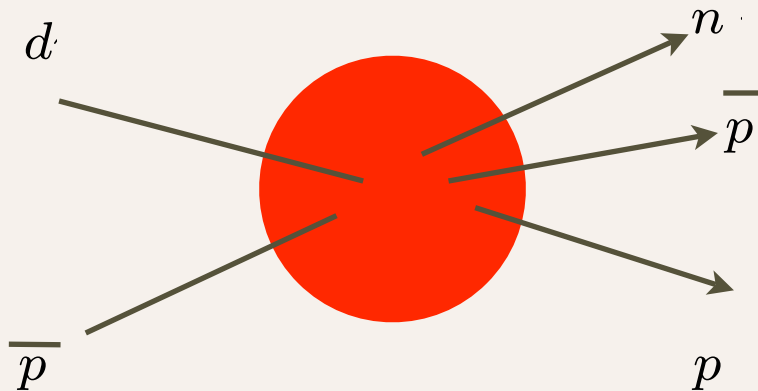
# Key QCD Experiment at GSI

Manifestations of Hidden Color in Deuteron Wavefunction

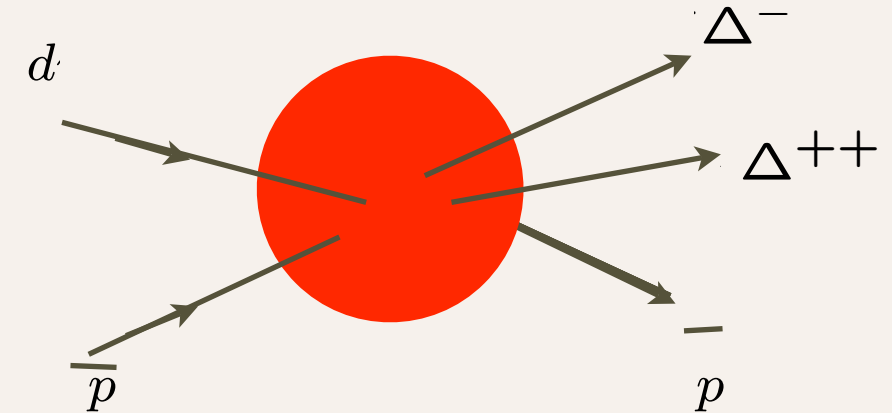
Compare  
at high  $t$ .

$$d\bar{p} \rightarrow \Delta^{++}\Delta^{-} + \bar{p}$$

$$d\bar{p} \rightarrow p n + \bar{p}$$



vs.



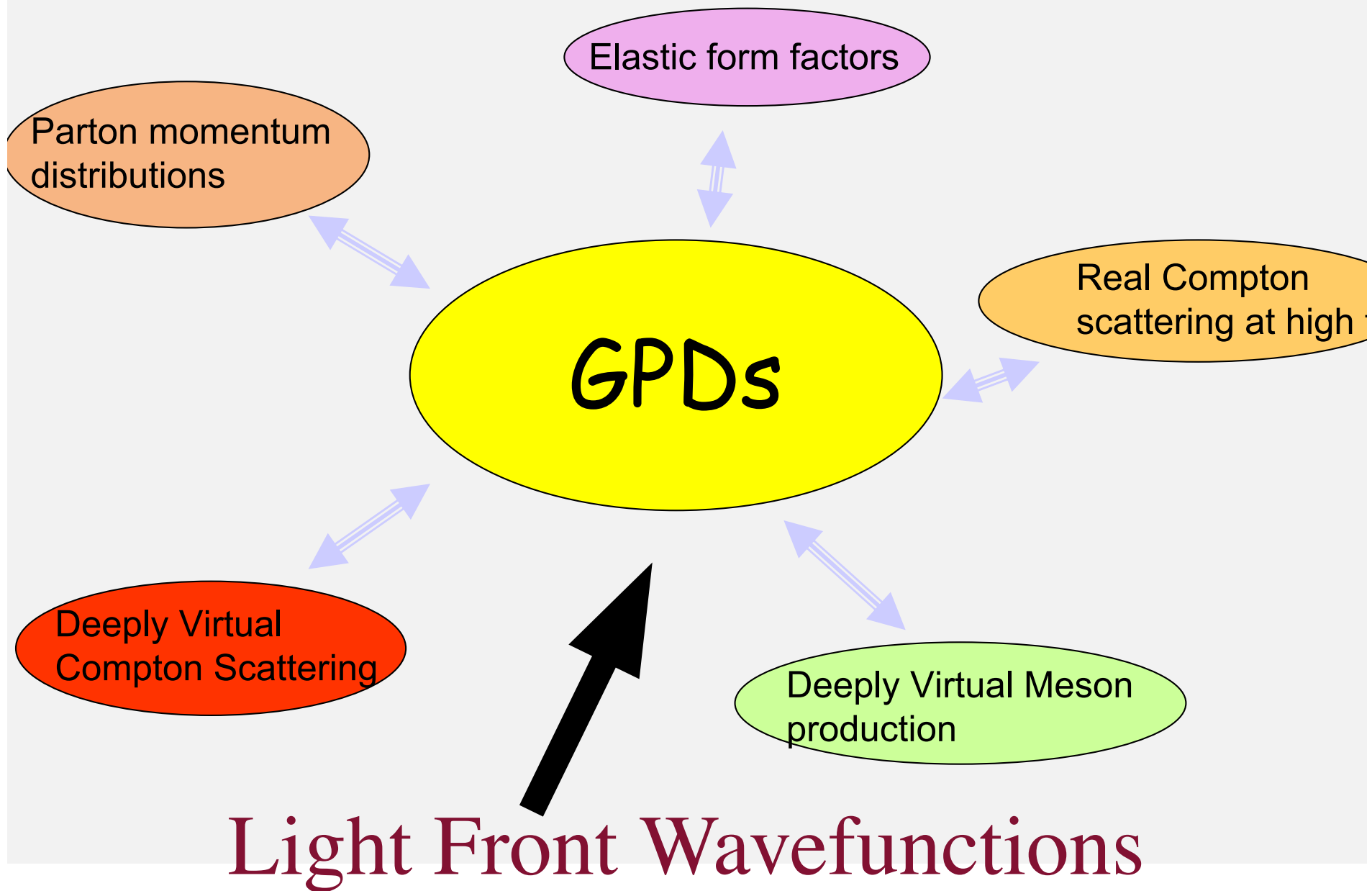
Ratio predicted to approach 2:5



# QCD at The Amplitude Level

- Light-Front Fock Expansions
- LFWFs boost invariant
- Direct connection to form factors, structure functions, distribution amplitudes, GPDs
- Higher Twist Correlations
- Orbital Angular Momentum
- Validated in QED, Bethe-Salpeter
- AdS/CFT Holographic Model

# A Unified Description of Hadron Structure



Light Front Wavefunctions

# LFWFS give a fundamental description of hadron observables

- LFWFS underly form factors, structure functions generalized parton distributions, scattering amplitudes
- Parton number not conserved:  $n=n'$  &  $n=n'+2$  at nonzero skewness
- GPDs are not densities or probability distributions
- Nonperturbative QCD: Lattice, DLCQ, Bethe-Salpeter, AdS/CFT

$$|p, S_z\rangle = \sum_{n=3} \Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i) |n; \vec{k}_{\perp i}, \lambda_i\rangle$$

### The Light Front Fock State Wavefunctions

$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

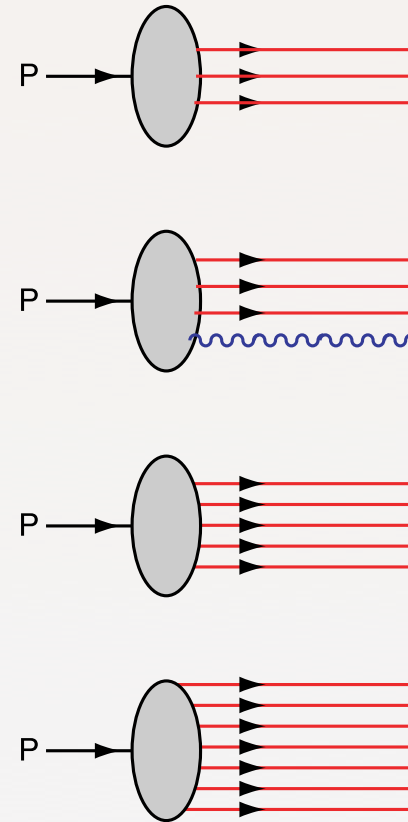
are boost invariant; they are independent of the hadron's energy and momentum  $P^\mu$ .

The light-cone momentum fraction

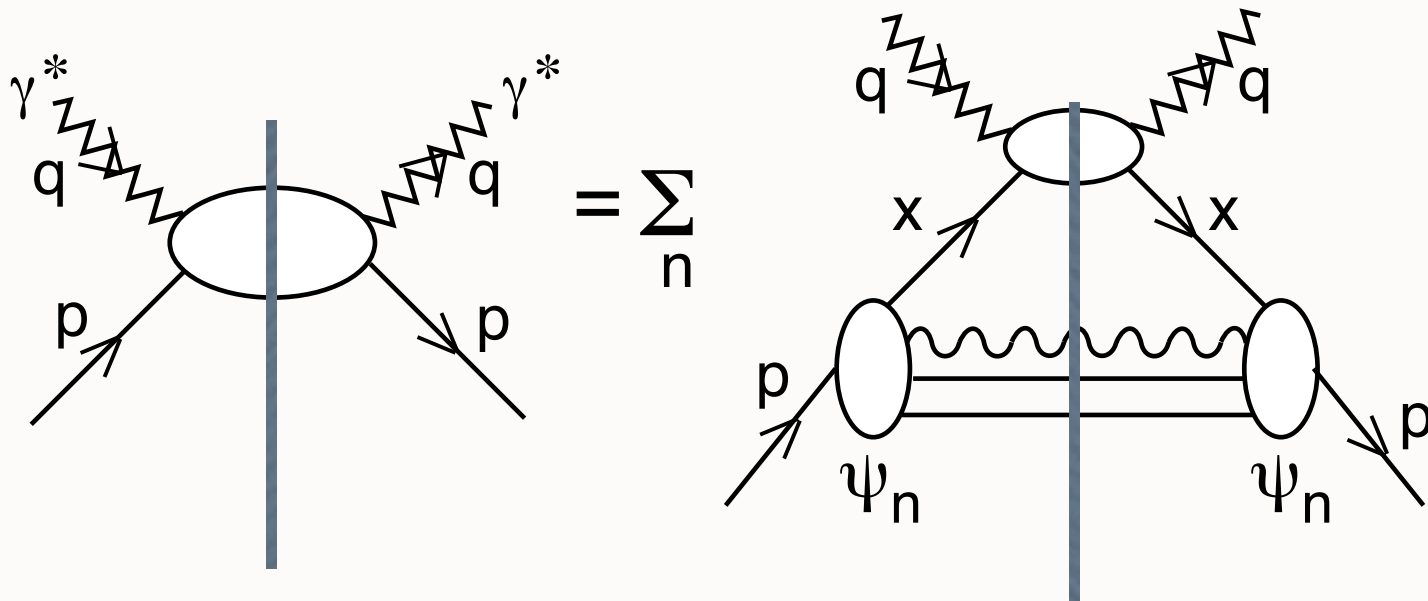
$$x_i = \frac{k_i^+}{p^+} = \frac{k_i^0 + k_i^z}{P^0 + P^z}$$

are boost invariant.

$$\sum_i^n k_i^+ = P^+, \quad \sum_i^n x_i = 1, \quad \sum_i^n \vec{k}_i^\perp = \vec{0}^\perp.$$



# Deep Inelastic Lepton Proton Scattering

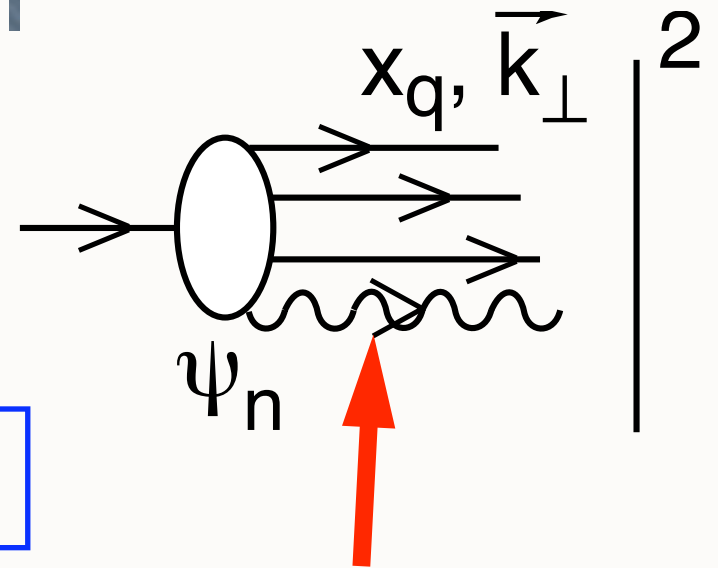


Imaginary Part of  
Forward Virtual Compton Amplitude

$$q(x, Q^2) = \sum_n \int^{k_\perp^2 \leq Q^2_\perp} d^2 k_\perp |\Psi_n(x, k_\perp)|^2$$

$$x = x_q$$

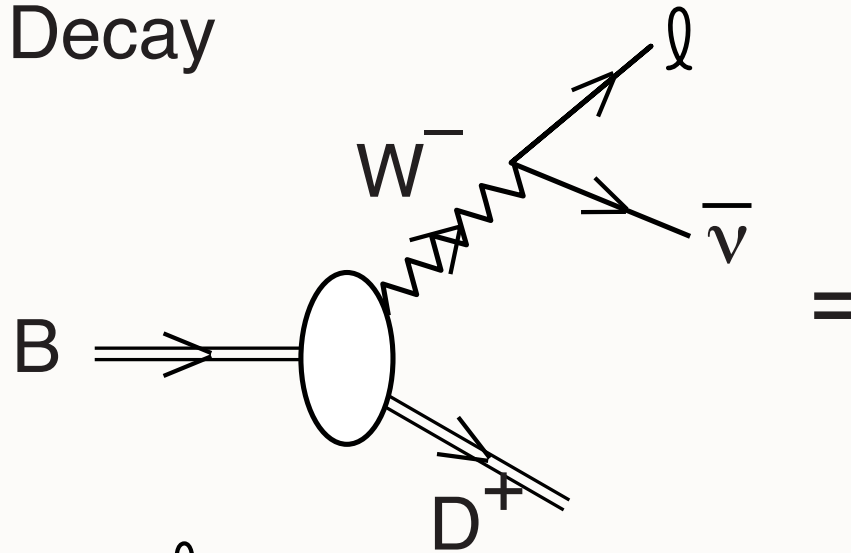
All spin, flavor distributions



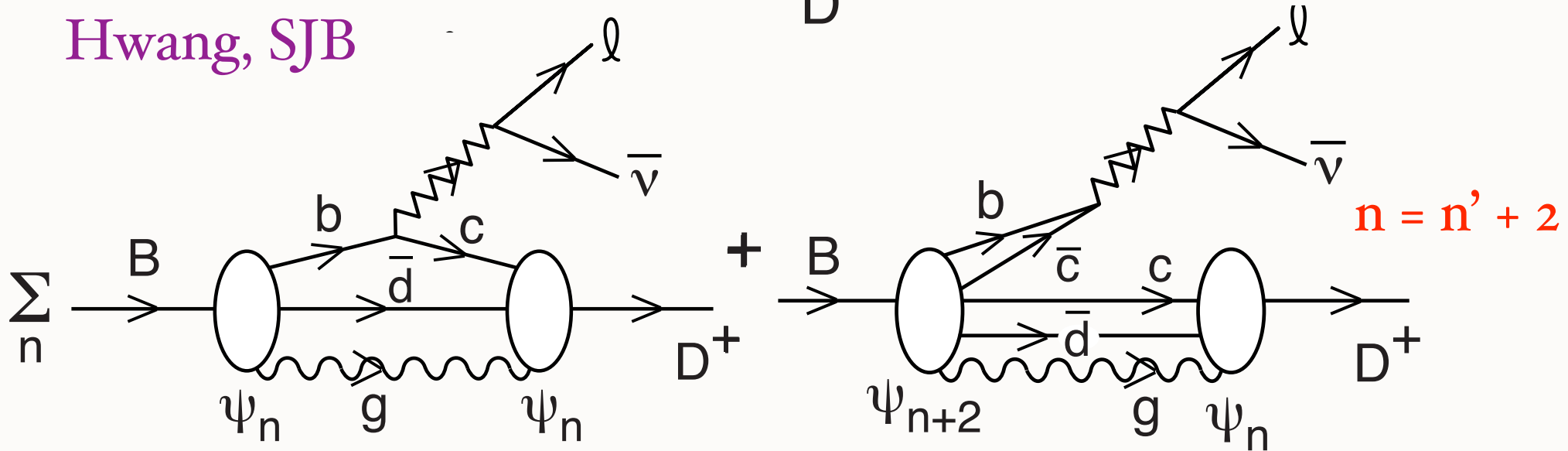
Light-Front Wave Functions  $\psi_n(x_i, \vec{k}_\perp i, \lambda_i)$

# Weak Exclusive Decay

$$\langle D | J^+ (0) | B \rangle$$



Exact Formula  
Hwang, SJB

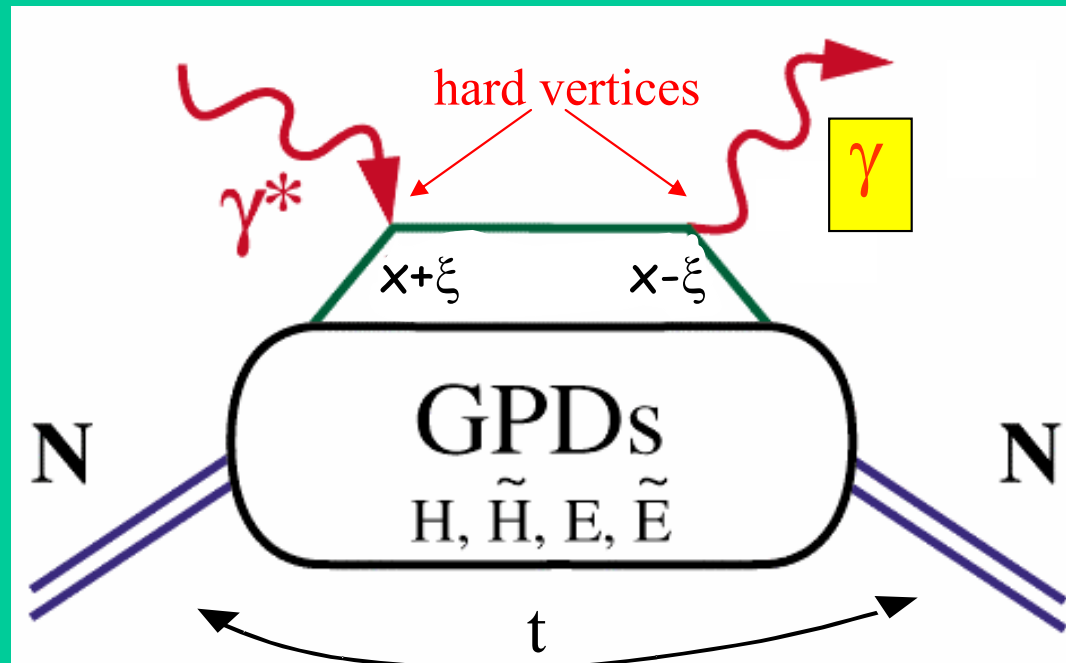


Annihilation amplitude needed for Lorentz Invariance

# GPDs & Deeply Virtual Exclusive Processes

“handbag” mechanism

## Deeply Virtual Compton Scattering (DVCS)



$x$  - longitudinal quark momentum fraction

$2\xi$  - longitudinal momentum transfer

$\sqrt{-t}$  - Fourier conjugate to transverse impact parameter

$H(x, \xi, t), E(x, \xi, t), \dots$

$$\xi = \frac{x_B}{2-x_B}$$

# Deeply Virtual Compton Scattering

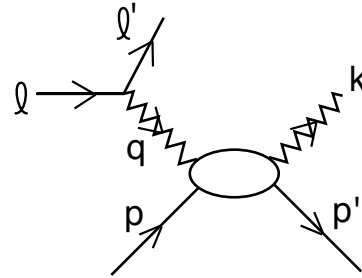
$$\gamma^* p \rightarrow \gamma p', \gamma^* p \rightarrow \pi^+ n',$$

- Remarkable sensitivity to spin, flavor, dynamics
- Measure Real and Imaginary parts from Bethe-Heitler interference; phase determined by Regge theory (Kuti-Weiskopf) Close, Gunion, sjb
- J=0 fixed pole: test QCD contact interaction!
- Sum Rules connecting to form factors, Lz
- Evolution Equations (ERBL), PQCD constraints
- Convolutions of Light-front wavefunctions



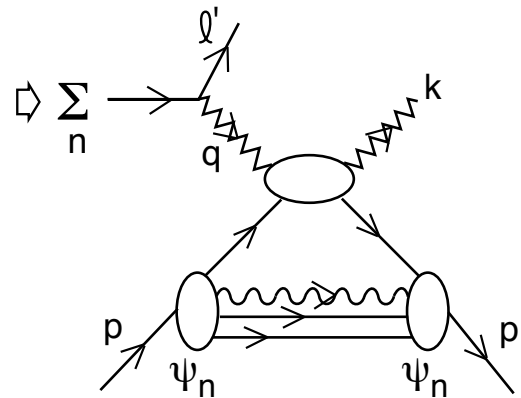
$$\langle p' \lambda' | J^\mu(z) J^\nu(0) | p \lambda \rangle$$

Large  $-q^2 = Q^2$

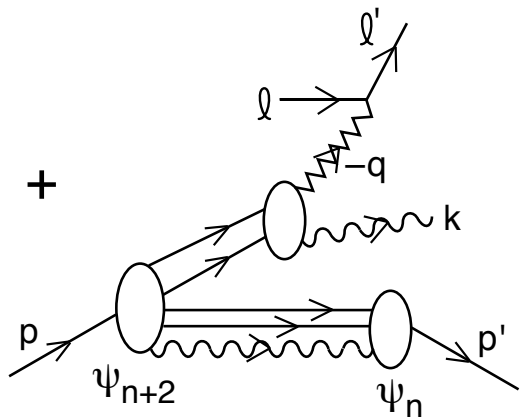


$$\gamma^* p \rightarrow \gamma p'$$

Given LFWFs,  
compute all  
GPDs !



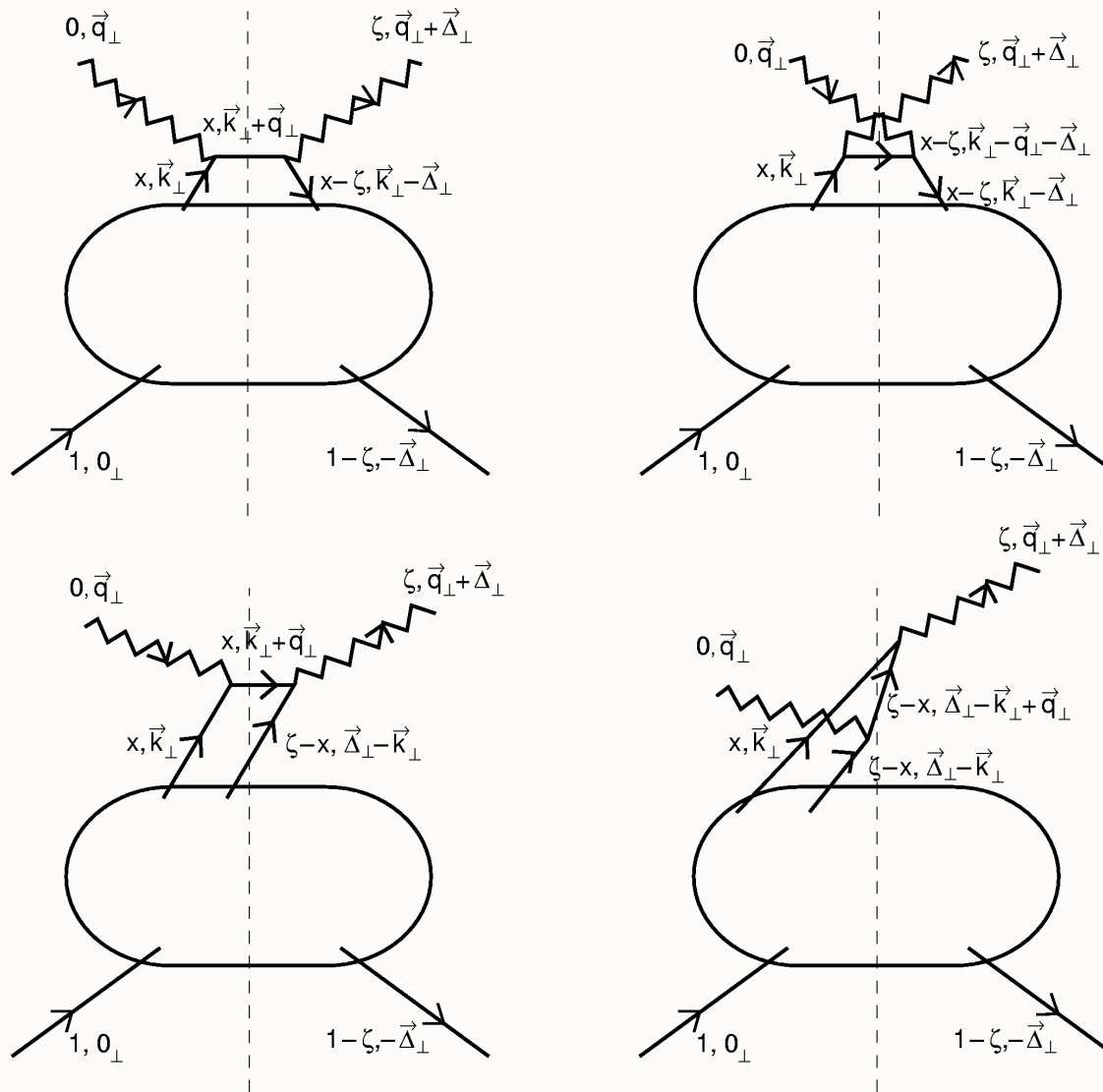
Deeply  
Virtual  
Compton  
Scattering



$$n = n' + 2$$

ERBL Evolution

Required for  
Lorentz Invariance



Light-cone wavefunction representation of deeply virtual Compton scattering <sup>☆</sup>

Stanley J. Brodsky <sup>a</sup>, Markus Diehl <sup>a,1</sup>, Dae Sung Hwang <sup>b</sup>

# Example of LFWF representation of GPDs ( $n \Rightarrow n$ )

Diehl, Hwang, sjb

$$\begin{aligned} & \frac{1}{\sqrt{1-\zeta}} \frac{\Delta^1 - i\Delta^2}{2M} E_{(n \rightarrow n)}(x, \zeta, t) \\ &= (\sqrt{1-\zeta})^{2-n} \sum_{n, \lambda_i} \int \prod_{i=1}^n \frac{dx_i d^2\vec{k}_{\perp i}}{16\pi^3} 16\pi^3 \delta\left(1 - \sum_{j=1}^n x_j\right) \delta^{(2)}\left(\sum_{j=1}^n \vec{k}_{\perp j}\right) \\ & \quad \times \delta(x - x_1) \psi_{(n)}^{\uparrow*}(x'_i, \vec{k}'_{\perp i}, \lambda_i) \psi_{(n)}^{\downarrow}(x_i, \vec{k}_{\perp i}, \lambda_i), \end{aligned}$$

where the arguments of the final-state wavefunction are given by

$$\begin{aligned} x'_1 &= \frac{x_1 - \zeta}{1 - \zeta}, & \vec{k}'_{\perp 1} &= \vec{k}_{\perp 1} - \frac{1 - x_1}{1 - \zeta} \vec{\Delta}_{\perp} & \text{for the struck quark,} \\ x'_i &= \frac{x_i}{1 - \zeta}, & \vec{k}'_{\perp i} &= \vec{k}_{\perp i} + \frac{x_i}{1 - \zeta} \vec{\Delta}_{\perp} & \text{for the spectators } i = 2, \dots, n. \end{aligned}$$

# Example of LFWF representation of GPDs ( $n+1 \Rightarrow n-1$ )

Diehl, Hwang, sjb

Diehl, Kroll

$$\begin{aligned}
 & \frac{1}{\sqrt{1-\zeta}} \frac{\Delta^1 - i\Delta^2}{2M} E_{(n+1 \rightarrow n-1)}(x, \zeta, t) \\
 &= (\sqrt{1-\zeta})^{3-n} \sum_{n, \lambda_i} \int \prod_{i=1}^{n+1} \frac{dx_i d^2\vec{k}_{\perp i}}{16\pi^3} 16\pi^3 \delta\left(1 - \sum_{j=1}^{n+1} x_j\right) \delta^{(2)}\left(\sum_{j=1}^{n+1} \vec{k}_{\perp j}\right) \\
 & \quad \times 16\pi^3 \delta(x_{n+1} + x_1 - \zeta) \delta^{(2)}(\vec{k}_{\perp n+1} + \vec{k}_{\perp 1} - \vec{\Delta}_{\perp}) \\
 & \quad \times \delta(x - x_1) \psi_{(n-1)}^{\uparrow*}(x'_i, \vec{k}'_{\perp i}, \lambda_i) \psi_{(n+1)}^{\downarrow}(x_i, \vec{k}_{\perp i}, \lambda_i) \delta_{\lambda_1 - \lambda_{n+1}},
 \end{aligned}$$

where  $i = 2, \dots, n$  label the  $n - 1$  spectator partons which appear in the final-state hadron wavefunction with

$$x'_i = \frac{x_i}{1-\zeta}, \quad \vec{k}'_{\perp i} = \vec{k}_{\perp i} + \frac{x_i}{1-\zeta} \vec{\Delta}_{\perp}.$$

# Link to DIS and Elastic Form Factors

DIS at  $\xi=t=0$

$$H^q(x,0,0) = q(x), \quad -\bar{q}(-x)$$

$$\tilde{H}^q(x,0,0) = \Delta q(x), \quad \Delta \bar{q}(-x)$$

Form factors (sum rules)

$$\int_{-1}^1 dx \sum_q [H^q(x, \xi, t)] = F_1(t) \text{ Dirac f.f.}$$

$$\int_{-1}^1 dx \sum_q [E^q(x, \xi, t)] = F_2(t) \text{ Pauli f.f.}$$

$$\int_{-1}^1 dx \tilde{H}^q(x, \xi, t) = G_{A,q}(t), \quad \int_{-1}^1 dx \tilde{E}^q(x, \xi, t) = G_{P,q}(t)$$



$$H^q, E^q, \tilde{H}^q, \tilde{E}^q(x, \xi, t)$$

Verified using  
LFWFs  
Diehl, Hwang, sjb

Quark angular momentum (Ji's sum rule)

$$J^q = \frac{1}{2} - J^G = \frac{1}{2} \int_{-1}^1 x dx [H^q(x, \xi, 0) + E^q(x, \xi, 0)]$$

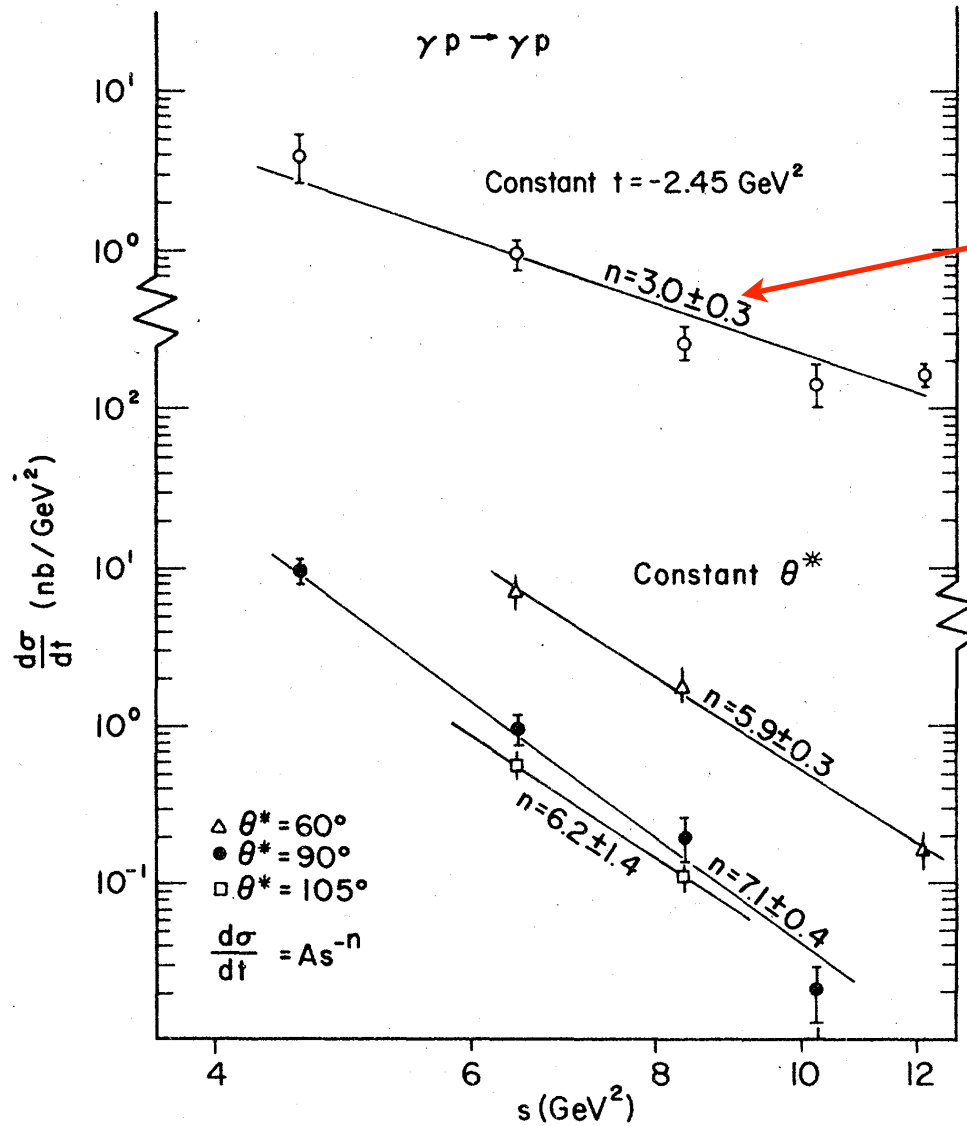
X. Ji, Phy.Rev.Lett.78,610(1997)

# J=0 Fixed pole in real and virtual Compton scattering

Damashek, Gilman;  
Close, Gunion, sjb

- Effective two-photon contact term
- Seagull for scalar quarks
- Real phase
- $M = s^0 F(t)$
- Independent of  $Q^2$  at fixed  $t$
- $\langle I/x \rangle$  Moment: Related to Feynman-Hellman Theorem
- Fundamental test of local gauge theory

$$\text{Test J=0 Fixed Pole: } s^2 \frac{d\sigma}{dt}(\gamma p \rightarrow \gamma p) \approx F_0^2(t)$$



J=0 fixed pole:  
Predict n=2

Cornell

Compton-scattering cross sections at constant  $t$  and at constant  $\theta^*$ . The straight lines are fits to the data. The fits shown here have no energy cuts.

# Key QCD Experiment at GSI

- Test DVCS in Timelike Regime  $\bar{p}p \rightarrow \gamma^* \gamma$
- J=0 Fixed pole  $q^2$  independent
- Analytic Continuation of GPDs
- Light-Front Wavefunctions
- charge asymmetry from interference

$$\bar{p}p \rightarrow \gamma^* \rightarrow l^+ l^- \rightarrow l^+ l^- \gamma \quad \bar{p}p \rightarrow \bar{p}p \gamma \rightarrow \gamma^* \gamma \rightarrow l^+ l^- \gamma$$



# AdS/QCD

- Only one scale  $\Lambda_{QCD}$  determines hadronic spectrum (slightly different for mesons and baryons).
- Ratio of Nucleon to Delta trajectories determined by zeroes of Bessel functions.
- String modes dual to baryons extrapolate to three fermion fields at zero separation in the AdS boundary.
- Only dimension 3,  $\frac{9}{2}$  and 4 states  $\bar{q}q$ ,  $qqq$ , and  $gg$  appear in the duality at the classical level!
- Non-zero orbital angular momentum and higher Fock-states require introduction of quantum fluctuations.
- Simple description of space and time-like structure of hadronic form factors.
- Dominance of quark-interchange in hard exclusive processes emerges naturally from the classical duality of the holographic model. Modified by gluonic quantum fluctuations.
- Covariant version of the bag model with confinement and conformal symmetry.

# Essential to test QCD

- J-PARC
- GSI antiprotons
- 12 GeV Jlab
- BaBar/Belle: ISR, two-gamma, timelike DVCS
- RHIC/LHC Nuclear Collisions; LHCb
- electron-proton, electron-nucleus collisions

# Novel Tests of QCD at GSI

Polarized antiproton Beam      Secondary Beams

- Characteristic momentum scale of QCD: 300 MeV
- Many Tests of AdS/CFT predictions possible
- Exclusive channels: Conformal scaling laws, quark-interchange
- $\bar{p}p$  scattering: fundamental aspects of nuclear force
- Color transparency: Coherent color effects
- Nuclear Effects, Hidden Color, Anti-Shadowing
- Anomalous heavy quark phenomena
- Spin Effects:  $A_N, A_{NN}$